

# Water Isotopes in Spatial Hydrology

Gabe Bowen

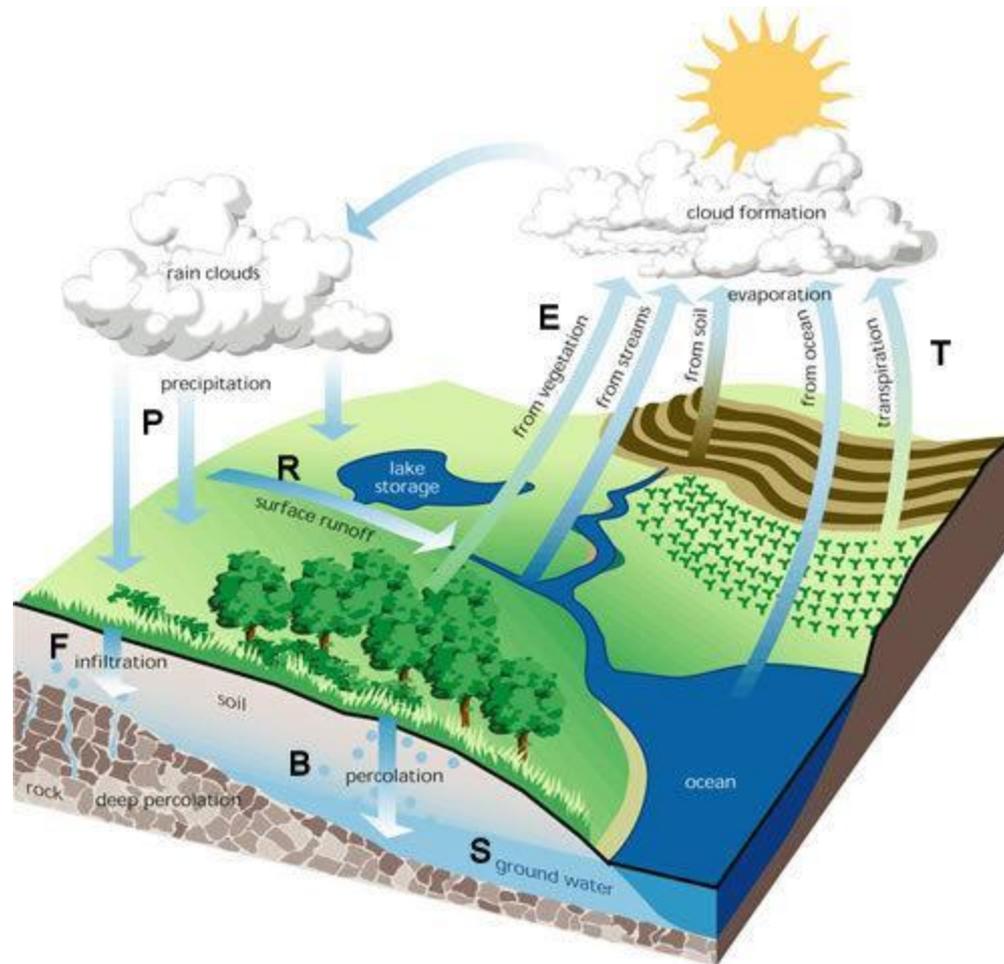
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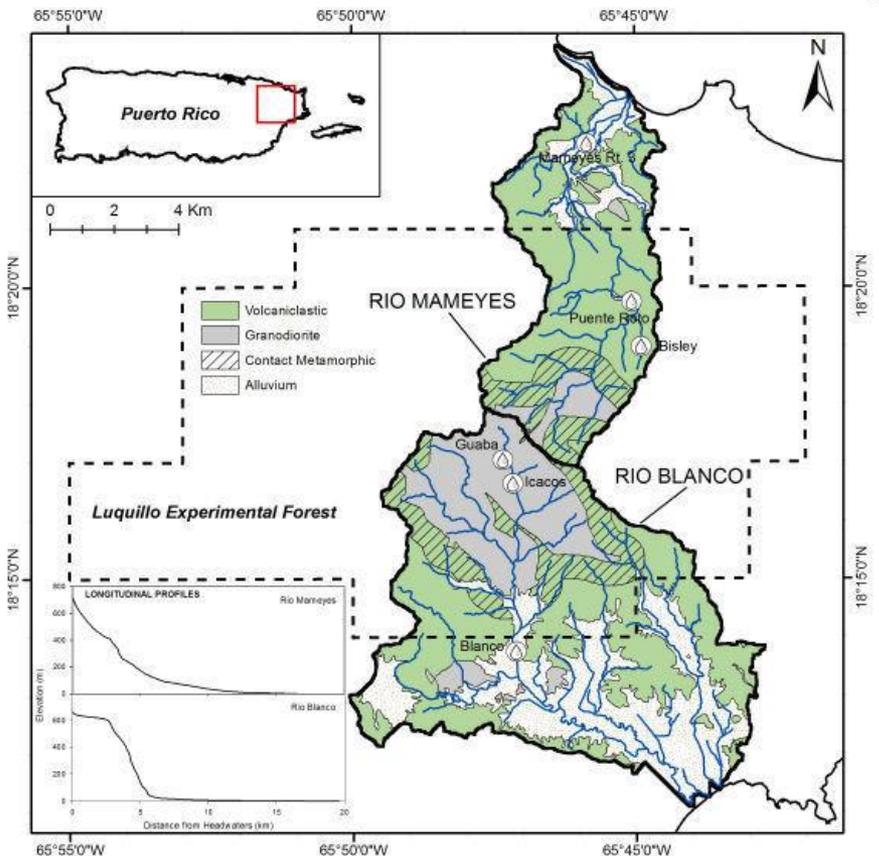
# Isotopes can be used to...

- ⊕ Trace mass fluxes
- ⊕ Identify and partition processes
- ⊕ Infer conditions

# Catchment water balance



$$P = R + E + T + \Delta S$$

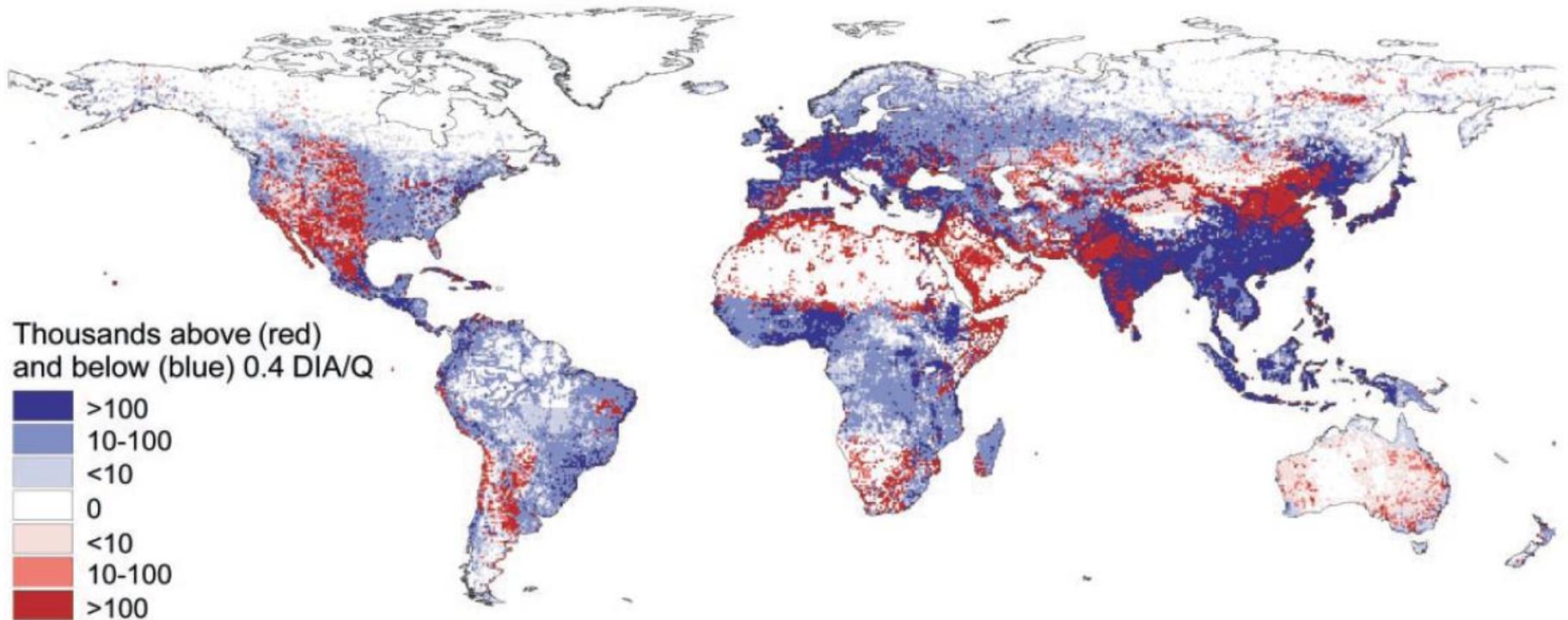


# 9 ideas

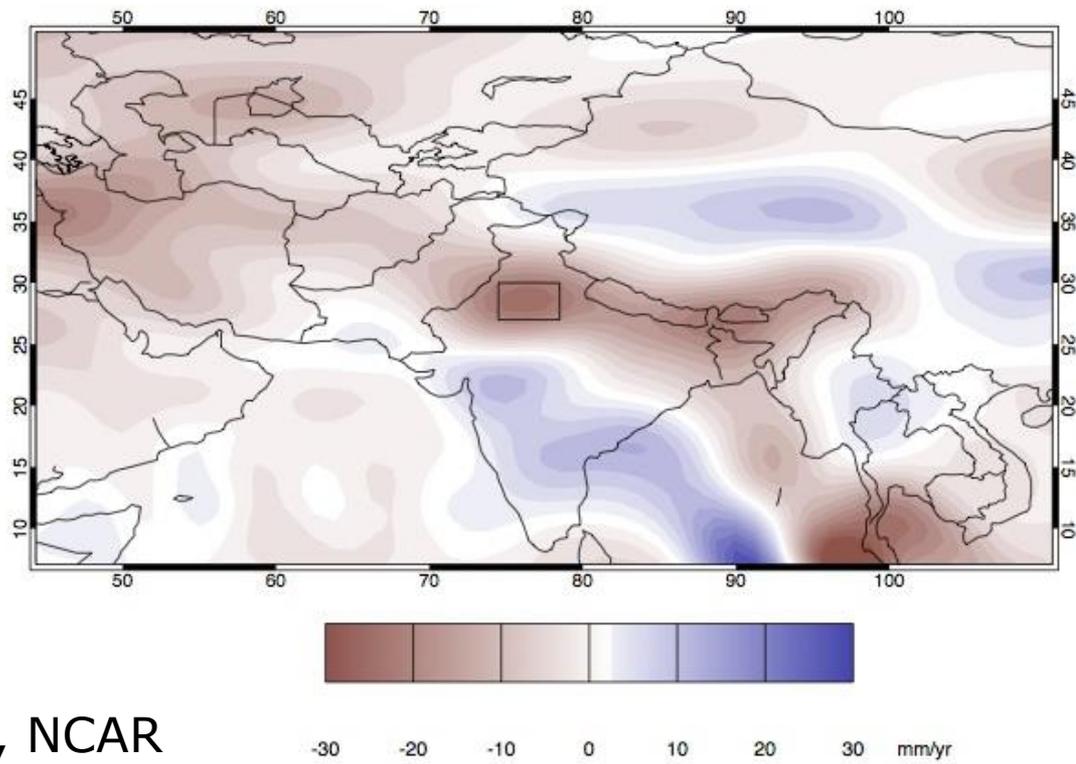
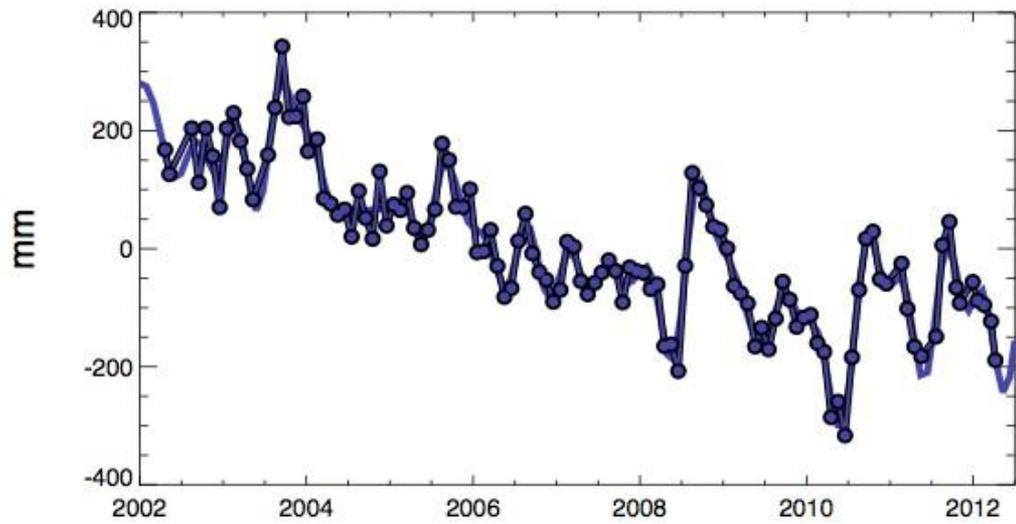
1. Water balance matters
2. It all starts with precipitation (isoscapes)
3. Interpolating in space and time
4. Most headwater catchments export old water
5. Urban and agricultural systems do not (always)
6. Groundwater looks like local precipitation, except when it isn't
7. Regional water balance trends are easy to extract from rivers
8. Lake basins evaporate, but even more they transpire
9. The water we drink often comes a long way to reach us

# 1. Water balance matters

Contemporary Population Relative to Demand per Discharge  
Stress Threshold ( $DIA/Q = 0.4$ )

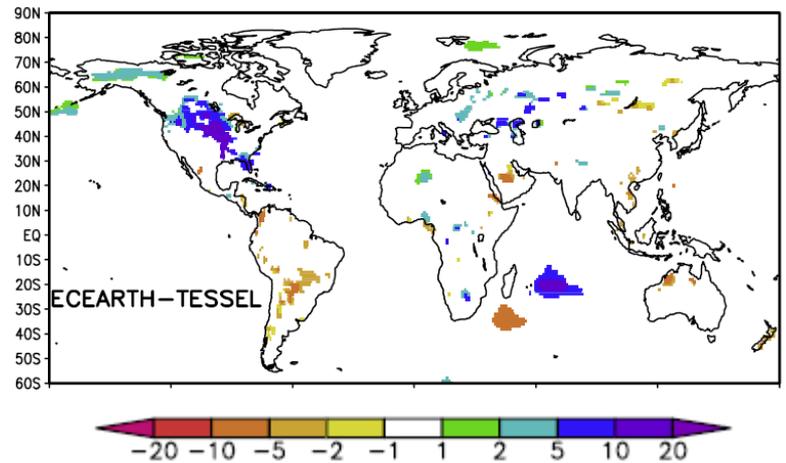
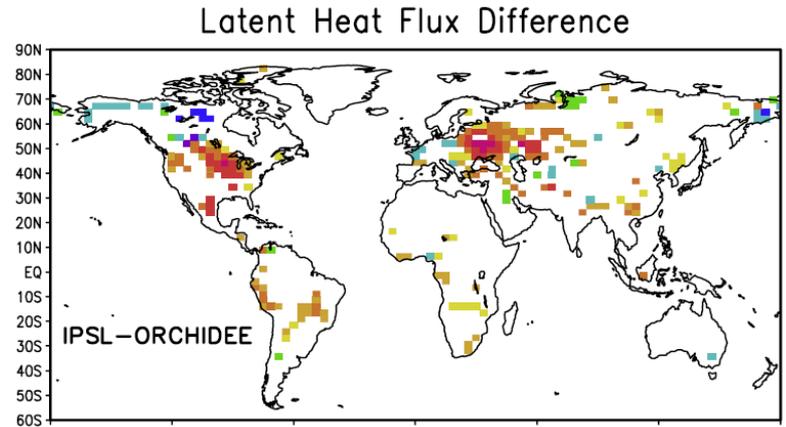
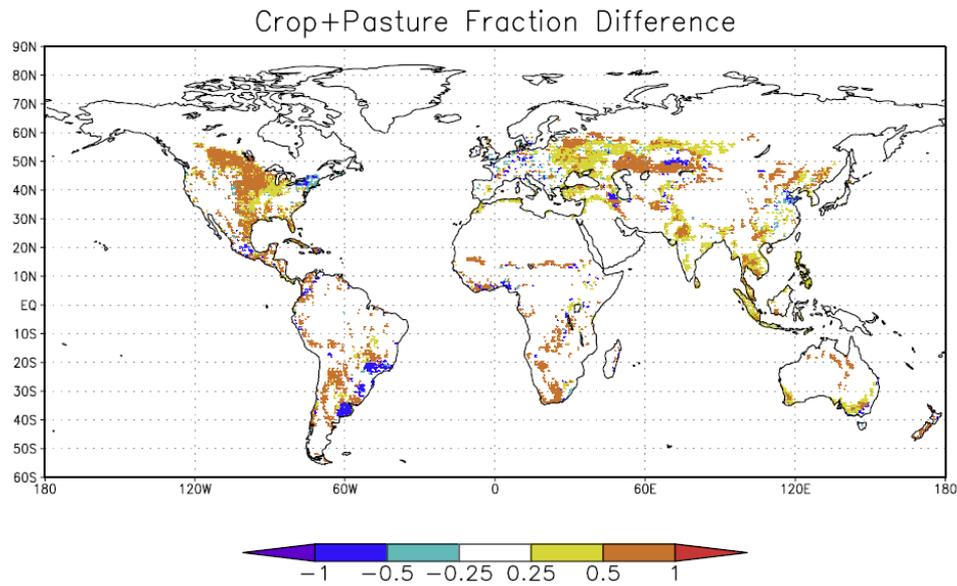


# GRACE Total Water Storage - Northern India



Sean Swenson, NCAR

# Water balance matters

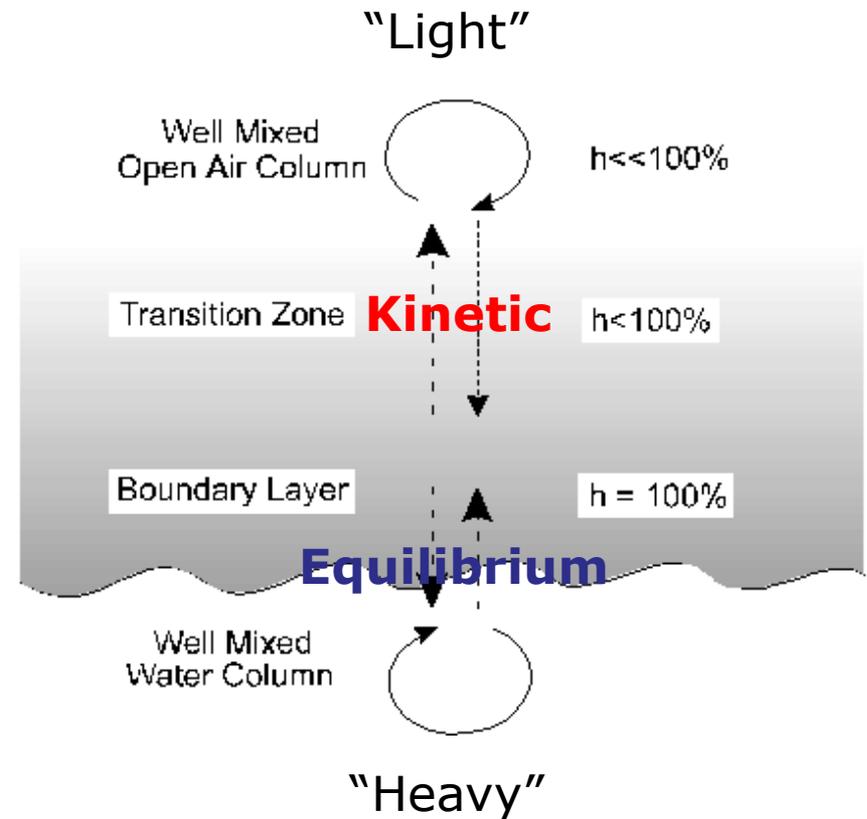


## 2. It all starts with precipitation (isoscapes)

- ⊕ First, some fundamentals!
- ⊕ What is the most important process leading to H and O isotope variation in water?
  1. Evaporation (condensation)
  2. Transport

# Phase Change Reaction: Craig-Gordon

- ⊕ Open air
  - ⊕ Well-mixed
  - ⊕ Large
- ⊕ Transition zone (TZ)
  - ⊕ Turbulently mixed
  - ⊕ Decreasing humidity upwards
- ⊕ Boundary layer (BL)
  - ⊕ Thin, well-mixed layer
  - ⊕ 100% RH
- ⊕ Liquid
  - ⊕ Large (ocean) or small (droplet) body of water
  - ⊕ Mixed or stratified



$$\delta_e = \frac{\alpha^* \delta_l + \varepsilon^* - h \delta_a - \Delta \varepsilon}{1 - h}$$

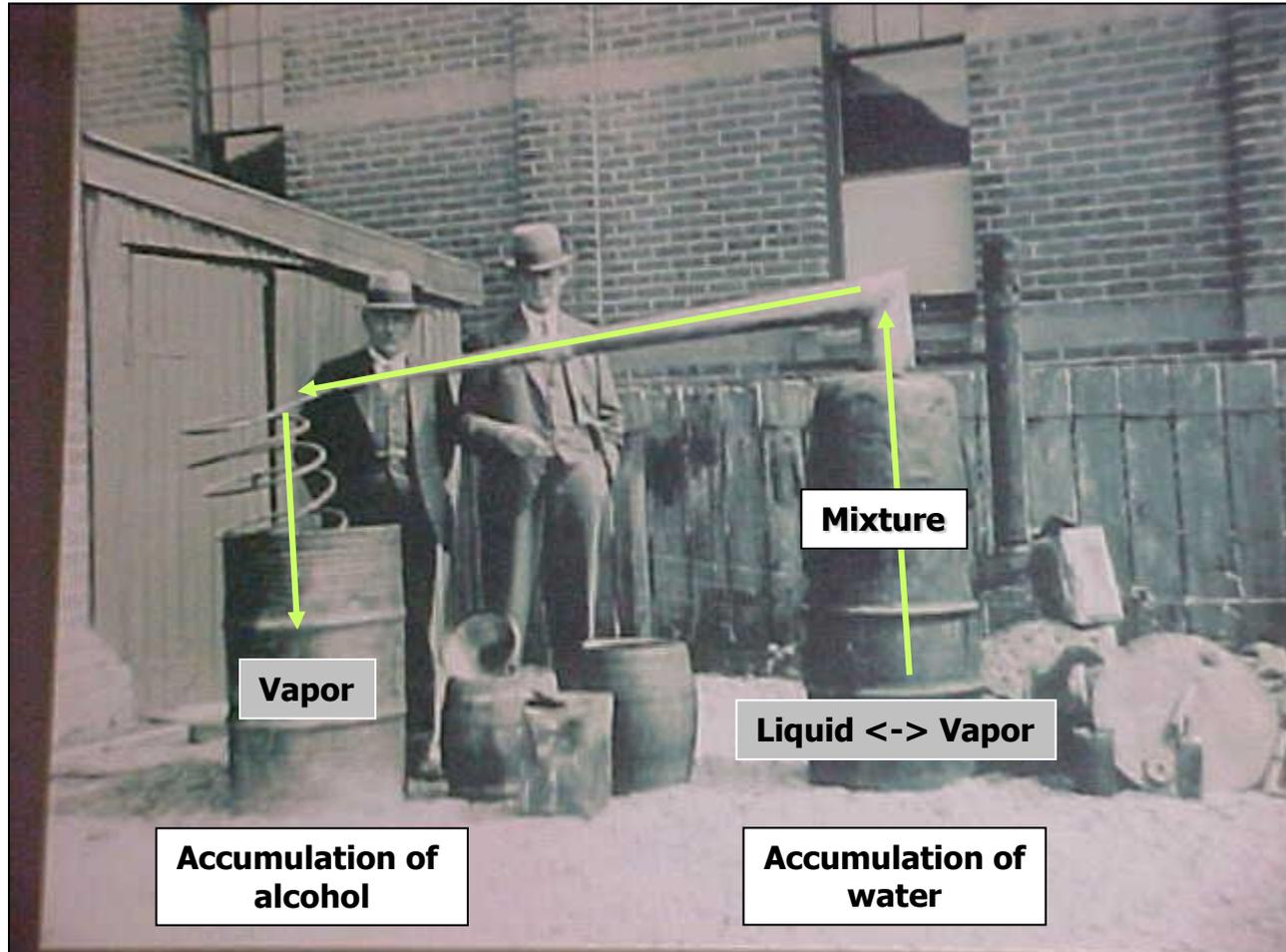
# Rayleigh Distillation

- ⊕ A processes by which fractionation (of isotopes, elements, molecules, elephants) leads to a change in 2-component reactant mixture
- ⊕ Is it Rayleigh Distillation?
  - ⊕ Open system
    - No addition of material
    - Rapidly and continuous removal of product
  - ⊕ Product is fractionated relative to the reactant
- ⊕ The Rayleigh equation describes the composition of the reactant pool as a function of reaction progress:

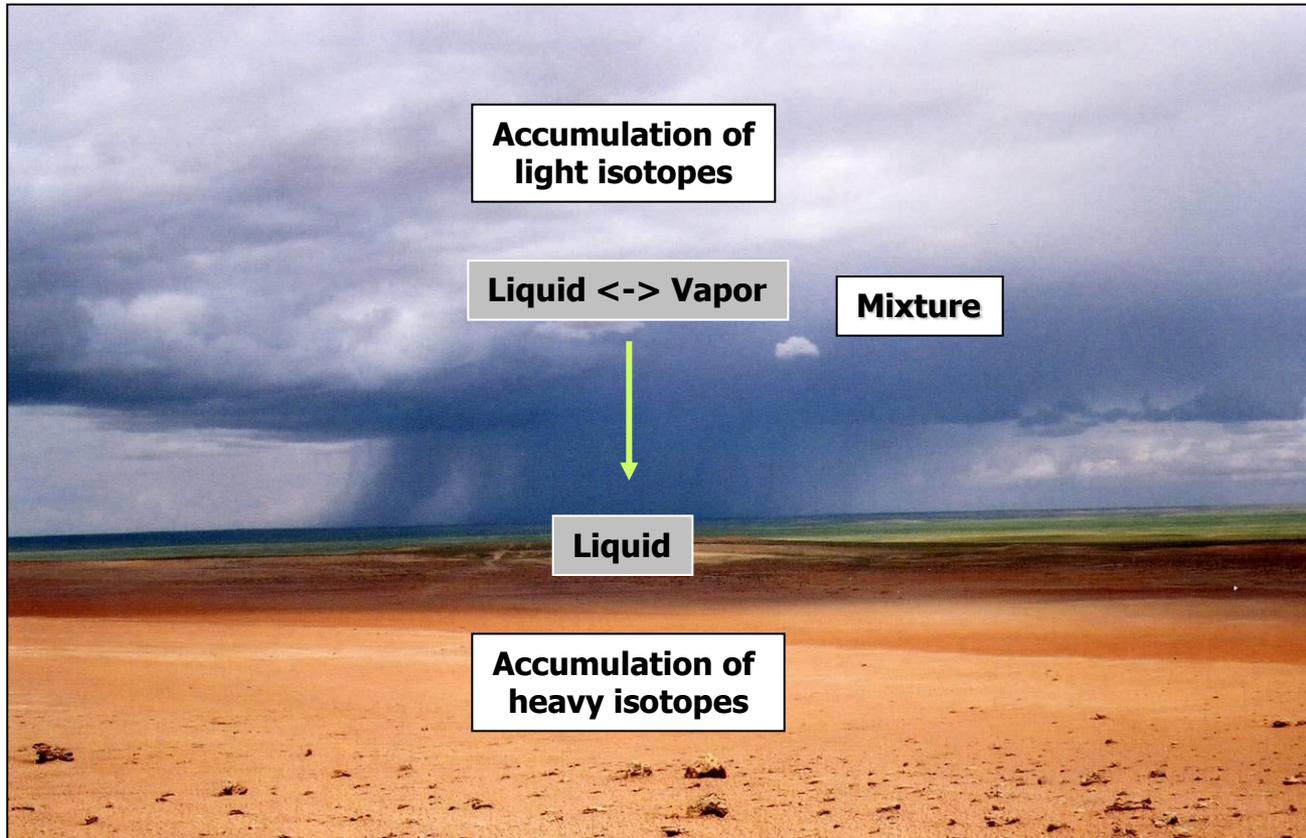
$$R = R_0 f^{(\alpha - 1)}$$

**$R$  and  $R_0$  are current and initial isotope ratios**  
 **$f$  is fraction of reactant remaining**

# Rayleigh Distillation

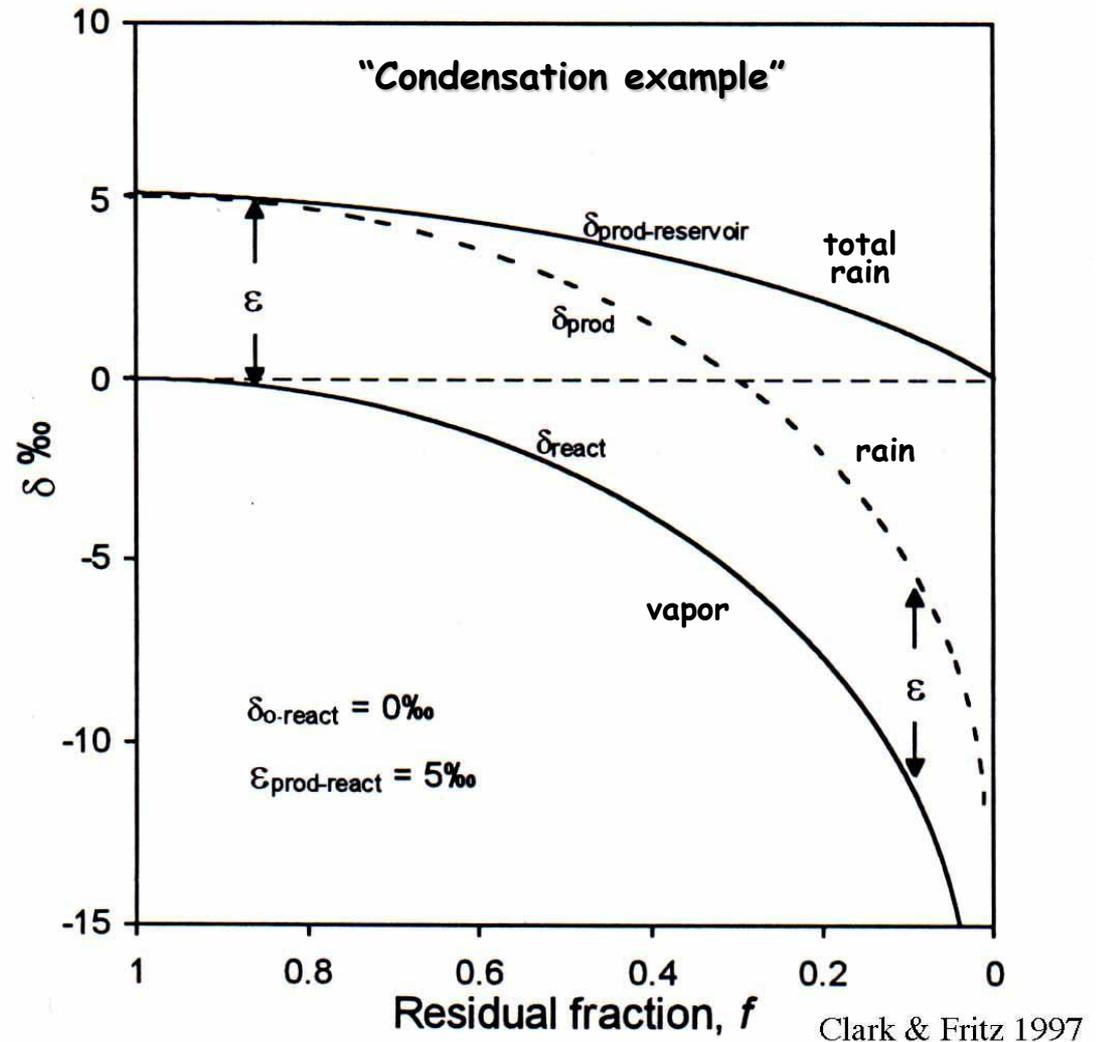


# Rayleigh Distillation



# Rayleigh Distillation and Precipitation

- Precipitation formed from condensation of cloud vapor
- Equilibrium process (free atmosphere RH  $\approx 100\%$ )
  - Equilibrium fractionation
- **But one element of complexity...**

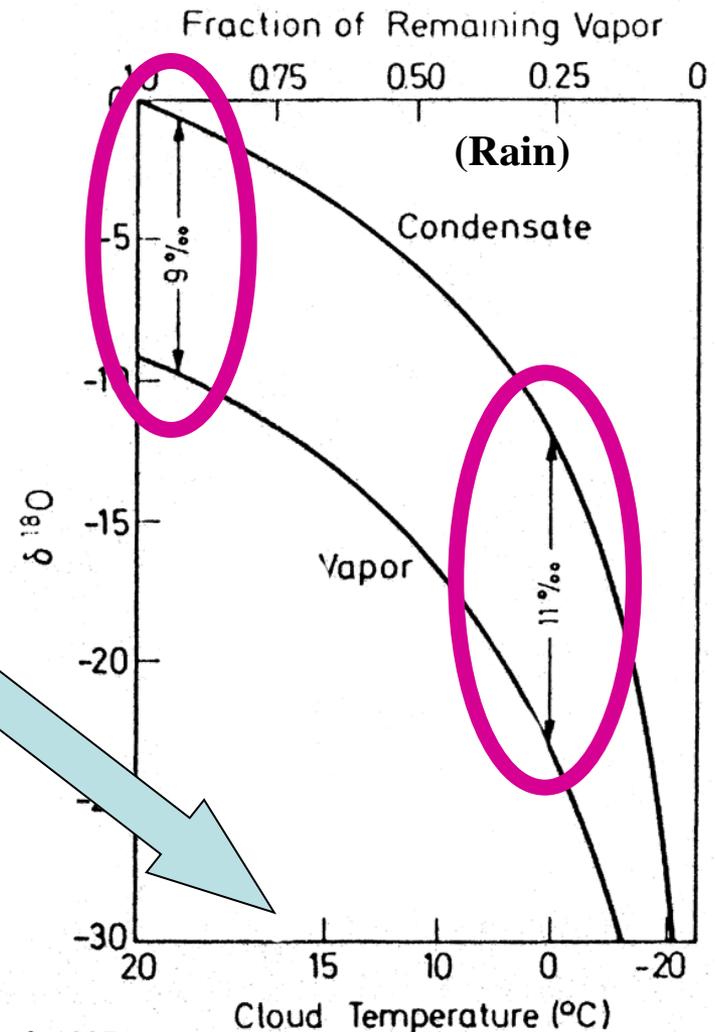


# Rayleigh Distillation and Precipitation

*!!! This does not cause the 'temperature effect', but it contributes (slightly) to it !!!*

As condensation proceeds, the temperature of the remaining cloud decreases.

Thus,  $\alpha$  increases, resulting in a greater difference between cloud and rain  $H_2O$



# Spatial Patterns and Rayleigh Distillation

- ⊕ Rayleigh distillation causes precipitation isotope ratios to get **lower** as air gets **drier**

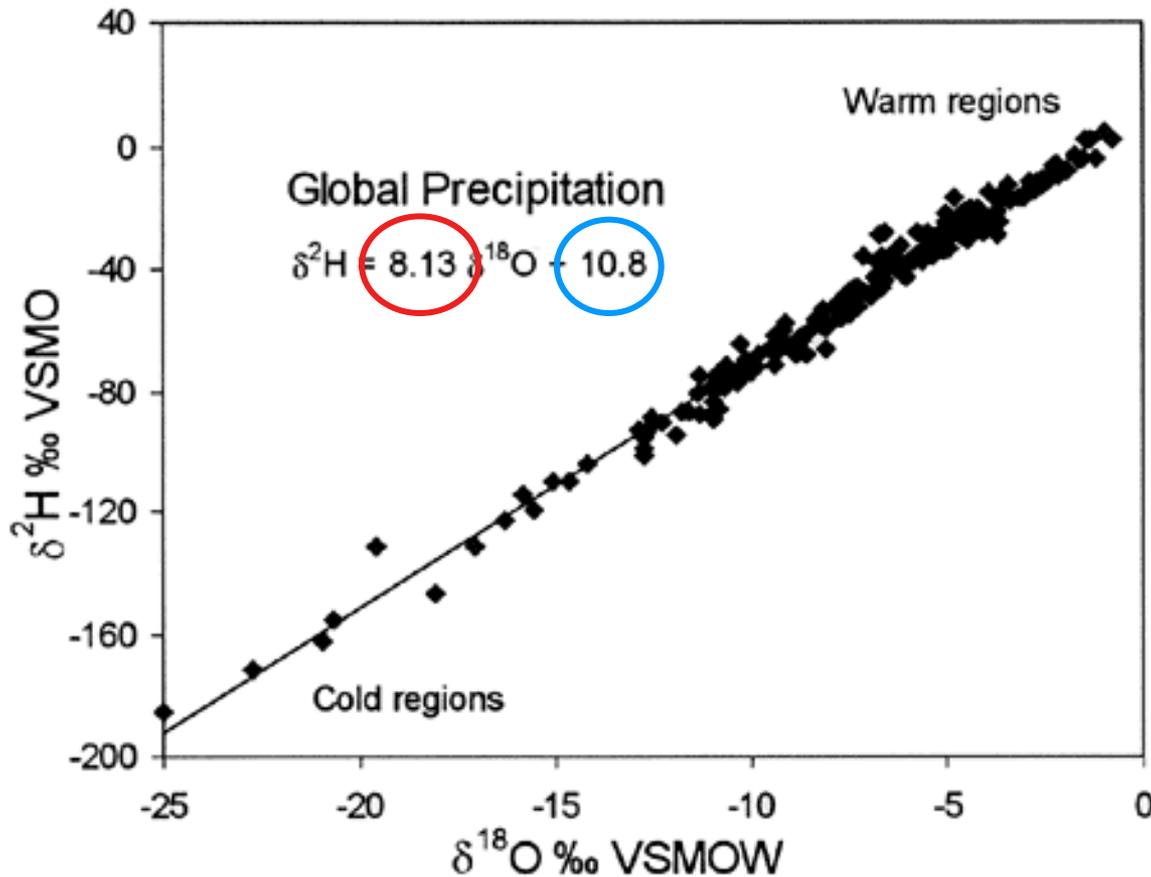
*What does this imply about the spatial distribution of precipitation isotope ratios?*

# Equilibrium fractionation factors for water isotopes

- ⊕ at 20° C
  - ⊕  $\epsilon^{2\text{H}} = 74\text{‰}$
  - ⊕  $\epsilon^{18\text{O}} = 9.2\text{‰}$
  - ⊕  $\epsilon^{2\text{H}} / \epsilon^{18\text{O}} = 8.0$
- ⊕ at 80° C
  - ⊕  $\epsilon^{2\text{H}} = 38\text{‰}$
  - ⊕  $\epsilon^{18\text{O}} = 4.5\text{‰}$
  - ⊕  $\epsilon^{2\text{H}} / \epsilon^{18\text{O}} = 8.4$

**Equilibrium enrichment factors for H isotopes are ~8 x those for O isotopes**

# The Global Meteoric Water Line



Condensation  
is an equilibrium process

so

Most precipitation  $\delta$  values  
lie along a Global Meteoric  
Water Line (GMWL) of  
slope 8

$$(\epsilon^2\text{H} / \epsilon^{18}\text{O} = 8)$$

The intercept of the  
GMWL is +10‰

# Equilibrium and kinetic enrichment factors

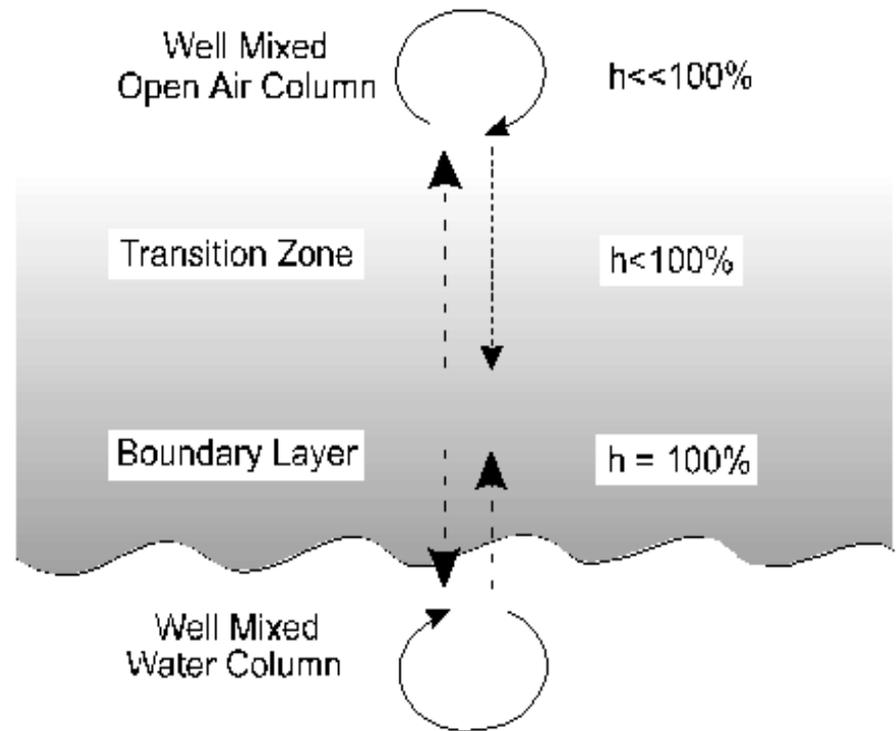
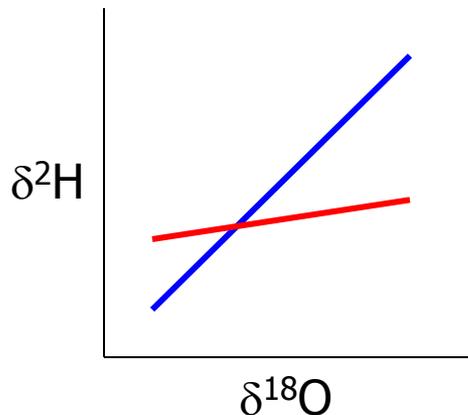
Q: What was the relationship between  $\epsilon_e^{2\text{H}}$  and  $\epsilon_e^{18\text{O}}$ ?

A:  $\epsilon_e^{2\text{H}} / \epsilon_e^{18\text{O}} = 8$

$\Delta\epsilon^{2\text{H}}$  and  $\Delta\epsilon^{18\text{O}}$  give us a different relationship

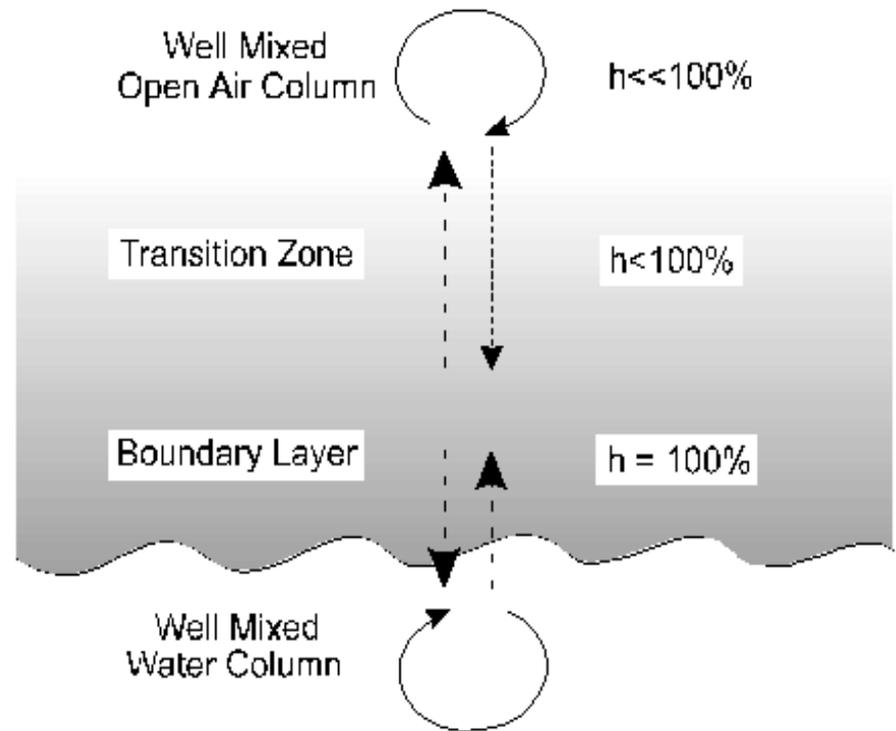
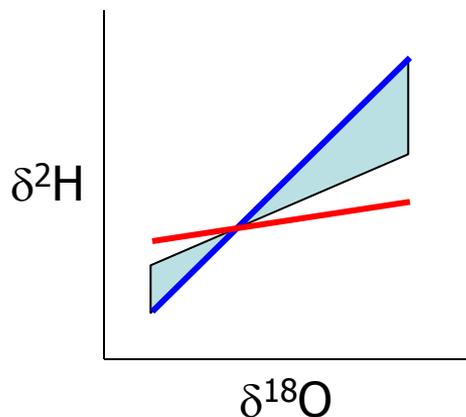
Kinetic  
 $\alpha^{2\text{H}} \approx \alpha^{18\text{O}}$

Equilibrium  
 $\alpha^{2\text{H}} = 8 * \alpha^{18\text{O}}$

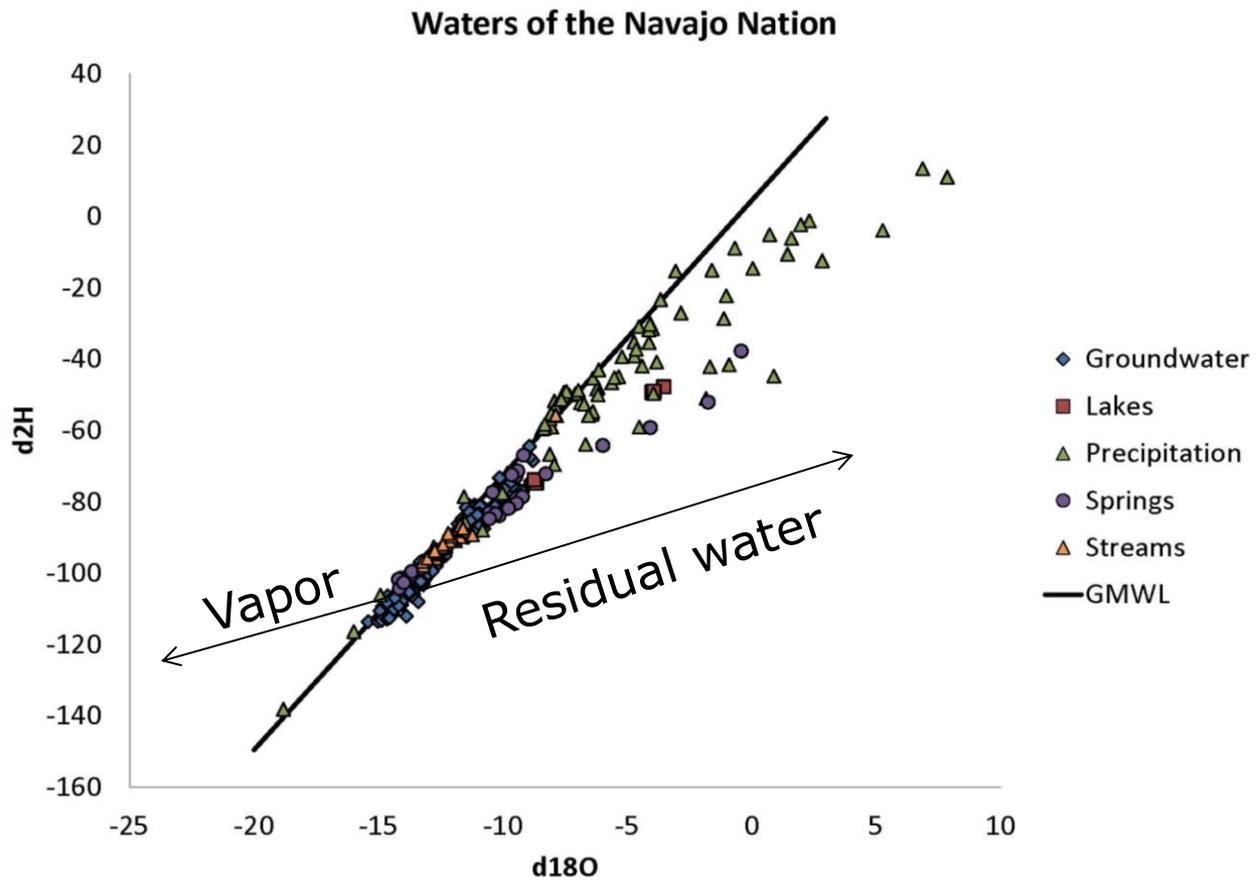


# Equilibrium and kinetic enrichment factors

- ⊕ The net ratio of  $^2\text{H}$  and  $^{18}\text{O}$  isotope effects is a blend of the Equilibrium and Kinetic ratios, typically between 3 and 8
- ⊕ The coupled  $^2\text{H}/^{18}\text{O}$  system gives us a “proxy” for kinetic fractionation...  
**deuterium excess**

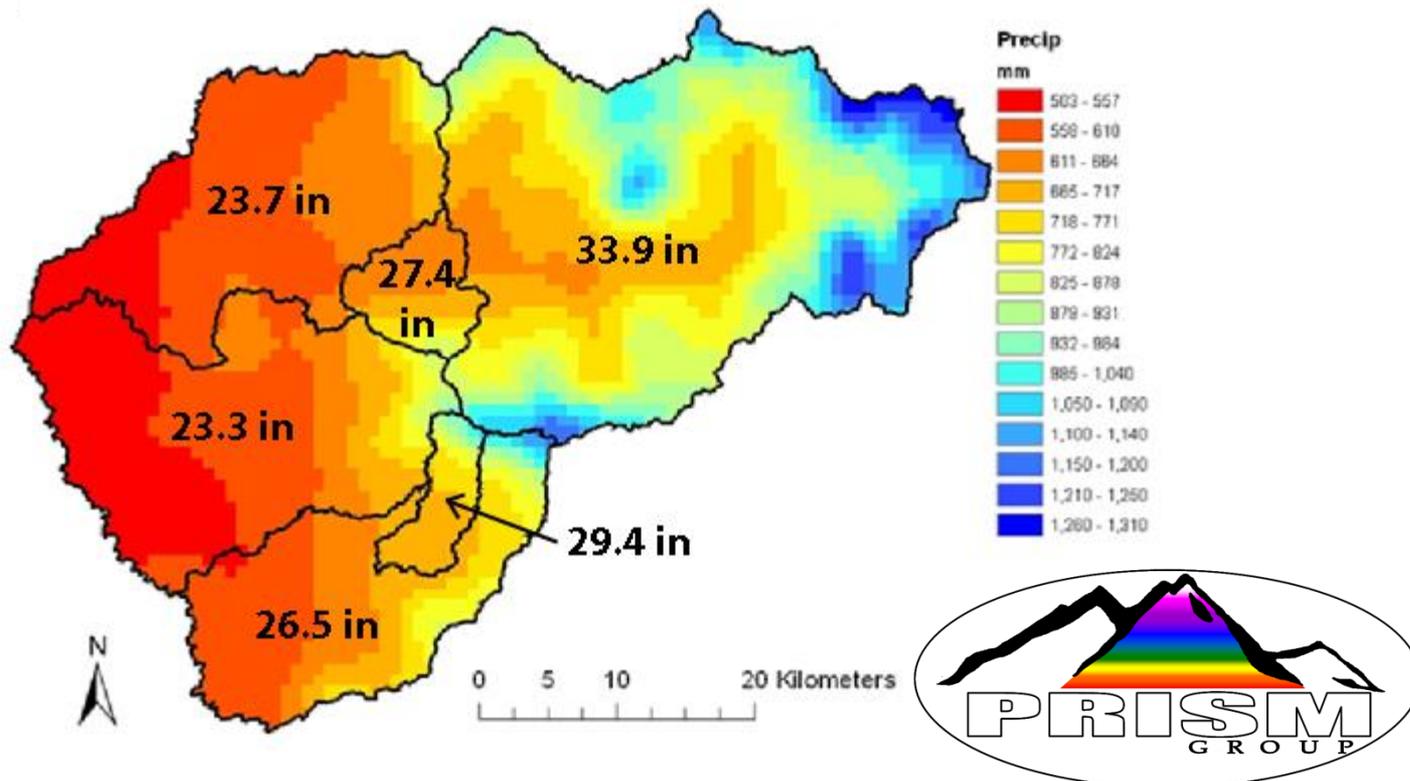


# Deuterium excess



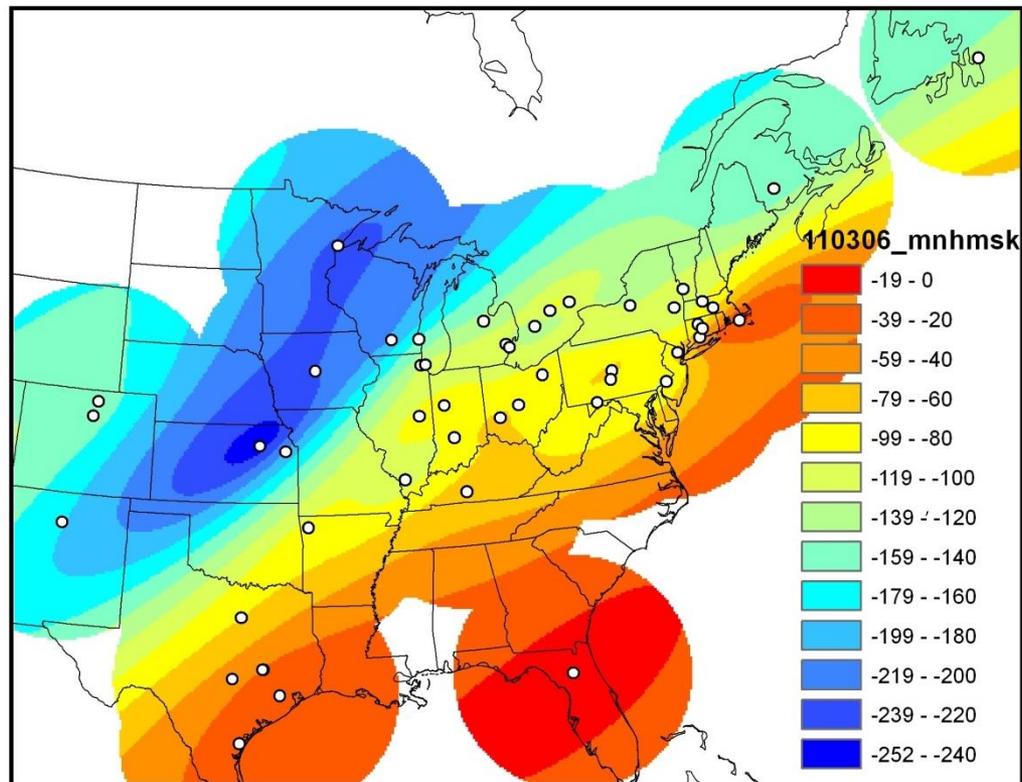
# Precipitation isoscapes

- ✦ Precipitation is an incompletely observed, spatially distributed flux
- ✦ Interpolating (extrapolating) from point measurements requires robust algorithms, consideration of process



# Precipitation isoscapes

- ⊕ What about precipitation isotope ratios?
  - ⊕ + Ratio of fluxes
  - ⊕ - Relatively poorly observed



# Spatial interpolation

- ⊕ Given spatially distributed data  $Z(x_i)$ , estimate the unknown value  $z(x_0)$  as a weighted average of  $Z(x_i)$

$$z(x_0) = \sum_{i=0}^n w_i(x_0) \times Z(x_i)$$

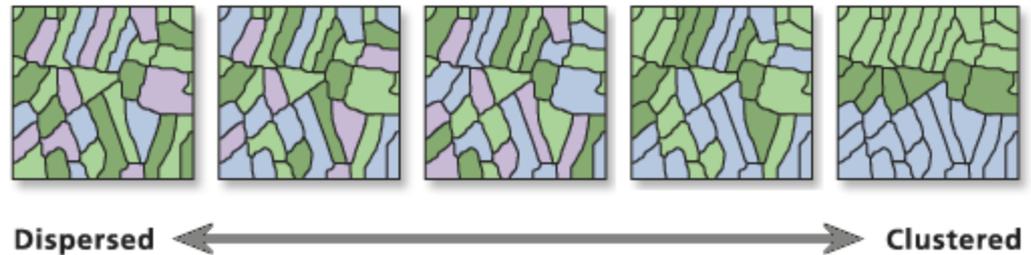
- ⊕ Challenge is in the determination of a model for  $w_i(x_0)$
- ⊕ General concepts/assumptions
  - ⊕ Spatial autocorrelation – closely spaced points are closely related
  - ⊕ Stationarity – 1°: expected mean and/or variance of the population of true values invariant over domain; 2°: spatial correlation structure invariant over domain

# Testing spatial autocorrelation

- ⊕ Are closely spaced values *more similar* than distantly spaced ones?

- ⊕ *More dissimilar?*

- ⊕ *Neither?*



- ⊕ Moran's I statistic (global):

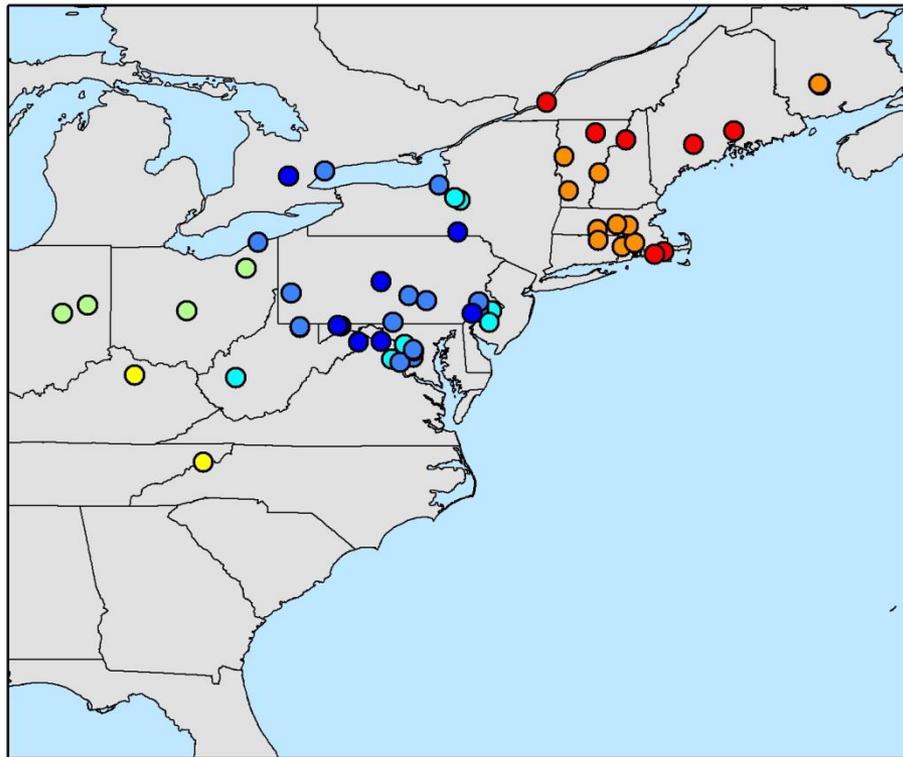
$$I = \frac{n \sum_{i=1}^n \sum_{j=1}^n w_{i,j} \Delta z_i \Delta z_j}{S_0 \sum_{i=1}^n \Delta z_i^2}$$

$S_0$  = aggregate weight

$$\Delta z_i = z_i - \mu_z$$

- ⊕  $I = -1$  values spatially dispersed
- ⊕  $I = +1$  values spatially correlated

# Superstorm Sandy example



1031\_AM  
d2H

- -167.2 - -144.5
- -144.4 - -121.9
- -121.8 - -99.2
- -99.1 - -76.6
- -76.5 - -54.0
- -53.9 - -31.3
- -31.2 - -8.7

Moran's I = 0.90 (ID<sup>2</sup>)

Z = 13.8

p << 0.001

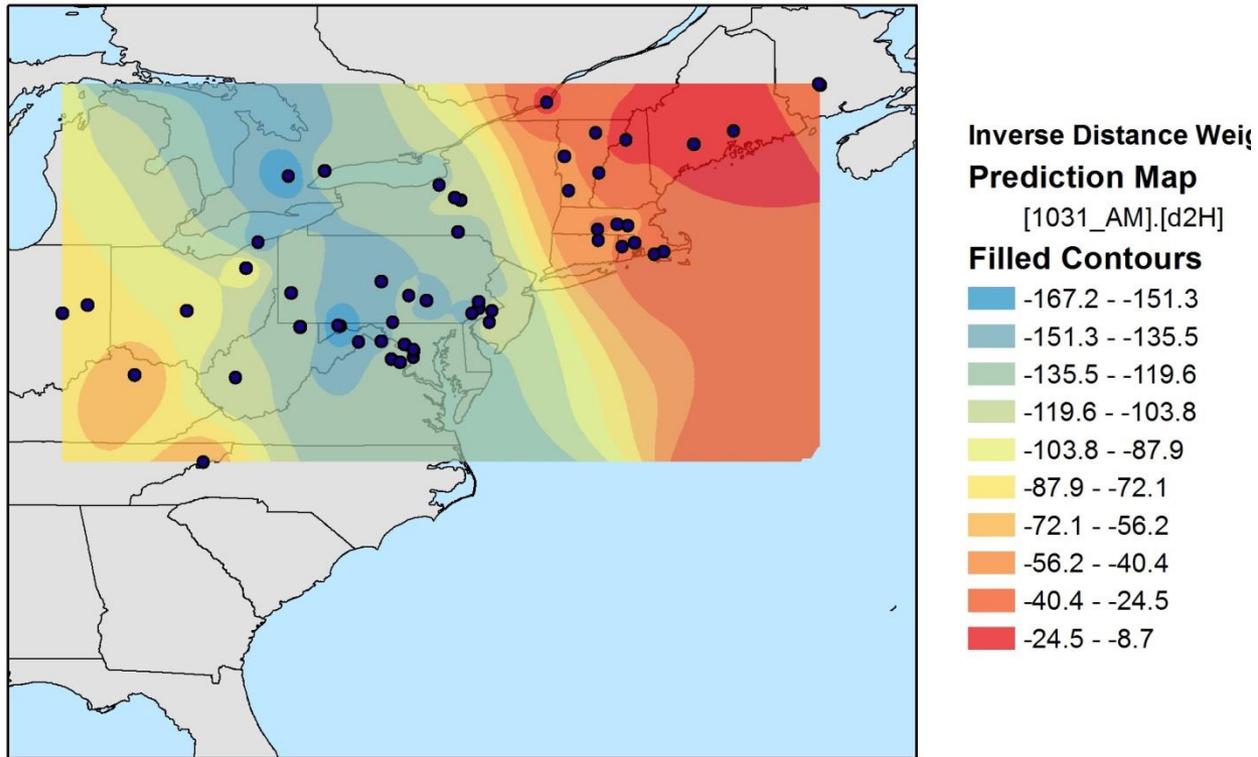
# Deterministic methods

- ⊕ Assume functional form of spatial correlation structure to calculate weights
- ⊕ Inverse distance

$$w_{i,j} = \left(\frac{1}{d}\right)^p$$

- ⊕  $p$  determines decay of weights with distance, can be assumed or optimized
- ⊕ Quick, easy, predictable
- ⊕ Arbitrary, prone to 'bulls eye' effects

# Inverse Distance



⊕ Optimized  $p = 2.8$

# Geostatistics - Kriging

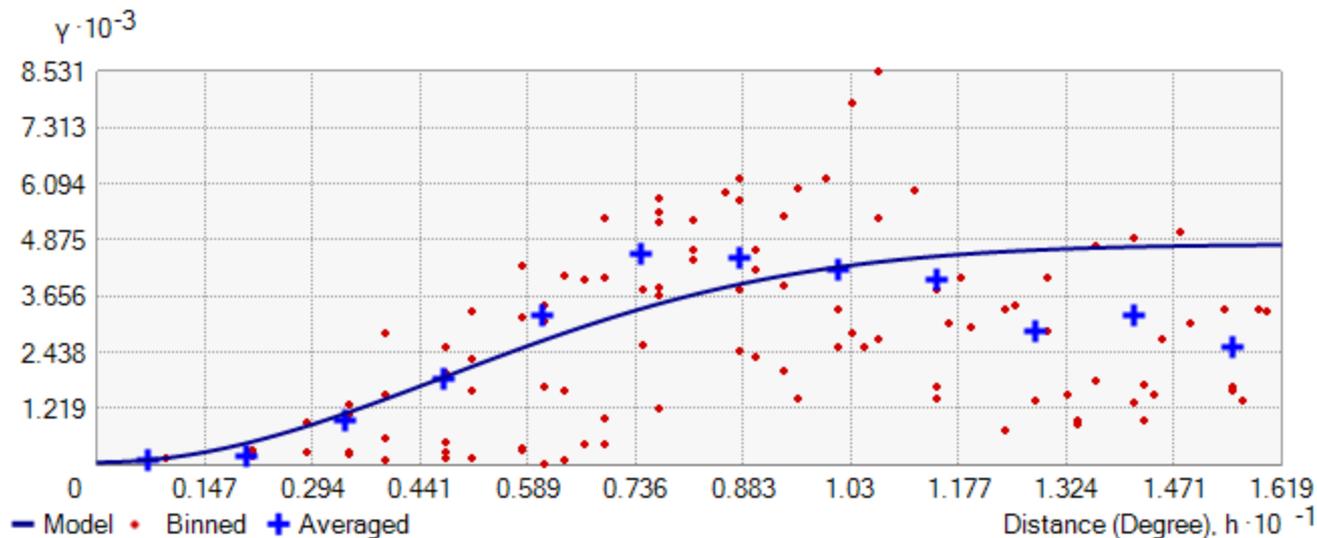
- ⊕ Use statistical properties of dataset to infer spatial correlation structure

$$y(x_i) = \mu + \varepsilon_i$$

- ⊕ Assume that  $y$  is the result of a random process with a mean  $\mu$  and spatially autocorrelated error  $\varepsilon_i$ 
  - ⊕ Data are  $n$  realizations
- ⊕ Assume 2nd order stationarity -> fit semivariogram model to observation
- ⊕ Various assumptions about  $\mu$ 
  - ⊕ 1st order stationarity + known (simple) or unknown (ordinary kriging)
  - ⊕ Non-stationary, deterministic (universal kriging)

# Sample and model semivariogram

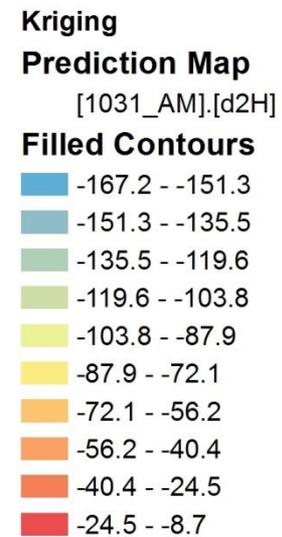
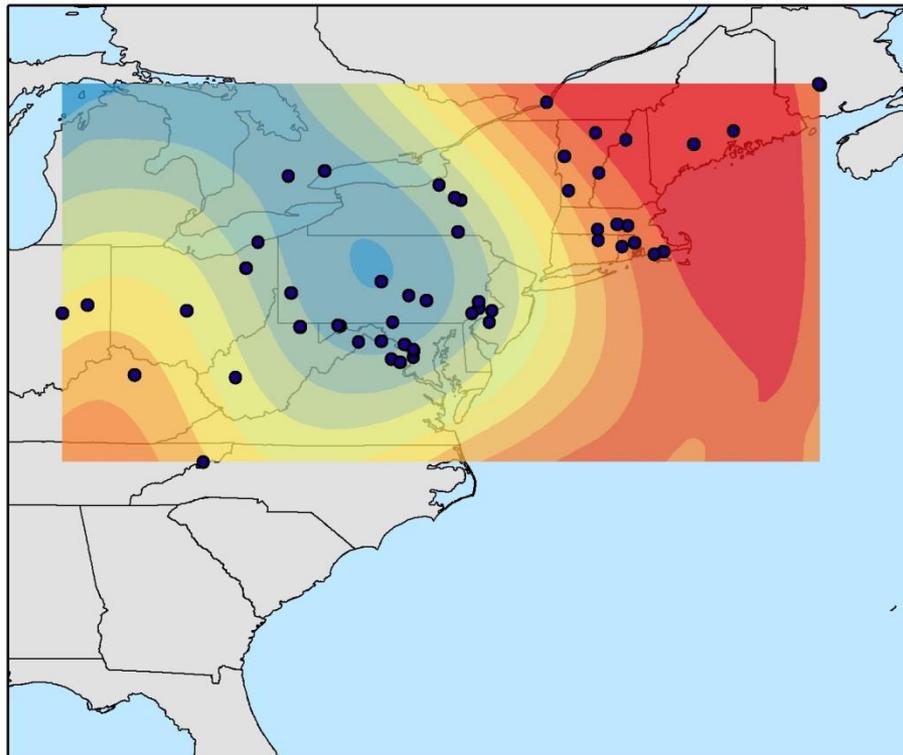
- Sample semivariogram: observed dissimilarity of values as a function of distance
- Semivariogram model: parametric function describing semivariance as function of distance
- The “art” of Kriging...although data can be used to optimize the semivariogram model you must choose the functional form



# Semivariogram models

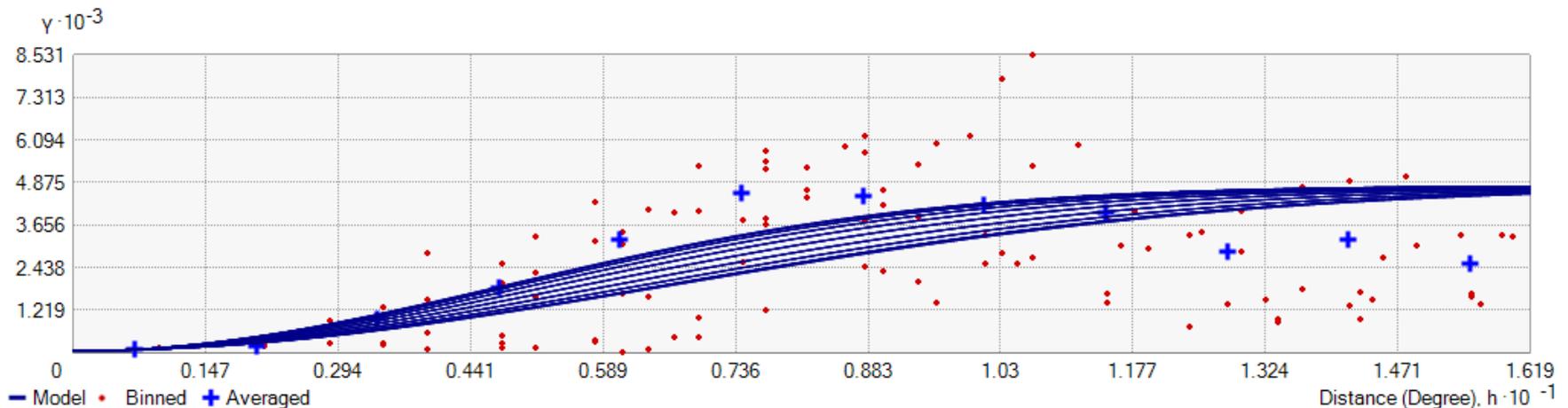
- ⊕ Common forms
  - ⊕ Matern
  - ⊕ Spherical
  - ⊕ Gaussian
- ⊕ Parameters (varies with form)
  - ⊕ Range: Decay with distance
  - ⊕ Sill: Maximum semivariance for values at distant points
  - ⊕ Nugget: Semivariance at semivariogram intercept (measurement error or heterogeneity)
  - ⊕ Shape: Rate of weight decay with distance

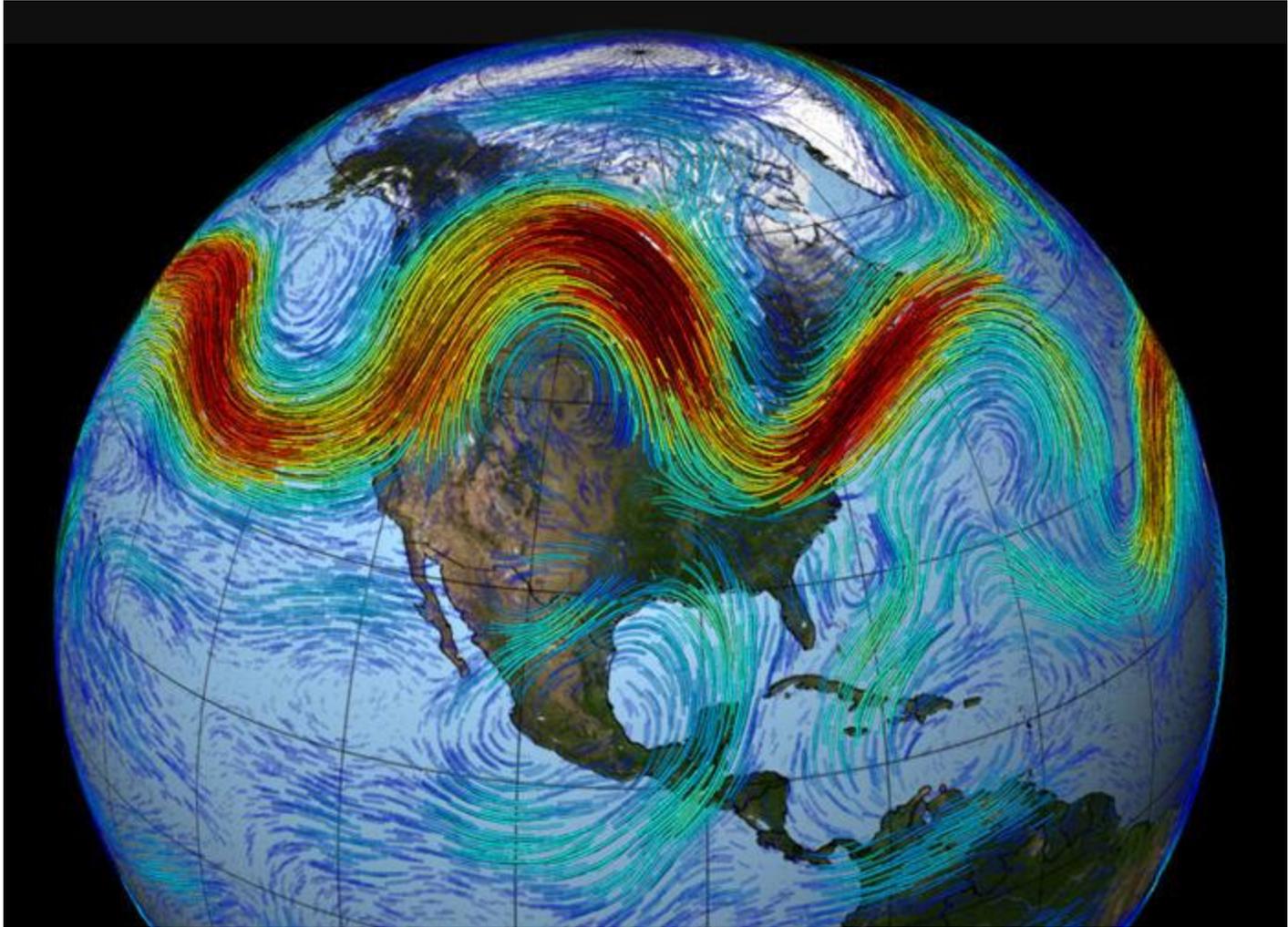
# Ordinary Kriging



# Anisotropy

- ⊕ Spatial relationships are often directional
- ⊕ Including anisotropy factor allows you to 'transform' spatial domain to regularize system geometry
- ⊕ Alternative (non-Euclidean) geometries are possible, but not supported in standard software

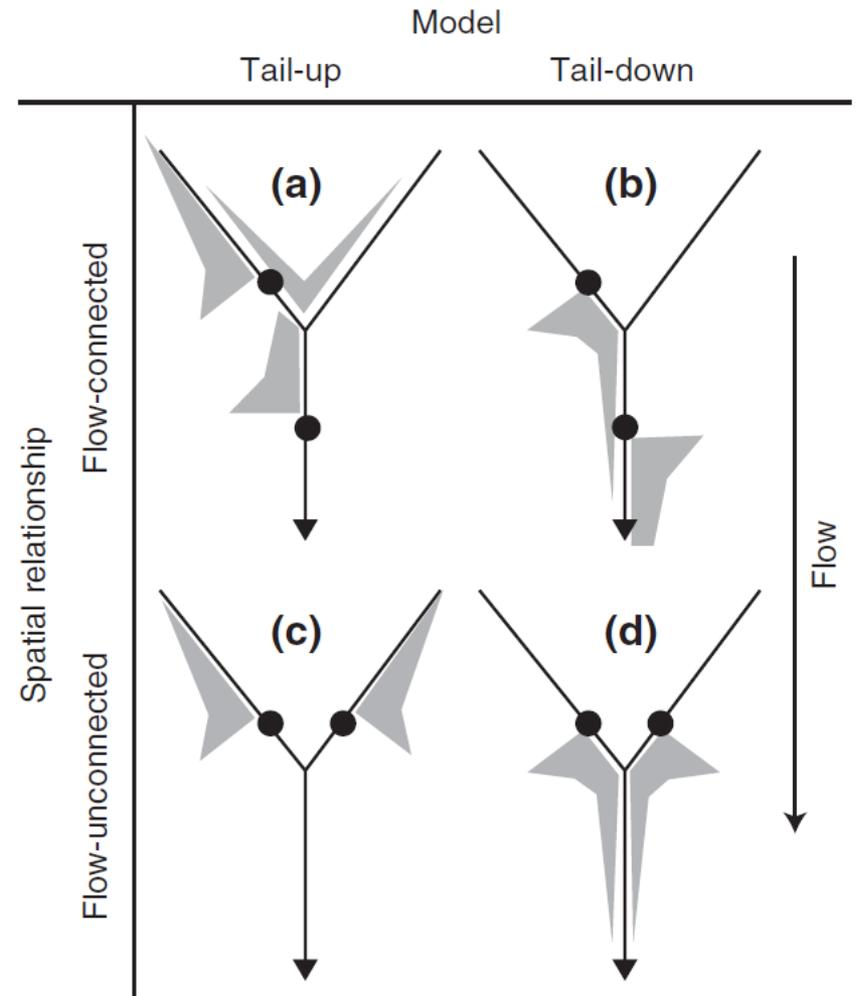
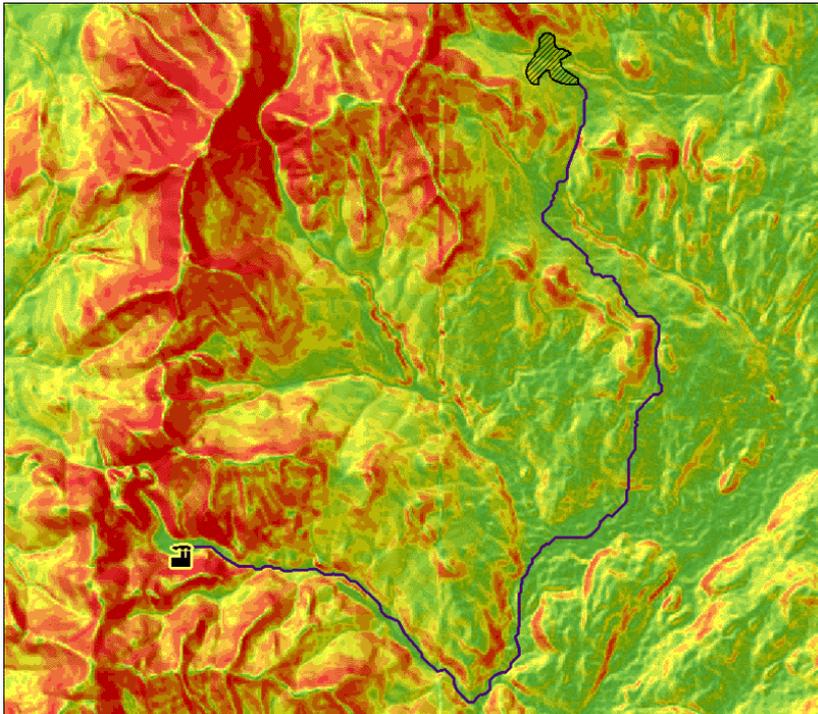






# Alternative geometries

- Traditional geostatistics uses a regular Euclidean conception of distance, but this need not be so



# Detrending

- ⊕ Spatial correlation can be expressed over different length scales
- ⊕ This leads to trade-offs between large and small scale patterns
- ⊕ In addition, interpolation can often be improved by incorporation of additional (non-geographic) information

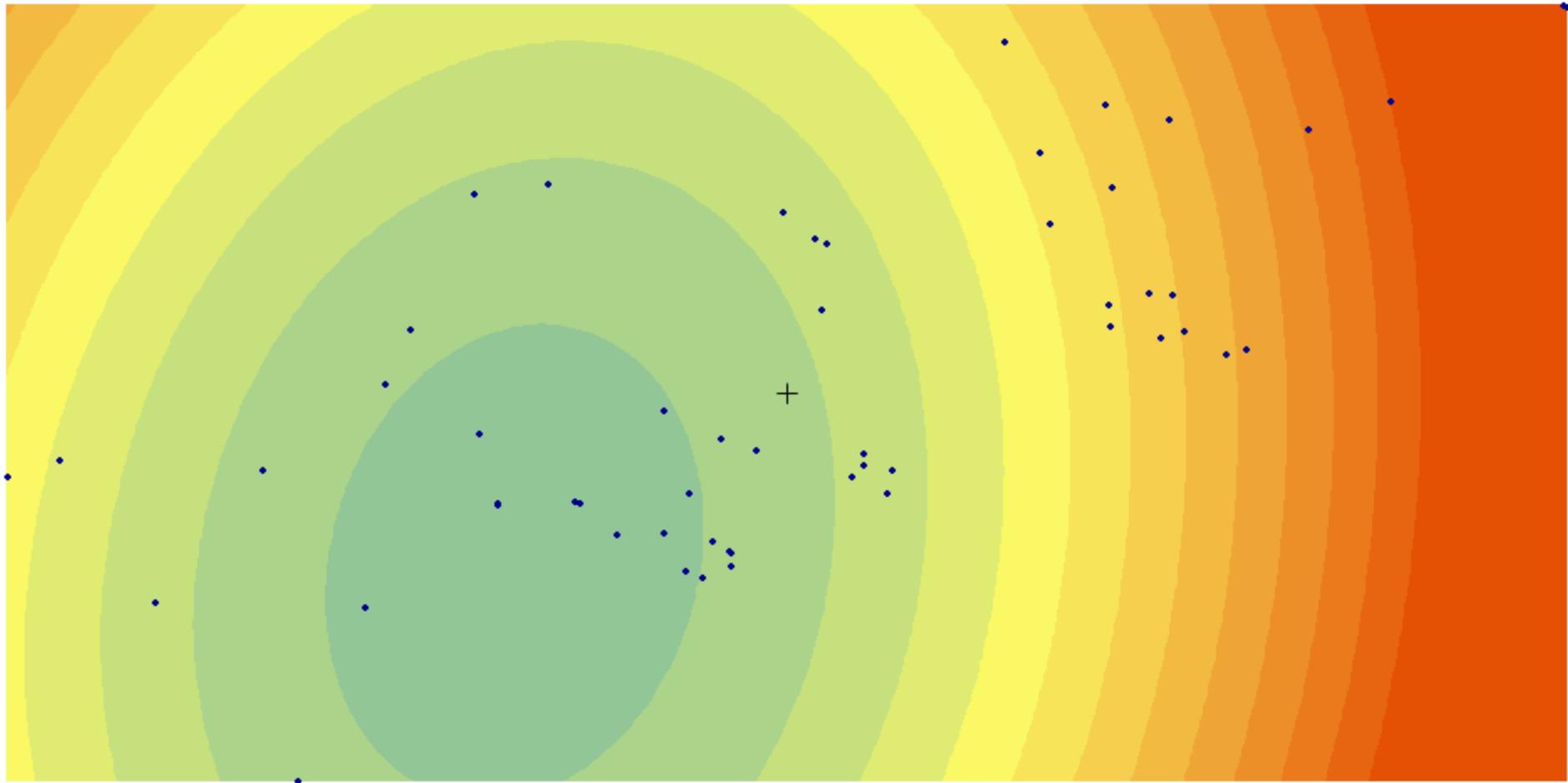
$$y(x_i) = \mu + \varepsilon_i$$

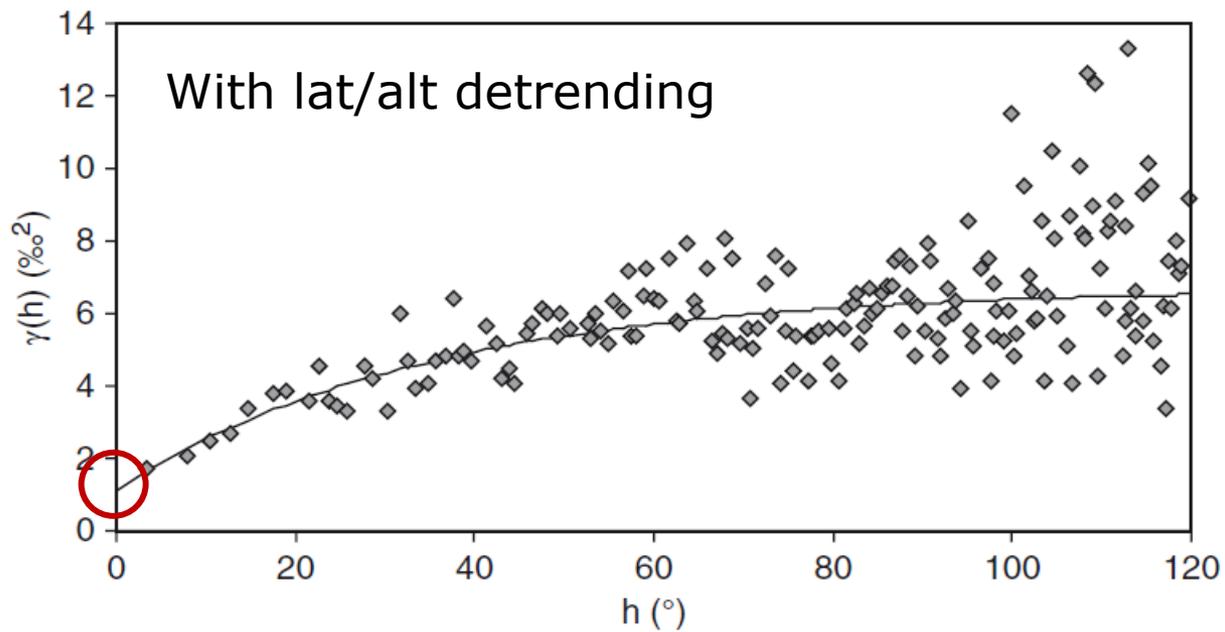
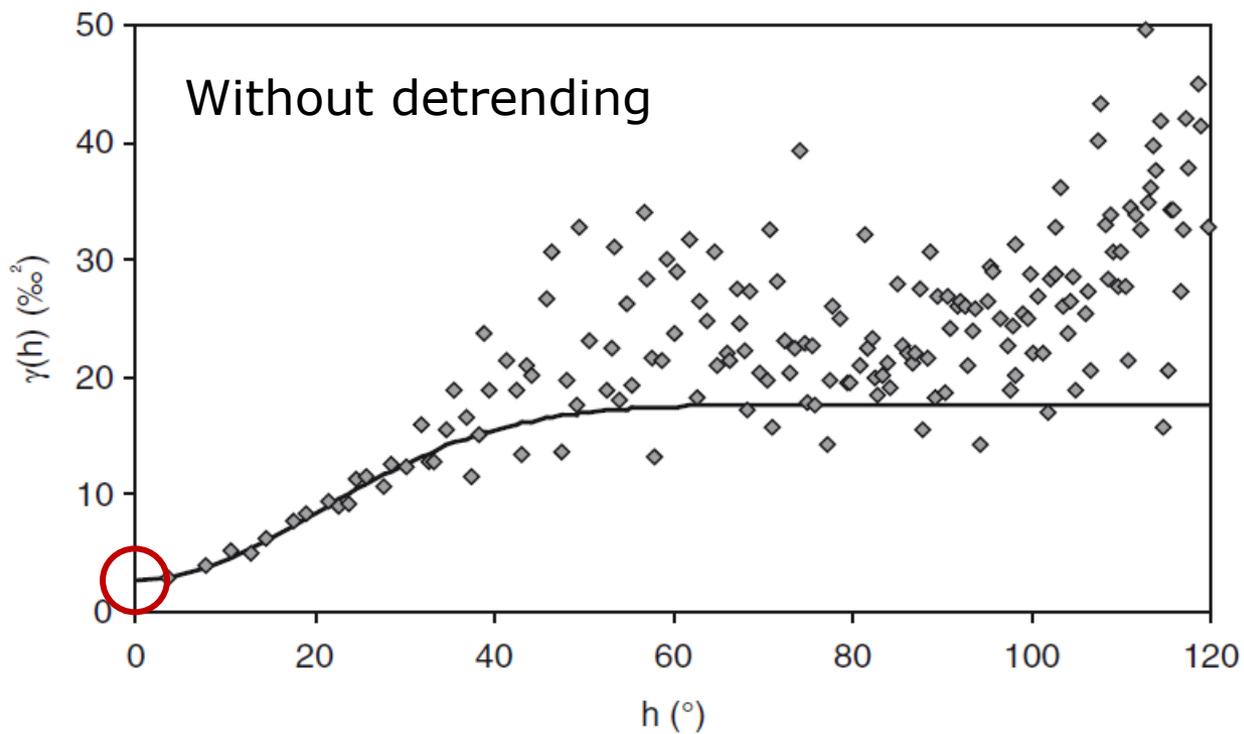


$$y(x_i) = v'(x_i)\beta + \varepsilon_i$$

- ⊕ Model for local mean ( $v'(x_i)\beta$ ) can range from simple function of location to complex multivariate function incorporating ancillary variables

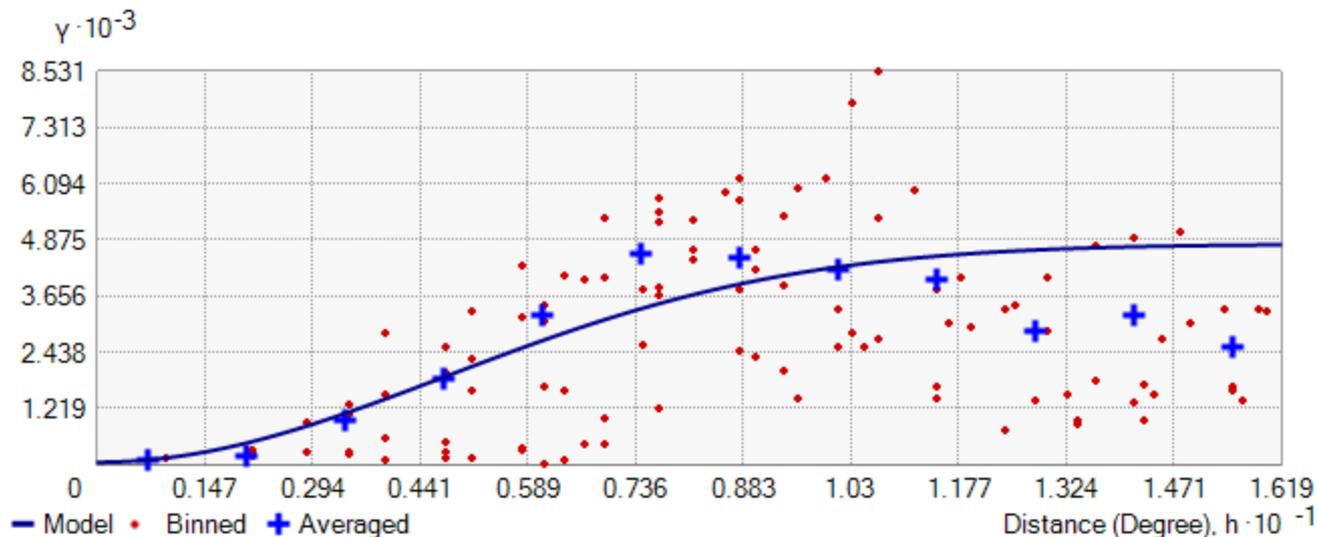
# Universal Kriging – Trend surface



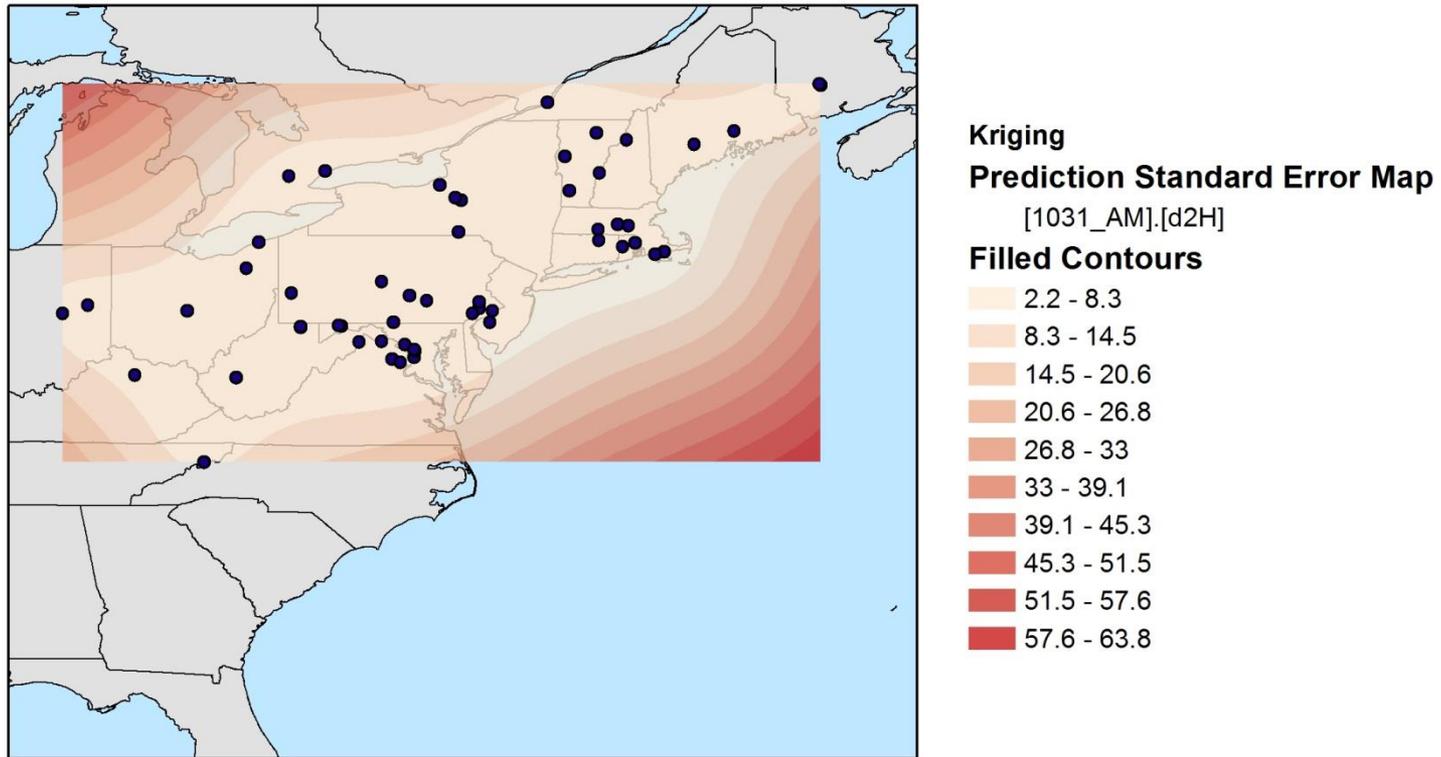


# Estimating uncertainty

- ⊕ Depending on method, multiple approaches are available
- ⊕ Range from analytical expressions for uncertainty in model to simulation-based numerical approaches
- ⊕ Kriging – variogram values basis for uncertainty of estimator



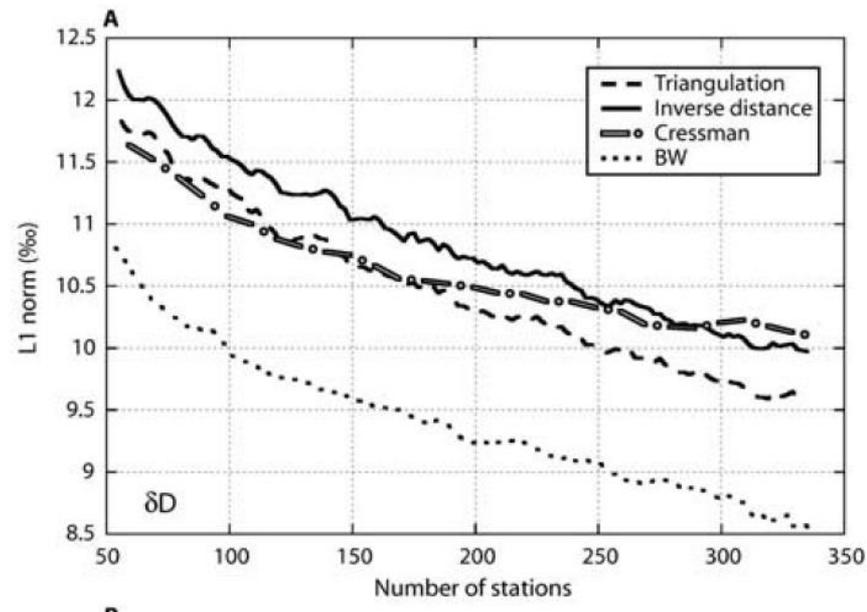
# Kriging uncertainty



- ⊕ Function of semivariogram model, data site distribution
- ⊕ Sensitive to model assumptions!

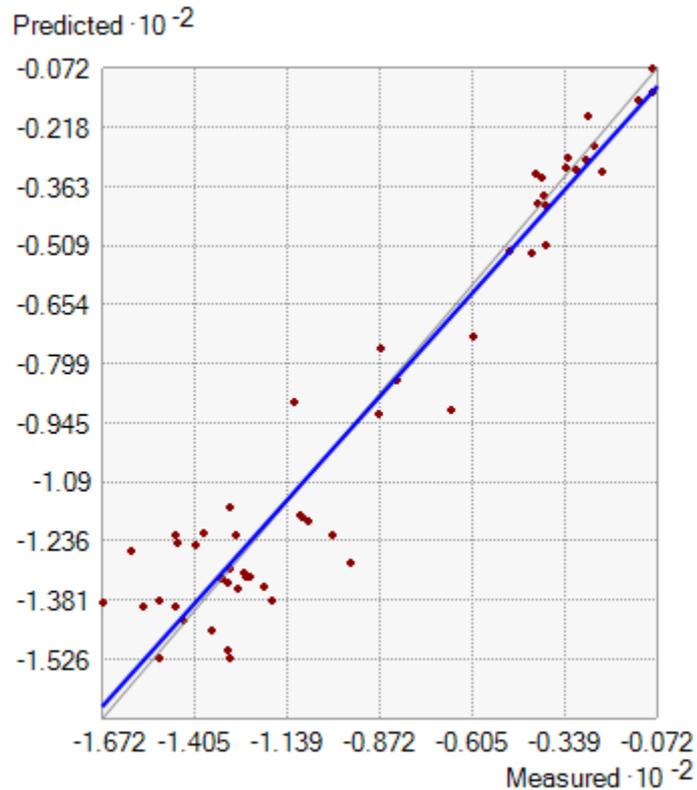
# Split-data tests

- ⊕ Simple approach
  - ⊕ Manually divide data into 2 subsets
  - ⊕ Fit model w/ first subset
  - ⊕ Validate w/ second subset
  - ⊕ + Quick, easy, supported by most software
  - ⊕ - Only 1 realization of model
  - ⊕ How many points to include?



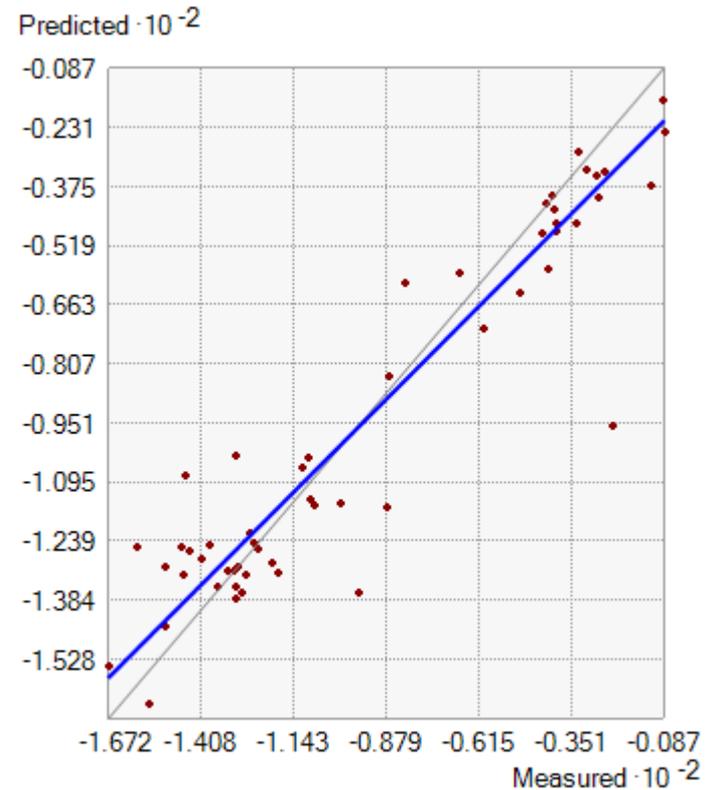
# Partial cross-validation

## Ordinary Kriging



RMSE = 13.4‰

## Universal Kriging

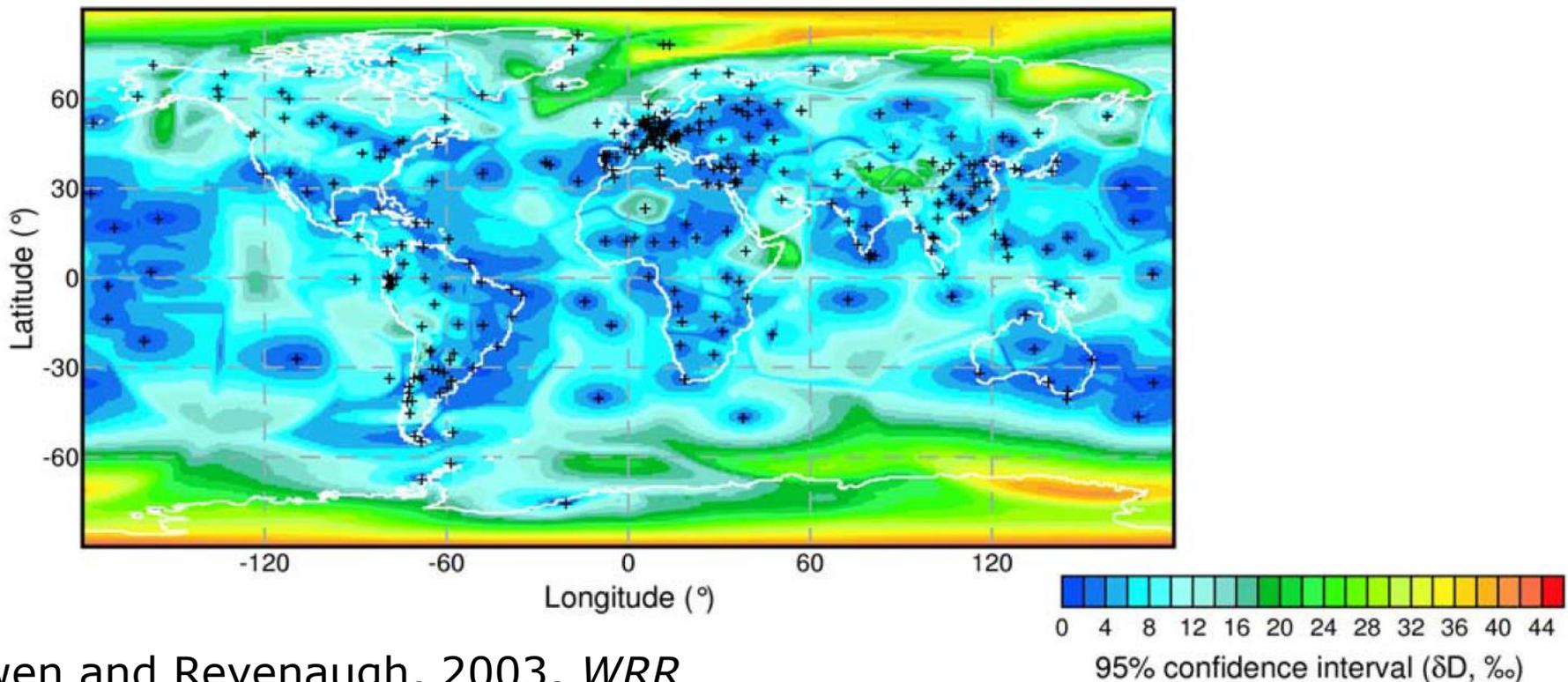


RMSE = 17.4‰

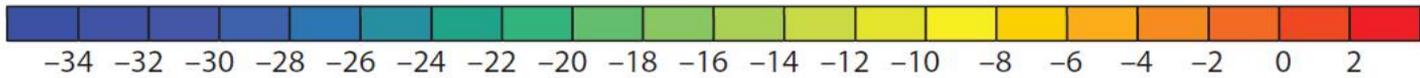
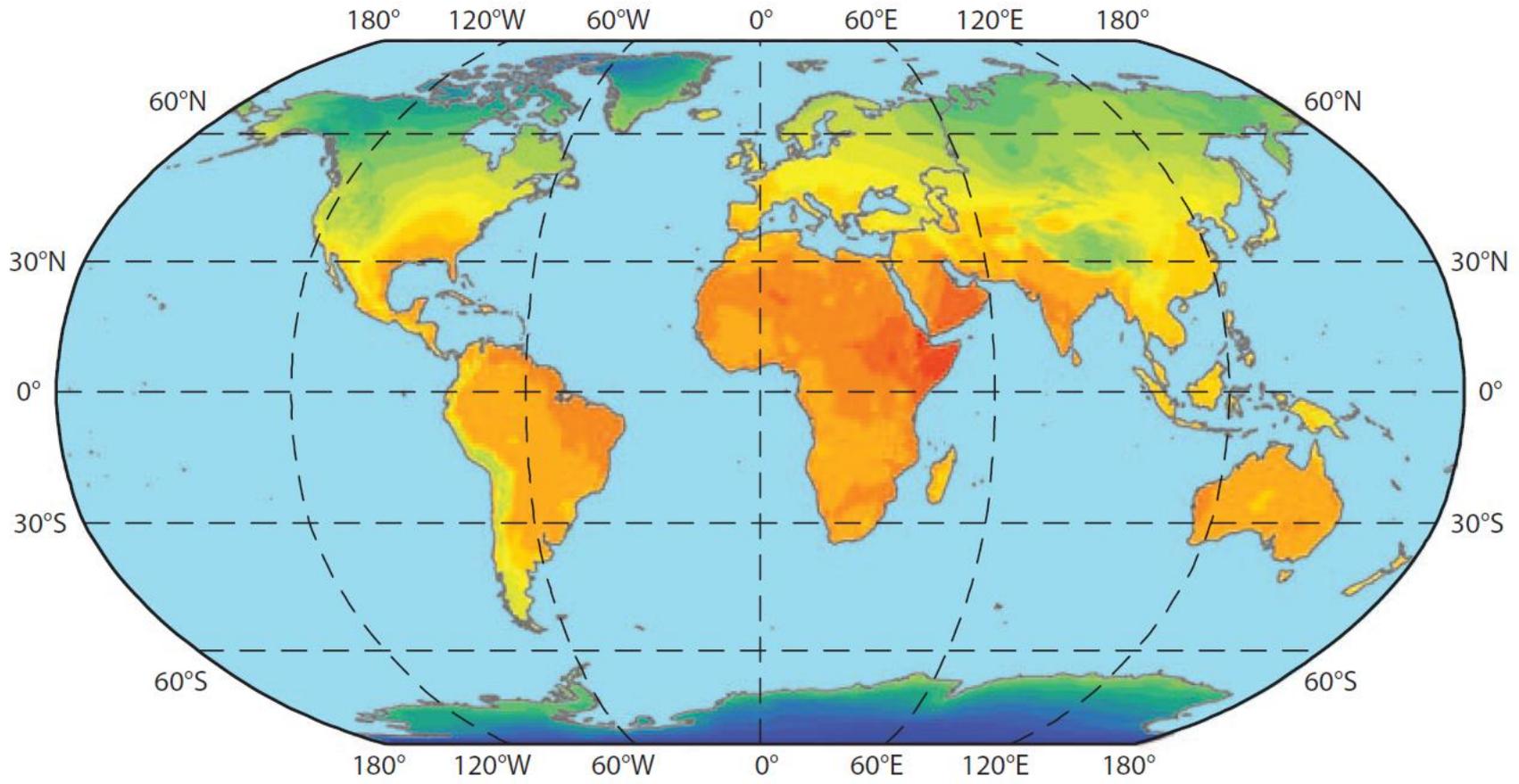
⊕ \*Note\* model not iteratively re-fit

# Simulation

- ⊕ Develop PDFs for model parameters
- ⊕ Iteratively calculate predictions to estimate PDFs for predictions across spatial domain
- ⊕ Can combine w/ resampling validation approaches



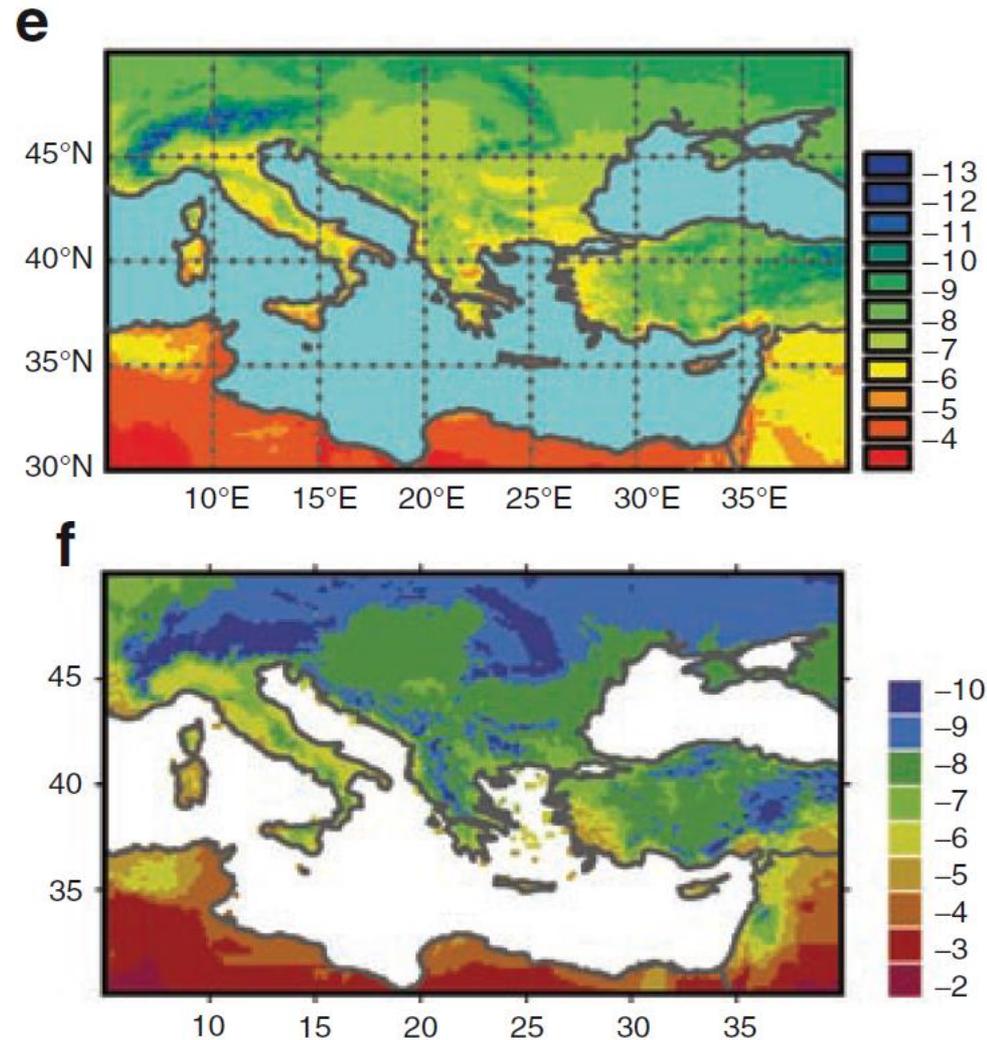
# Precipitation isotope examples



Annual average  $\delta^{18}\text{O}$  (‰)

# Regional models

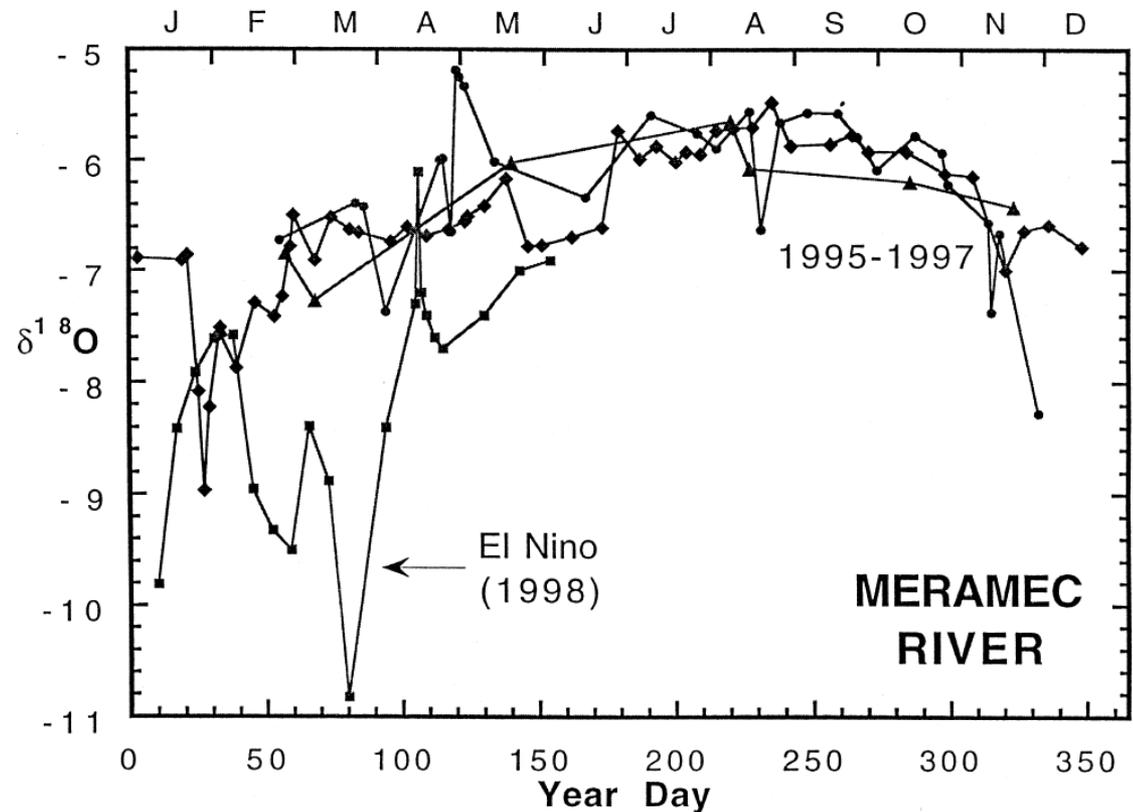
- ⊕ Optimal parameterization varies with region
- ⊕ Regional models can be generated over a range of spatial scales
- ⊕ Recent effort pursuing global models as aggregate of local functions...



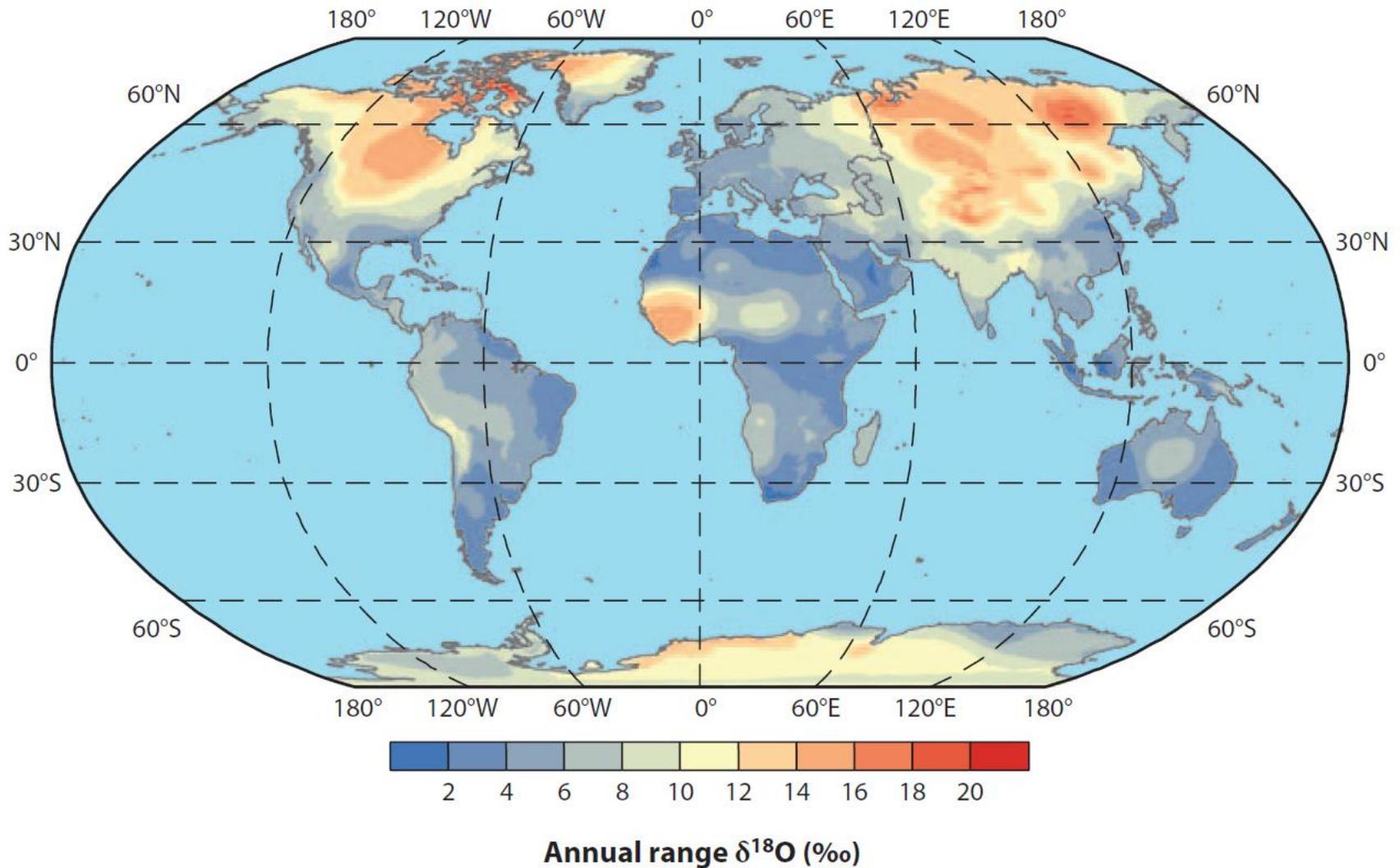
Bowen, 2010, *Isoscapes*  
after Lykoudis and Argiriou, 2007, *JGR*

# 3. Interpolating in space and time

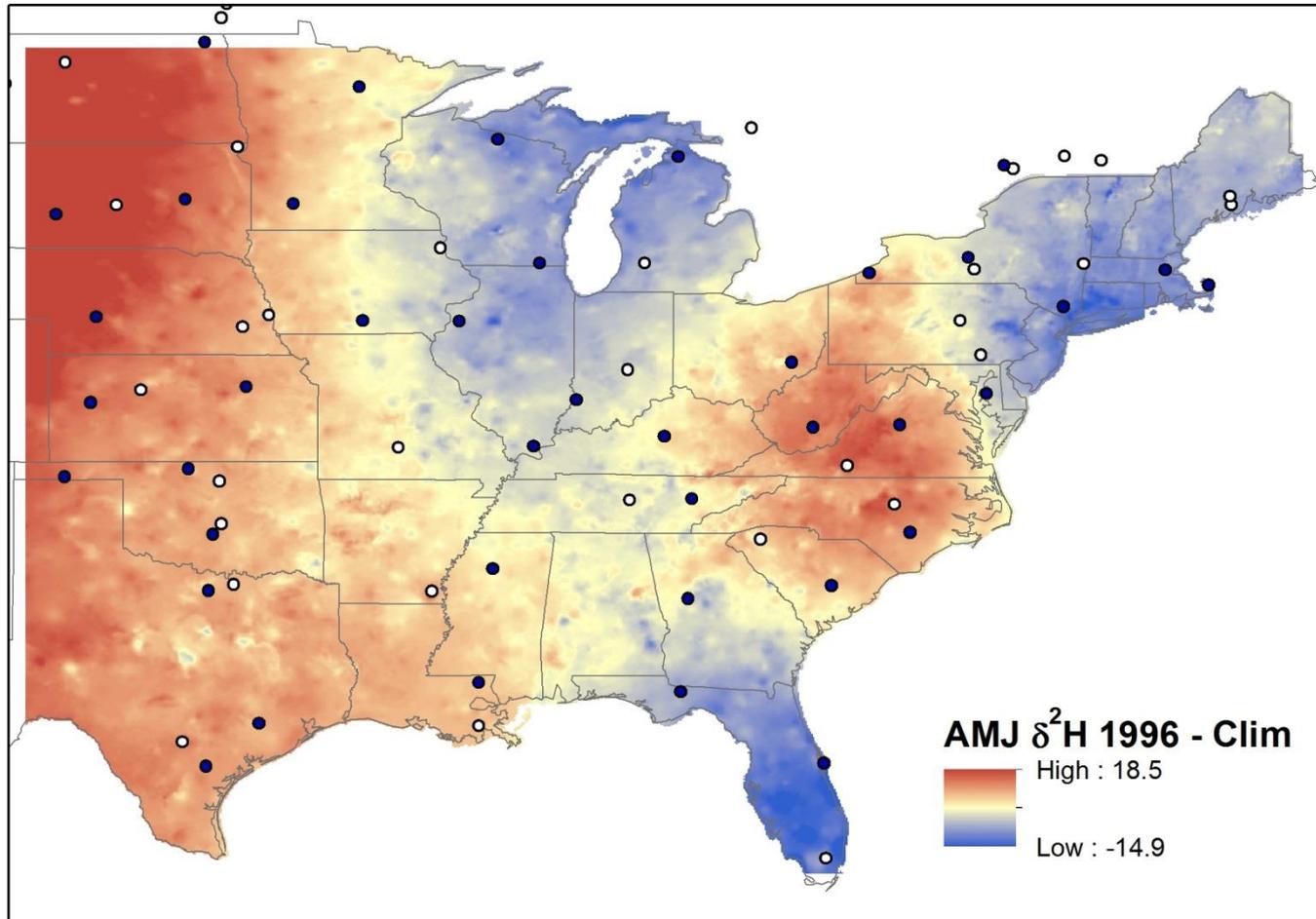
- ⊕ Lots of information in water isotope time-series
- ⊕ Requires understanding of precipitation isotope variation in spatial and temporal domains



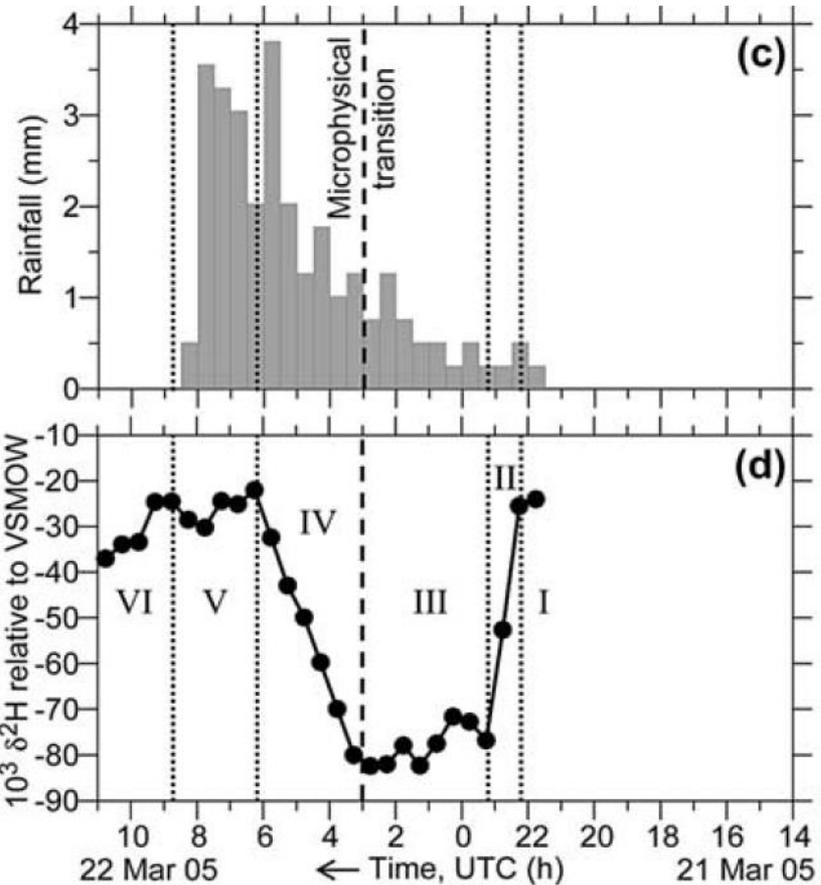
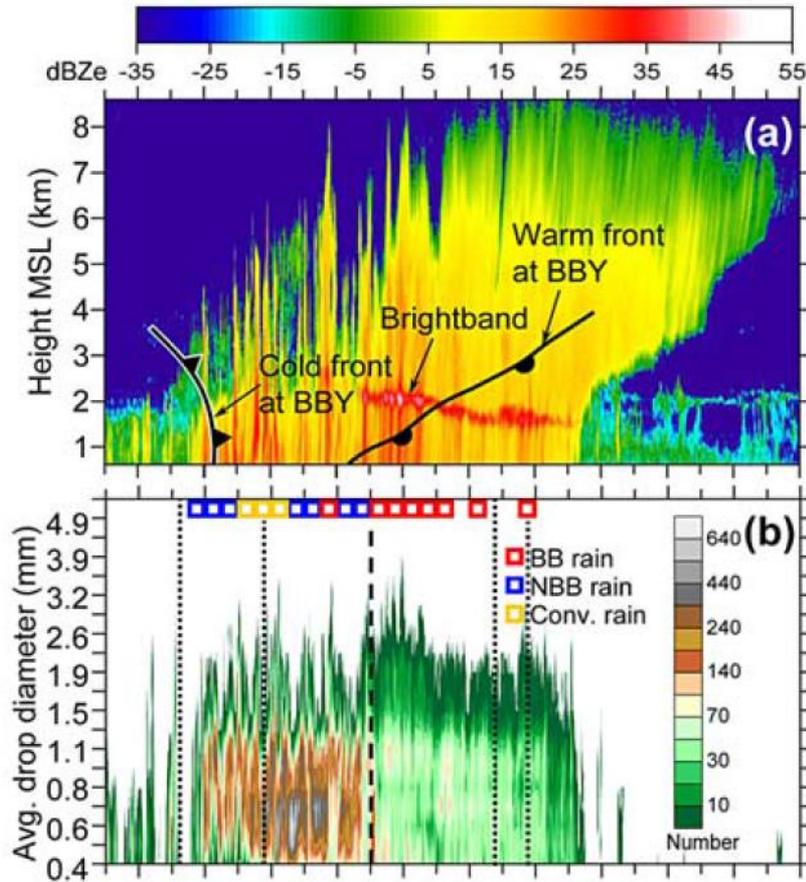
# Temporal variation - seasonality

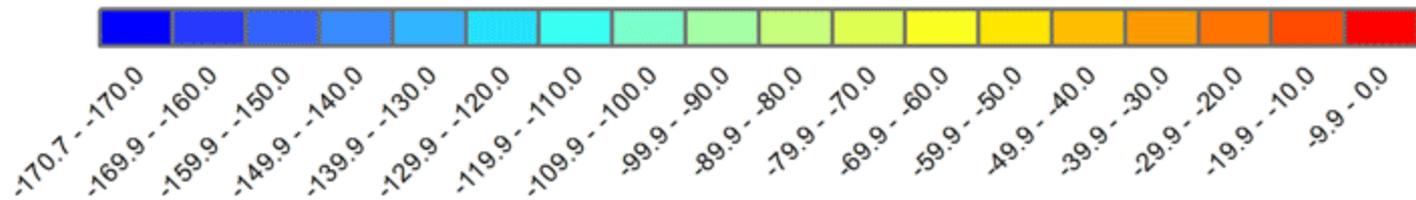
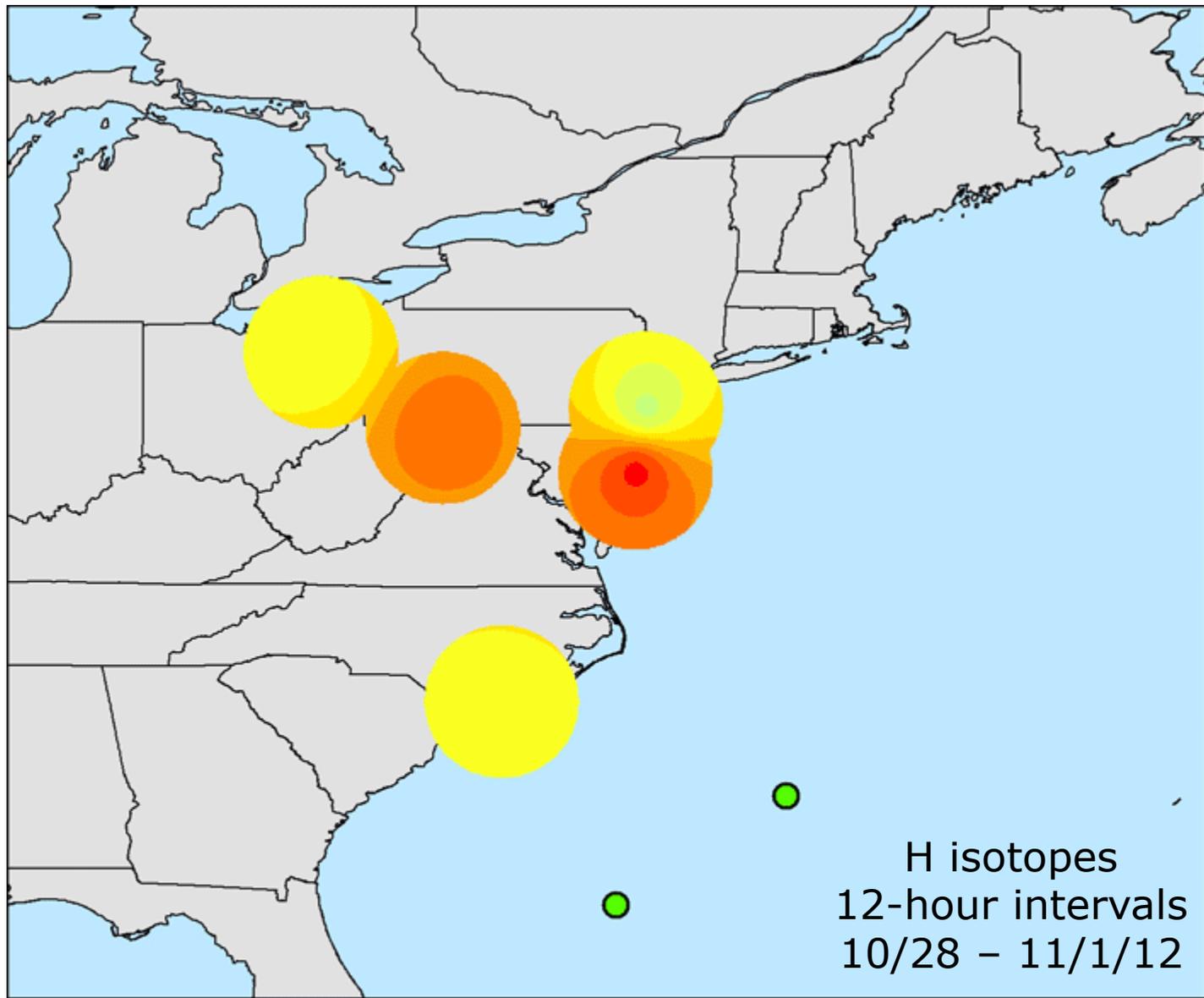


# Temporal variation - interannual

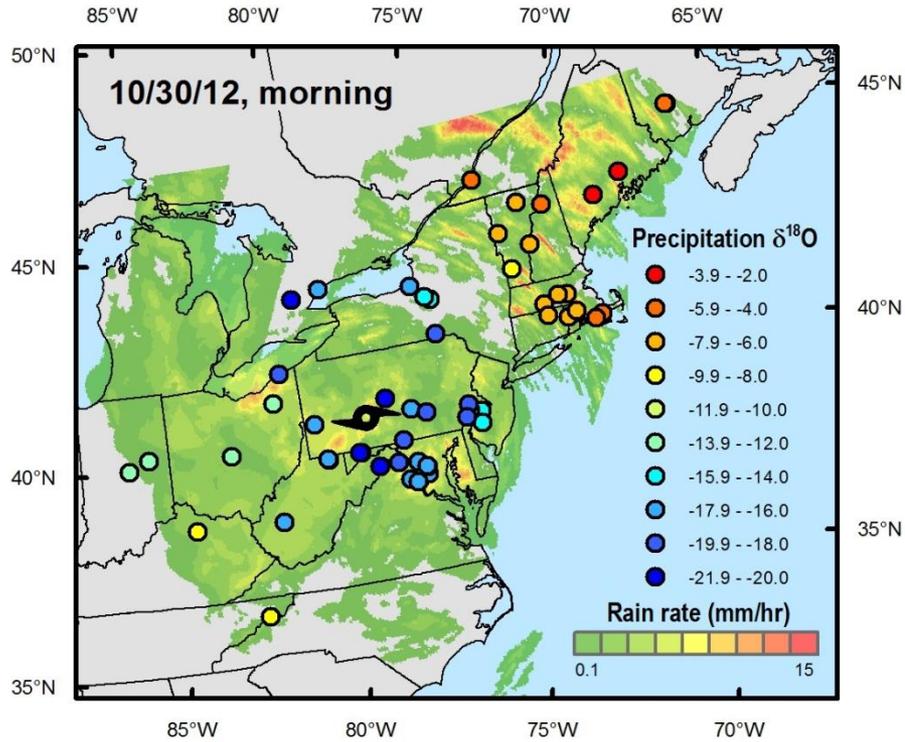


# Temporal variation - meteorological

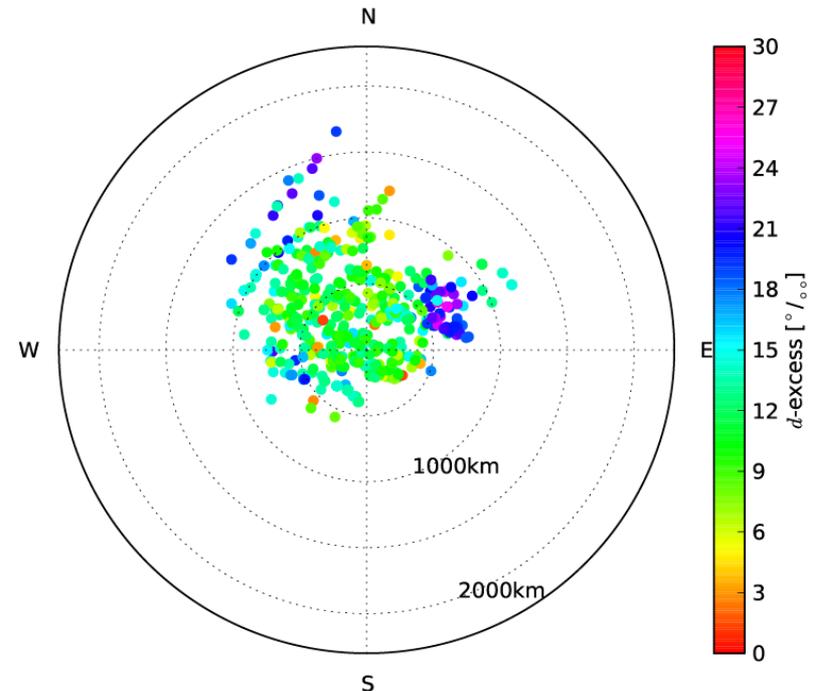




# Predictability?

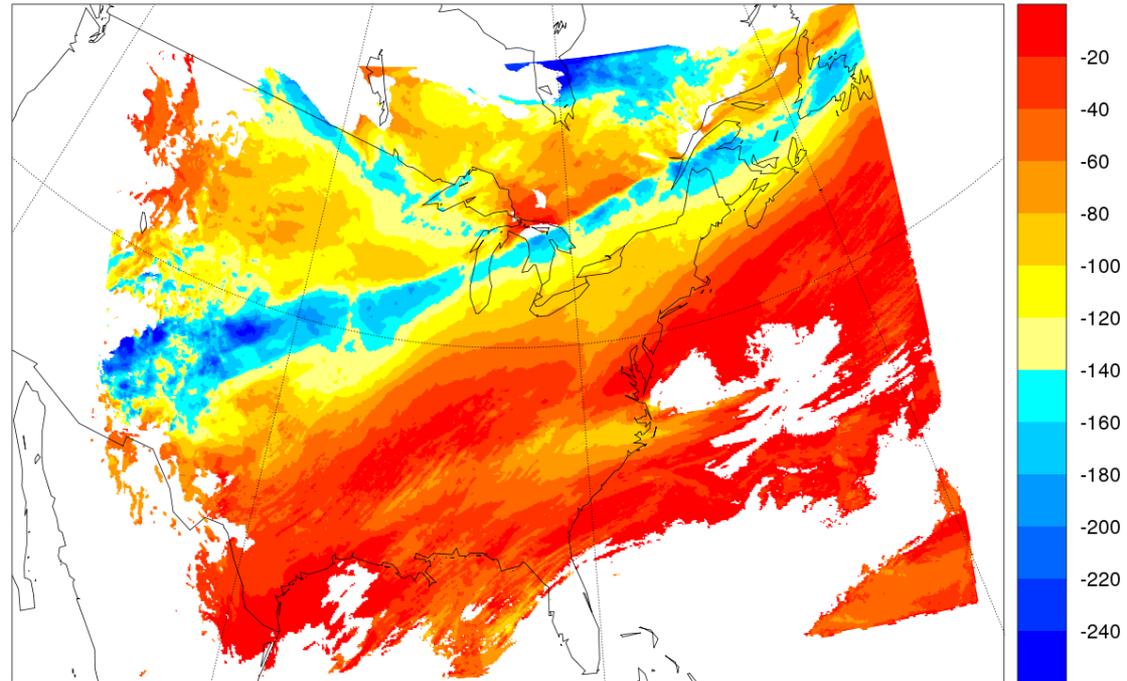
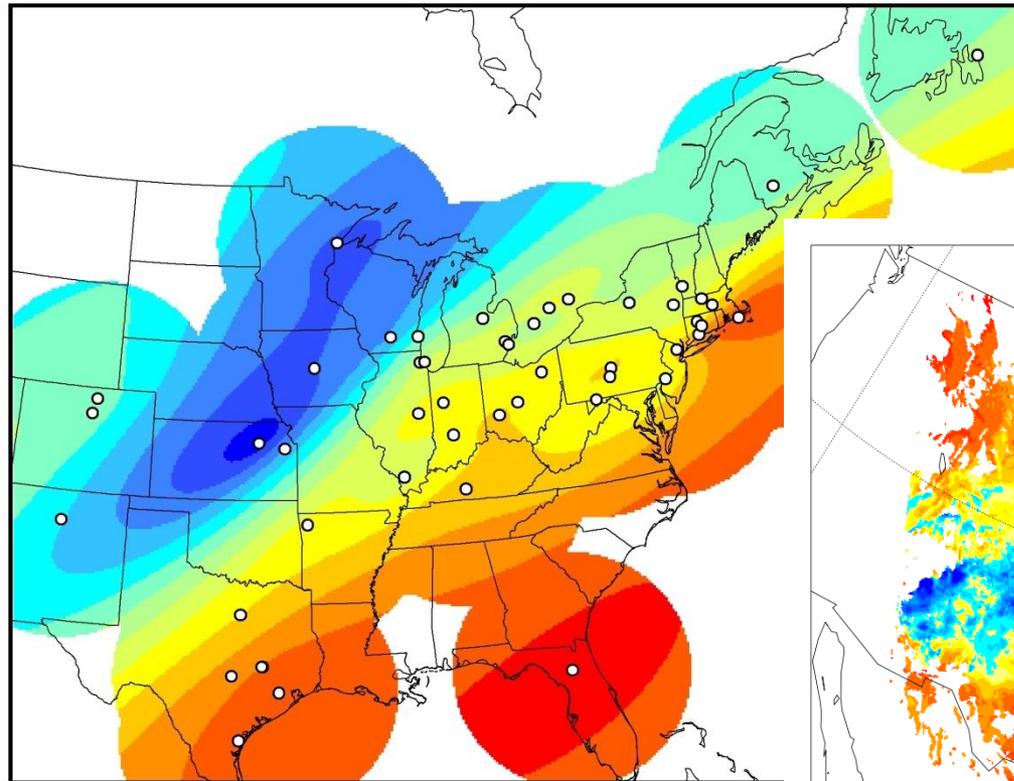


☉ Synoptic relationships?



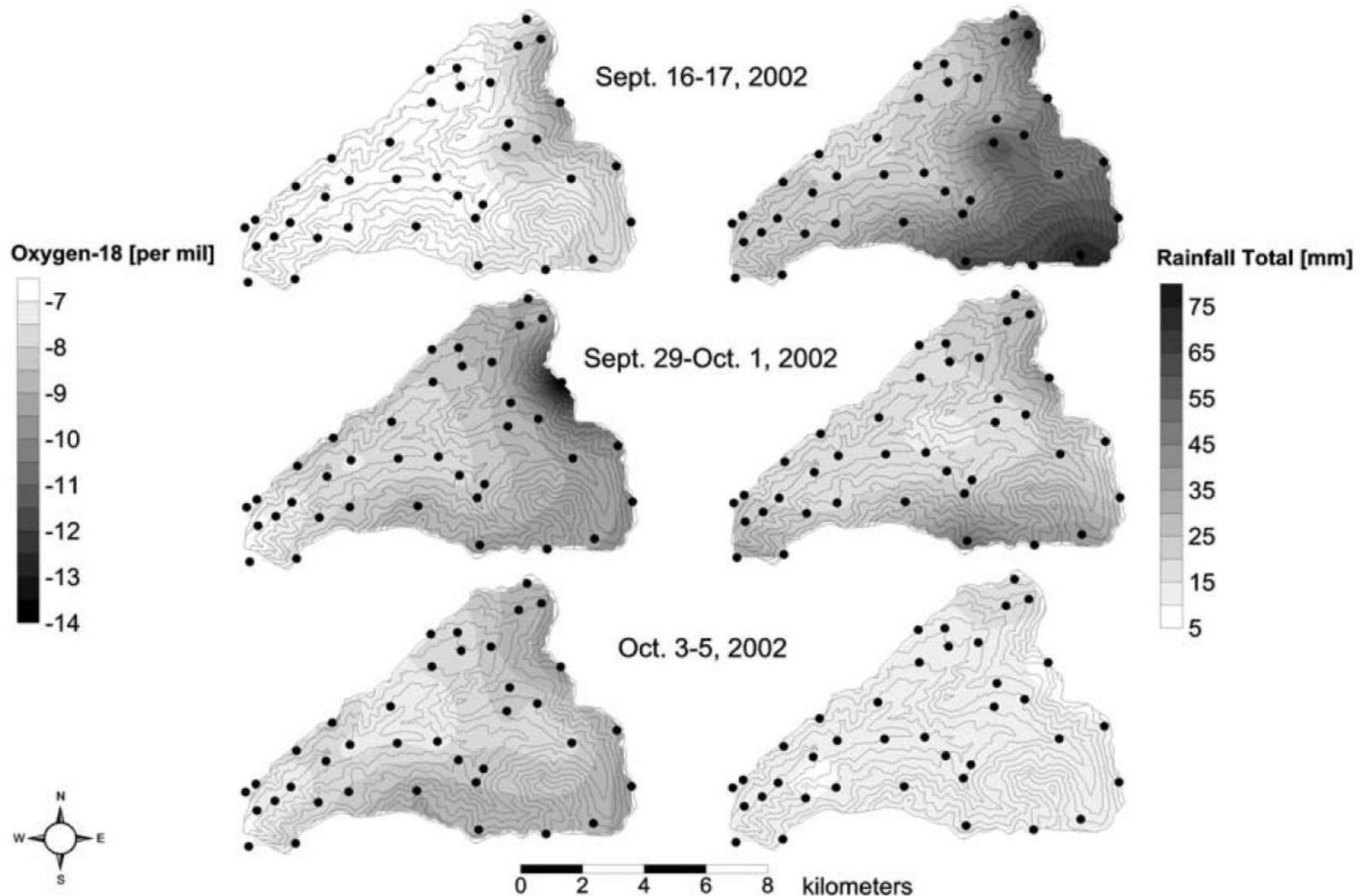
# Predictability?

⊕ Dynamical models?

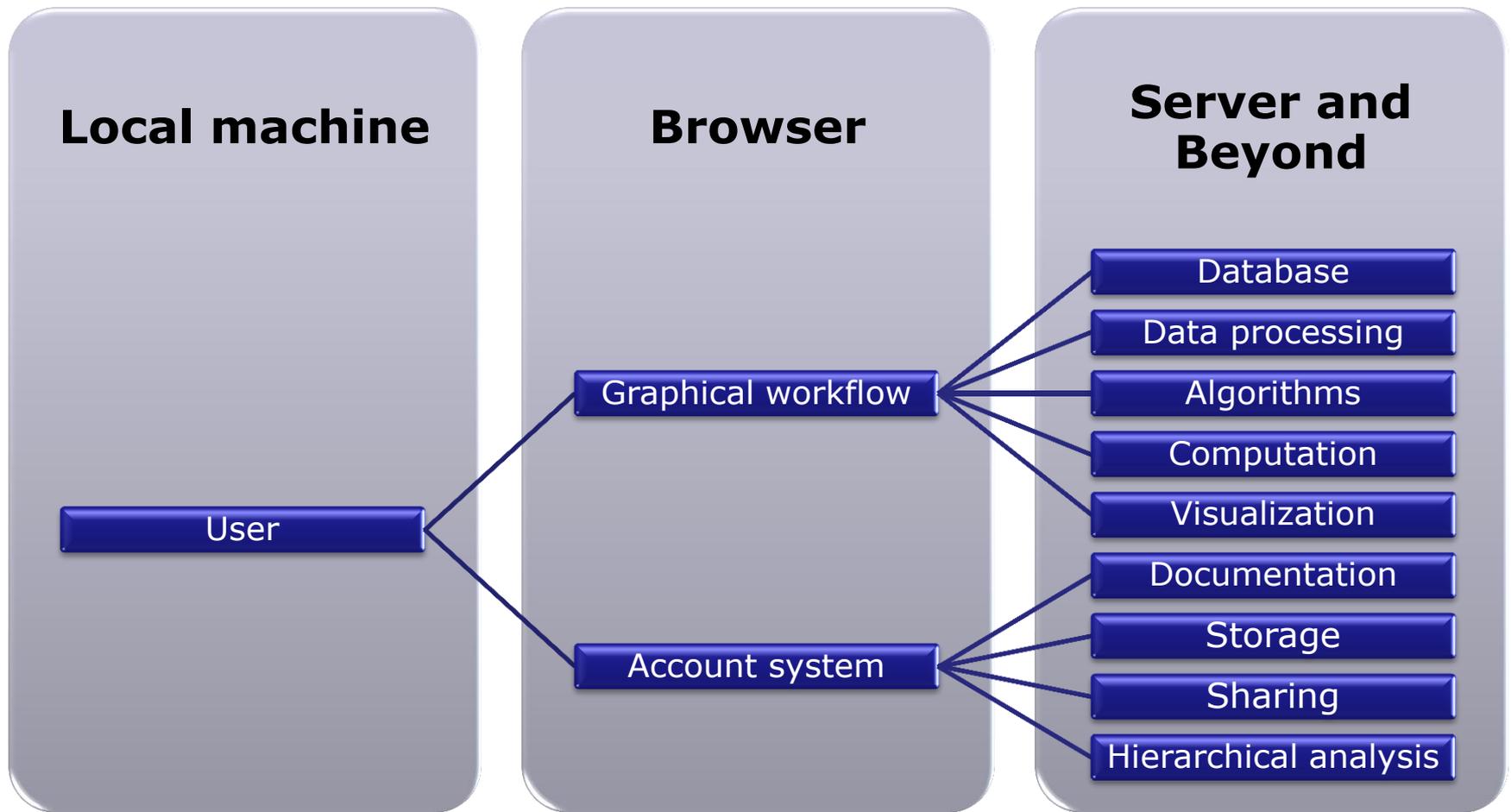


**Groundhog Day storm, 2011  
storm average  $\delta^2\text{H}$**

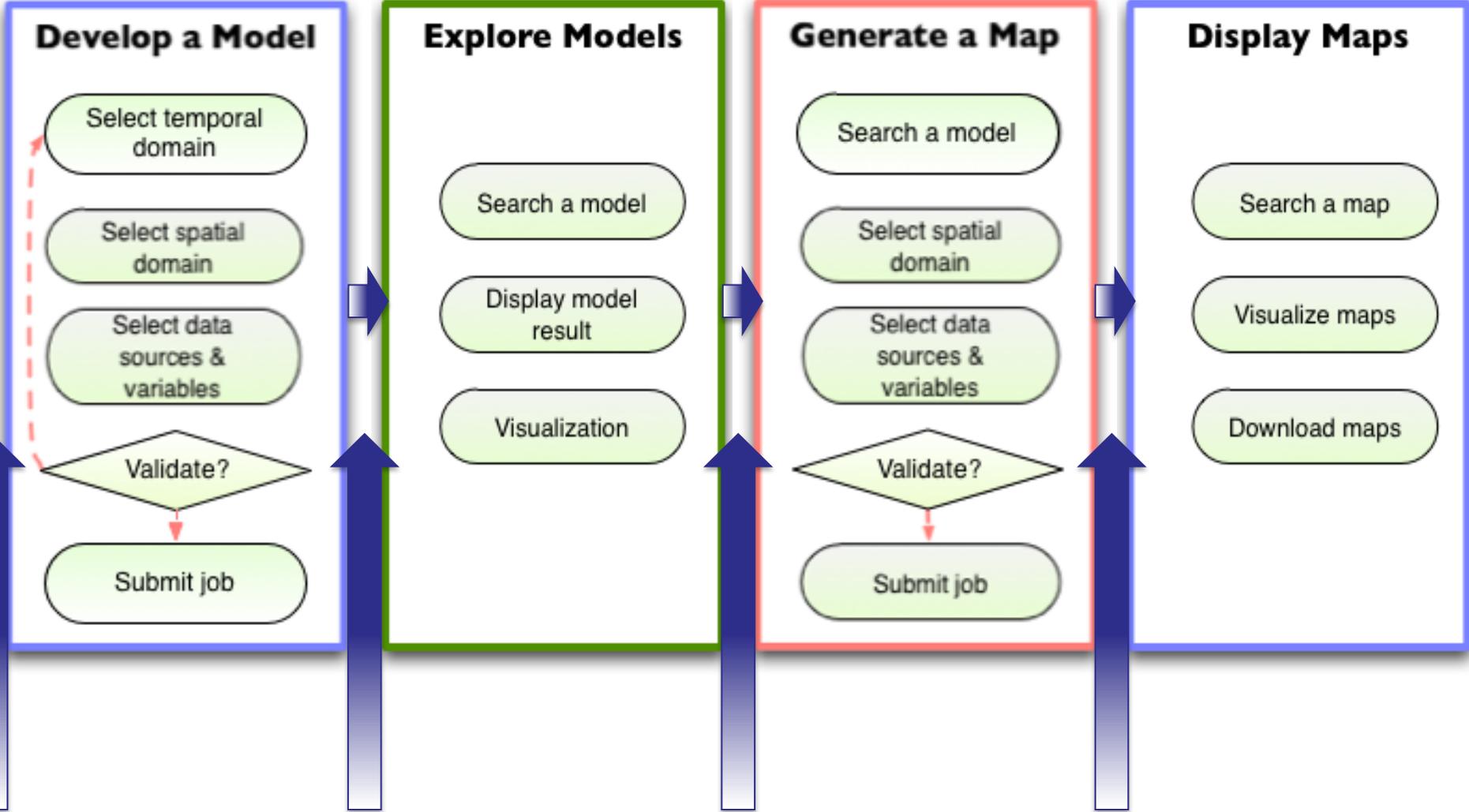
# Emperical approach



# IsoMAP (<http://isomap.org>)



# Precipitation Modeling Workflow



Search 

predkrig 
  predreg 
  stdkrig 
  stdreg

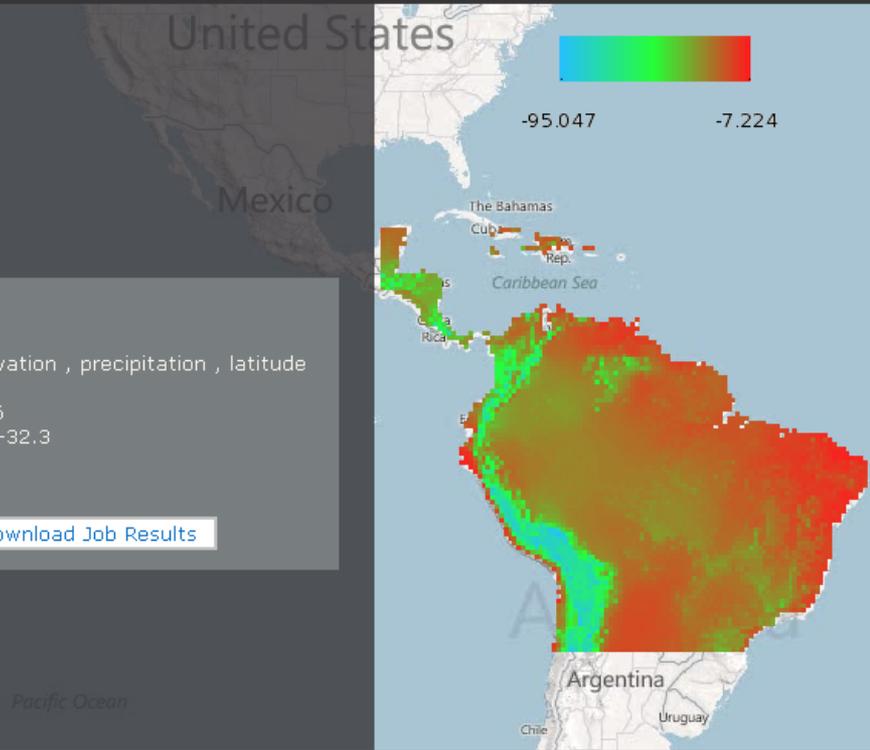
September 23, 2011

Map navigation controls: zoom in (+), zoom out (-), pan (hand), home (house), full screen (maximize), and refresh (circular arrow).

Job Key  e.g., 3000 or >3000  
 AND  Job Description   
 AND  Case Name

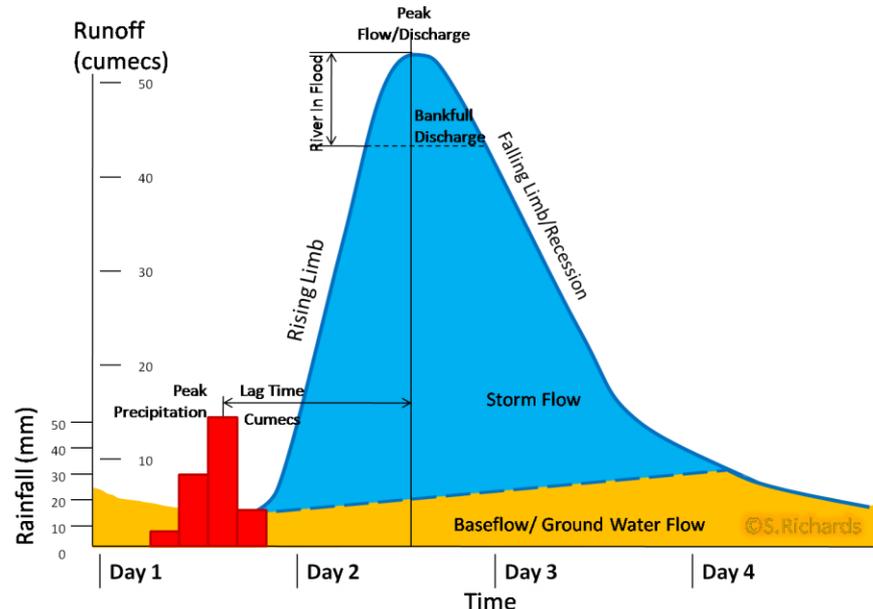
Job Key	Owner	Case Name	Start Time
6581	KeithHobson	Sotomap1	2011-08-26T14:31:14Z
6569	wassenaarl	india3	2011-08-26T14:04:33Z
6477	vwilgs	Africa_delta2H_DJF	2011-08-23T12:51:03Z
6407	jbowest	d2H_AnnualMap_jbow	2011-08-17T14:23:18Z
6359	gjbowen	Goldschmidt	2011-07-08T13:03:25Z
5905	gjbowen	DJF_CLIM_AFRICA_MAP	2011-07-08T13:01:50Z
5857	gjbowen	globeclim_dec_map	2011-07-06T15:38:25Z
5856	gjbowen	globeclim_nov_map	2011-07-06T15:03:33Z
5855	gjbowen	globeclim_oct_map	2011-07-06T14:52:50Z
5852	gjbowen	globeclim_sep_map	2011-07-06T14:50:20Z
5851	gjbowen	globeclim_aug_map	2011-07-06T14:46:51Z
5850	gjbowen	globeclim_jul_map	2011-07-06T14:20:03Z
5849	gjbowen	globeclim_jun_map	2011-07-06T14:18:57Z

Model Information (6581)  
 Model type: precipitation  
 Dependent variable: d2h  
 Independent variables: elevation , precipitation , latitude absolute value  
 Latitude range: -27 to 20.6  
 Longitude range: -90.4 to -32.3  
 Year range: 1968 to 2000  
 Number of stations: 60



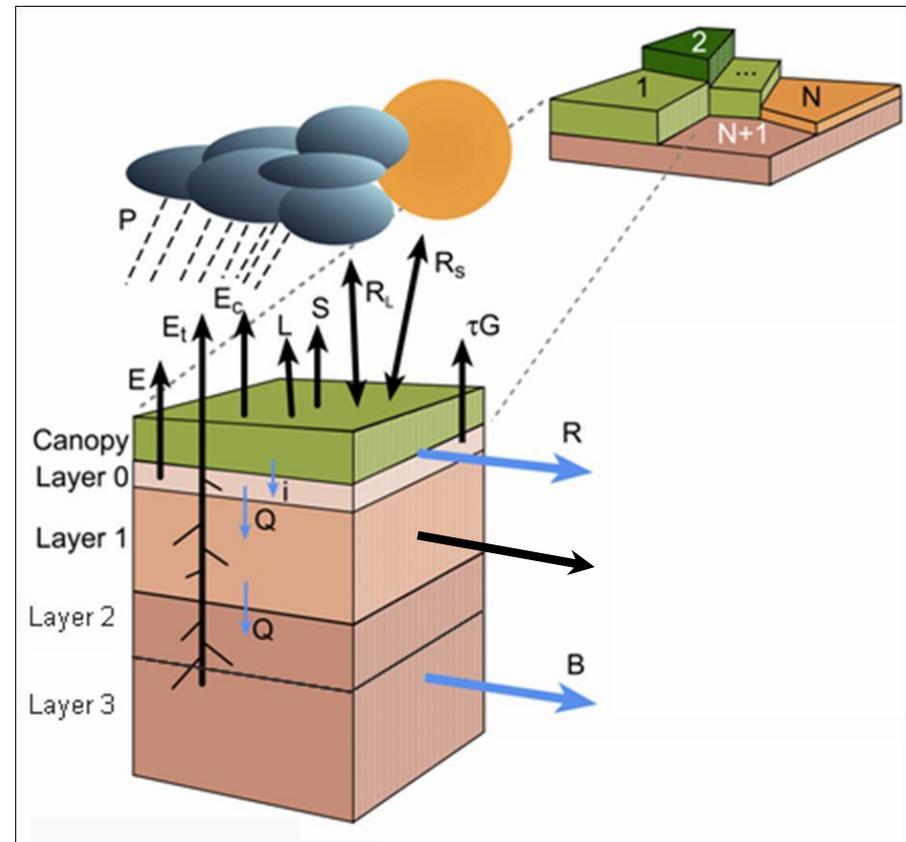
# 4. Most headwater catchments export old water

- ⊕ Accurate rainfall-runoff models are one of the fundamental goals of catchment hydrology
  - ⊕ Flood control
  - ⊕ Water management
  - ⊕ Water quality
- ⊕ Summarized in terms of storm hydrograph



# Rainfall routing

- ⊕ How is storm precipitation delivered to streams?
  - ⊕ Overland flow
  - ⊕ Interflow
  - ⊕ Groundwater recharge/baseflow
- ⊕ What are the transit times associated with these flowpaths?

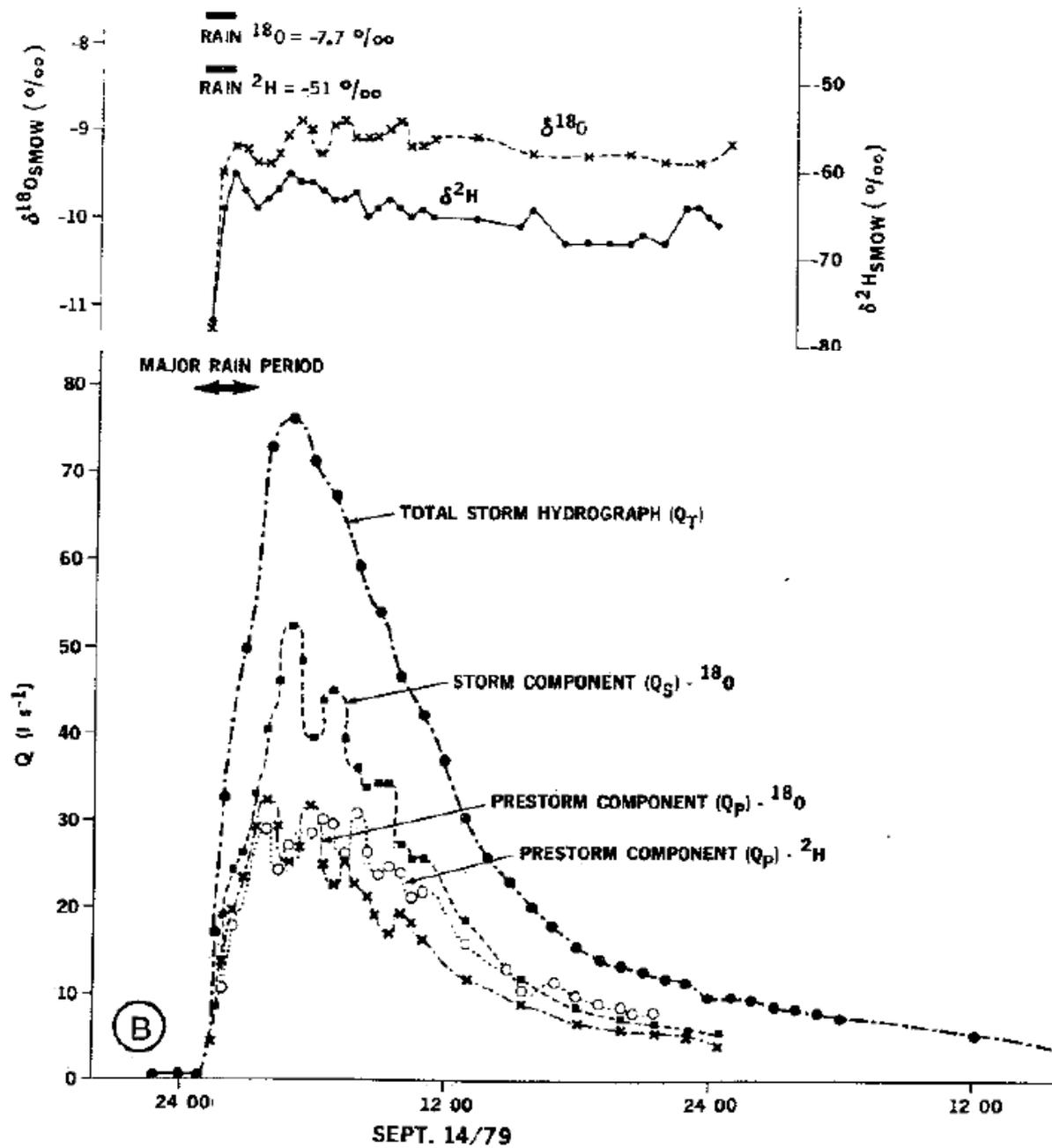


# Hydrograph separation

- Given any conservative tracer that is present in different abundance in **pre-event** and **event** water, the fraction of pre-event water in storm flow at any time is

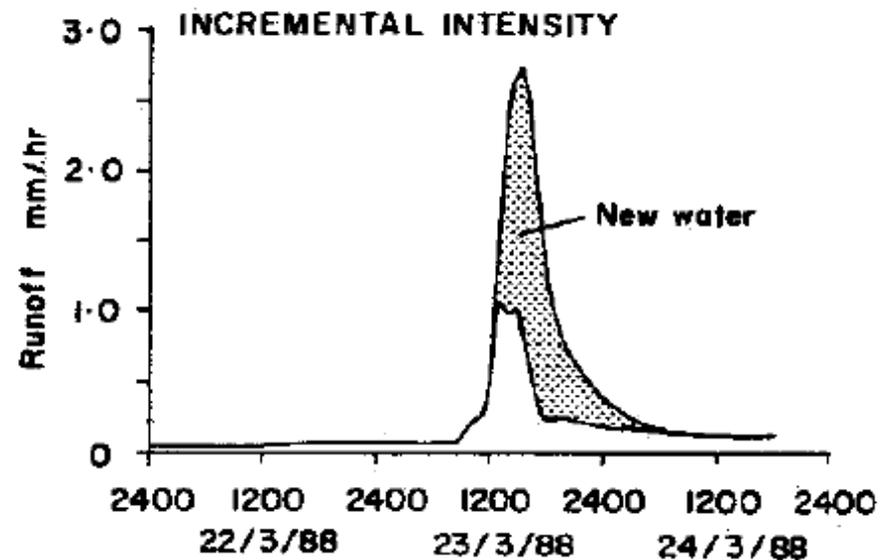
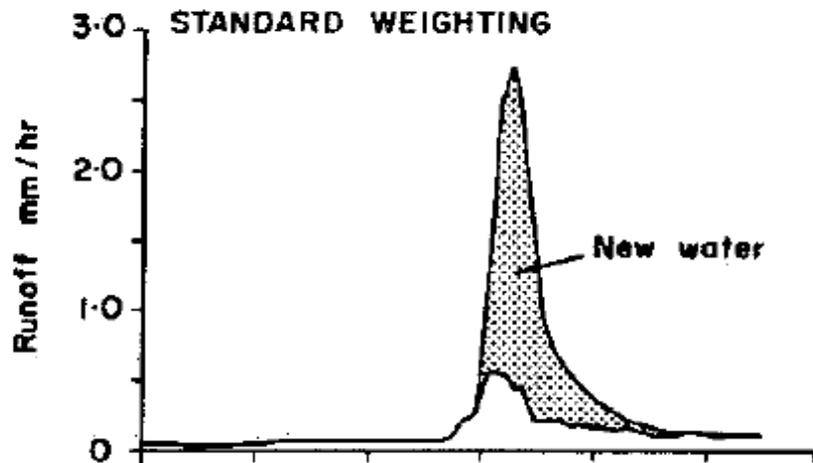
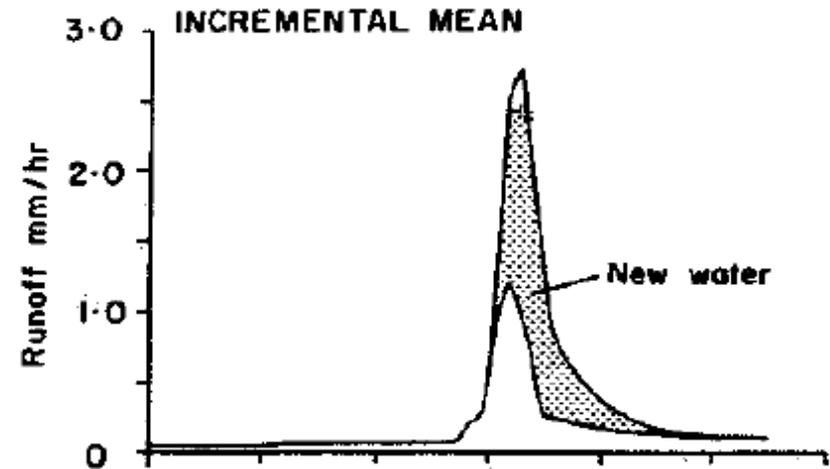
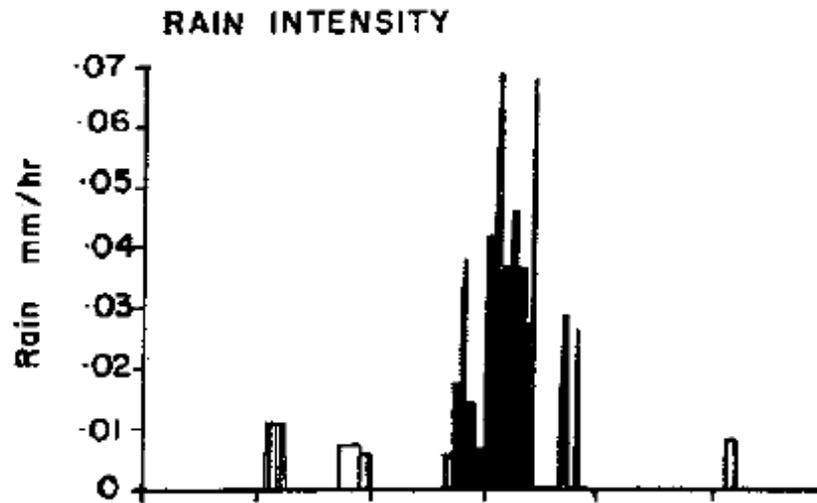
$$f_{pe} = \frac{C_s - C_e}{C_{pe} - C_e}$$

- Major assumption:  $C_e$  and  $C_{pe}$  are constant and can be accurately characterized
- Isotope hydrograph separation takes advantage of temporal variation in precipitation  $\delta$  values



Bottomley et al., 1984  
*J Hydrol*

# Characterizing inputs



# “Old water paradox”

Study	Location	Catchment area (ha)	Tracer	Percentage pre-event water	
				peak	volume
Jordan (1994)	Switzerland	3.6	$^{18}\text{O}$		45, 75
Waddington et al. (1993)	Ontario	160	$^{18}\text{O}$	87, 93	
McDonnell et al. (1991)	New Zealand	3.8	D	92-100	
O'Gunkoya & Jenkins (1991)*	United Kingdom	1000	D		54-90
McDonnell et al. (1990)	New Zealand	310	D		21-33
Nolan and Hill (1990)	California	1060	D		57
Bonell et al. (1990)	New Zealand	218	D		59
		310	D	38	38 to >97
Blowes and Gillham (1988)	Ontario	0.75	$^{18}\text{O}$	9, 45	22, 50
Turner et al. (1987)	W. Australia	82	$^{18}\text{O}$ , D		69-95
Herrman et al. (1987)*	Germany	76	$^{18}\text{O}$		84
Rodhe (1987)	Sweden	3	$^{18}\text{O}$		81, 87
		4	$^{18}\text{O}$		81, 96
		17	$^{18}\text{O}$	87	
		50	$^{18}\text{O}$		85-99

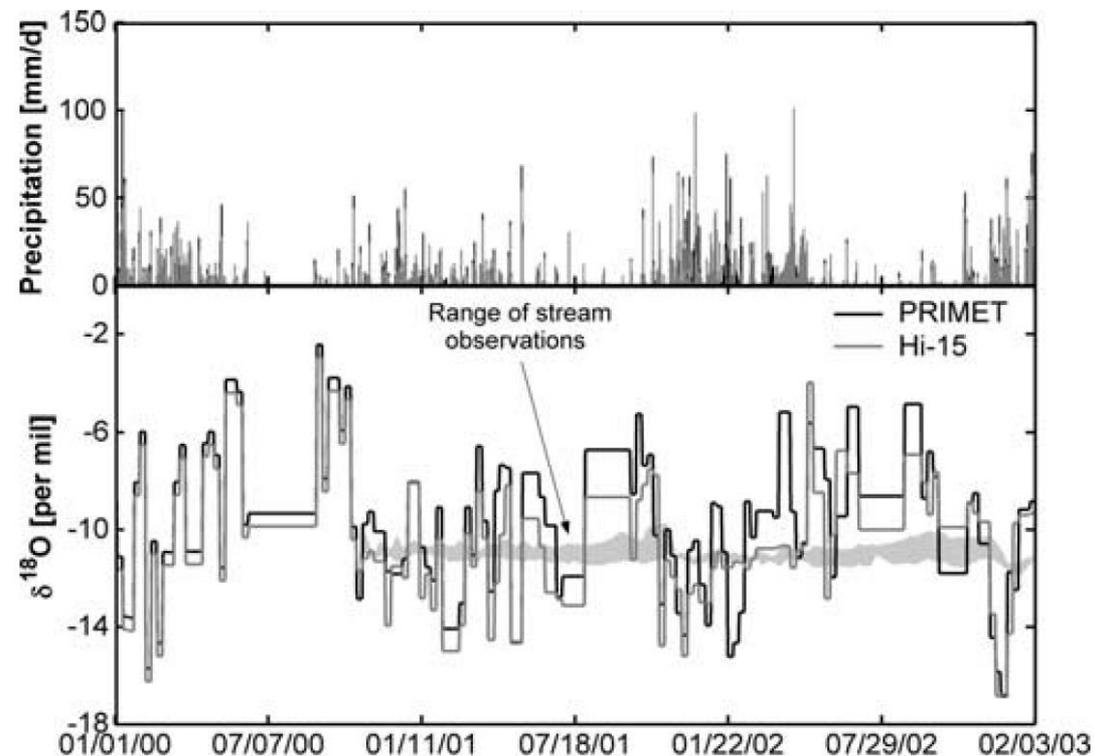
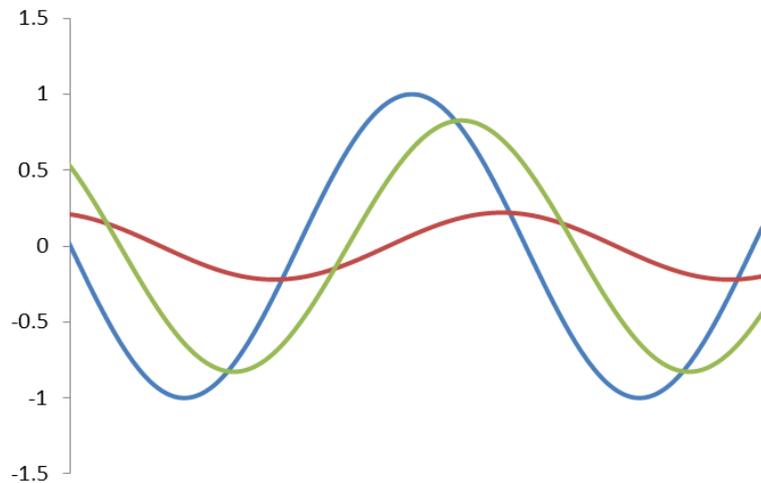
....

# “Old water paradox”

- ⊕ Even in small, steep catchments, most storm flow is “old” water
- ⊕ Mean residence time of water in catchments is much longer than implied by simple interpretation of storm hydrograph, rainfall-runoff models
- ⊕ How does storm discharge actually work?
  - ⊕ If water is not transferred directly, how does addition of precipitation rapidly force release of pre-event water?
- ⊕ Hypotheses
  - ⊕ Pressure waves
  - ⊕ Capillary fringe
  - ⊕ Macropore flow

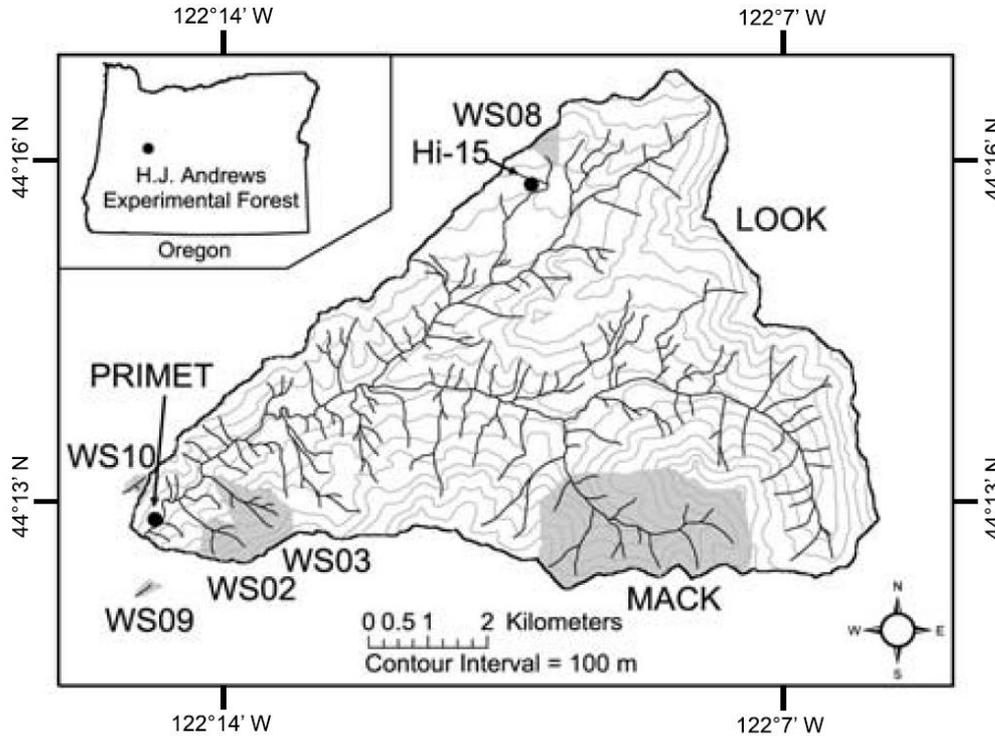
# Baseflow transit time distributions

- Given measured input and output time series, optimize the function  $f(t)$  describing the distribution of transit times within a catchment

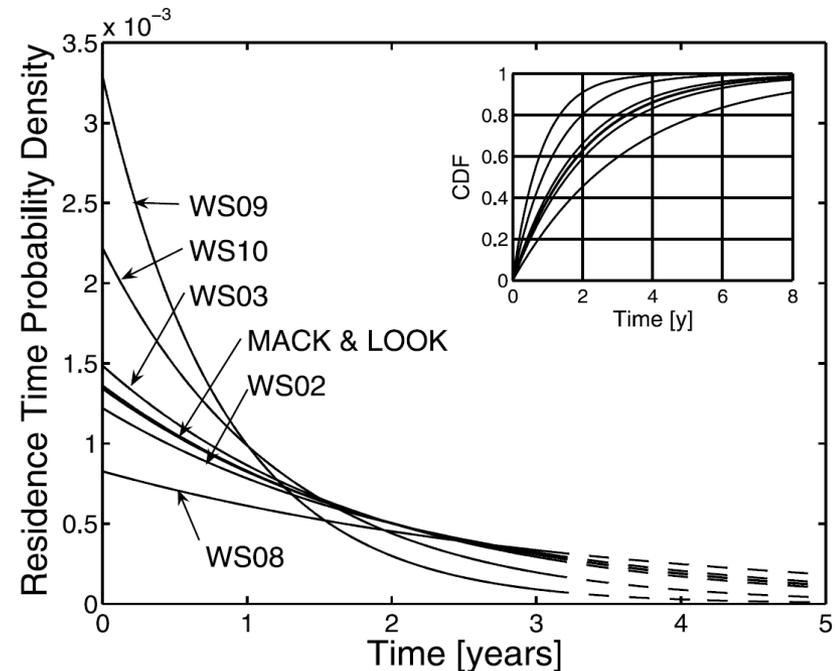


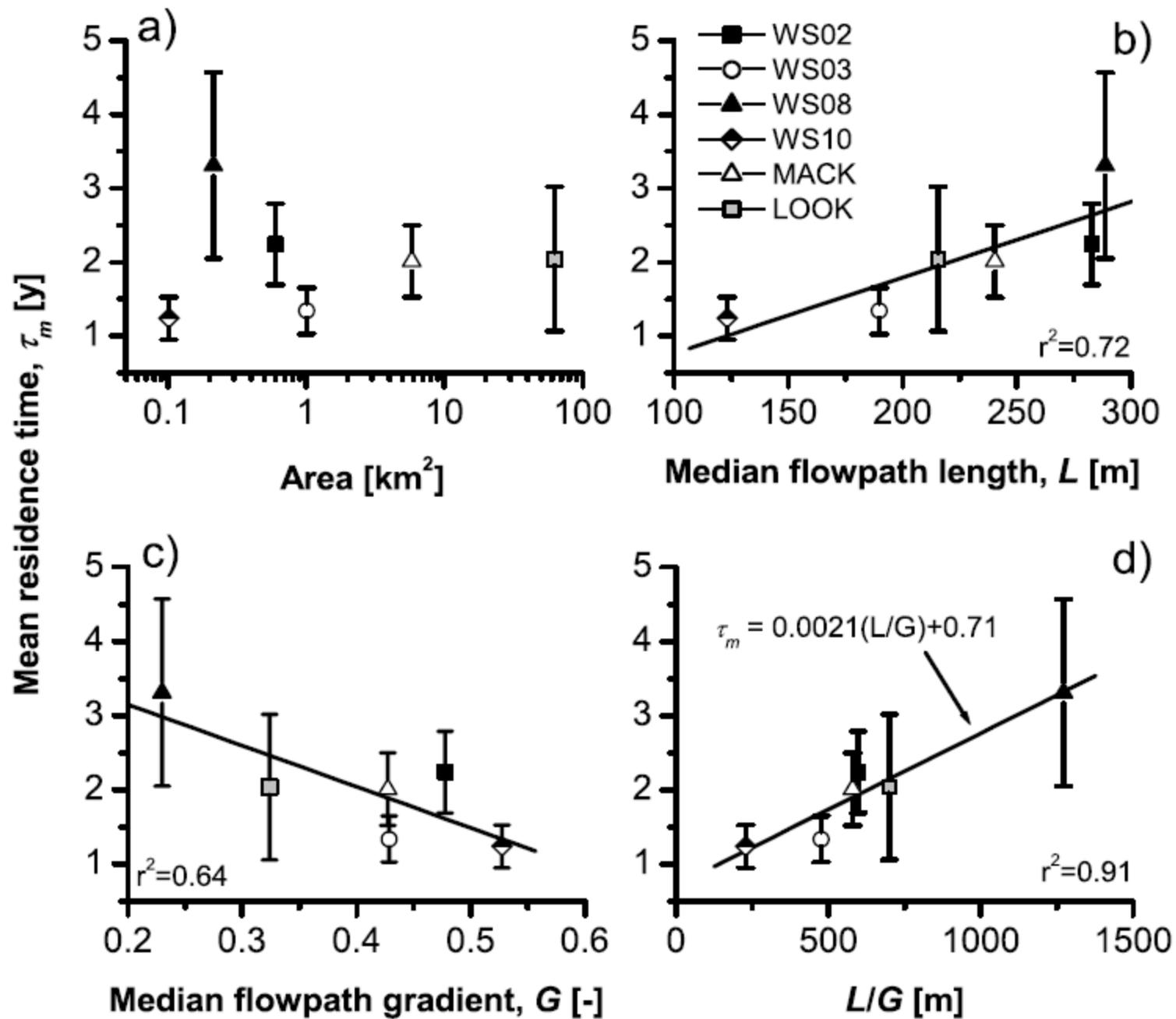
McGuire et al.  
2005  
WRR

# Baseflow transit time distributions



- Mean residence times are long (years)
- What catchment properties control distribution?

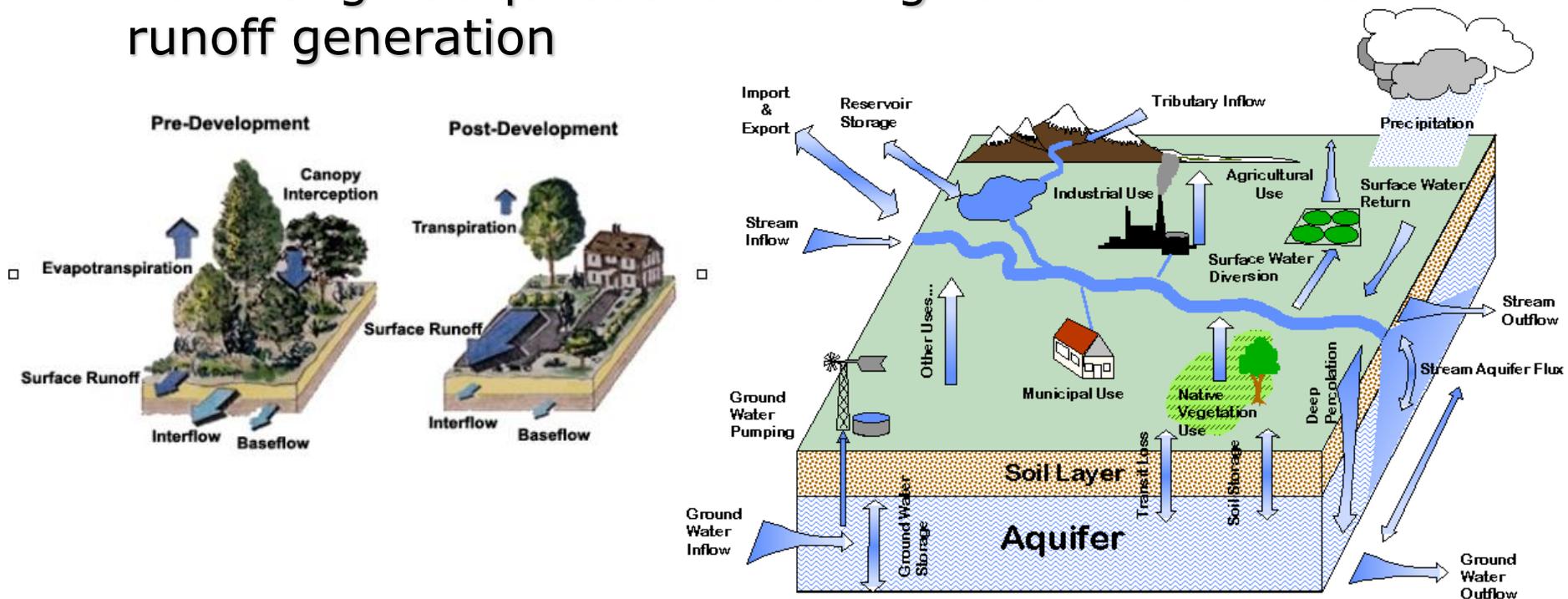




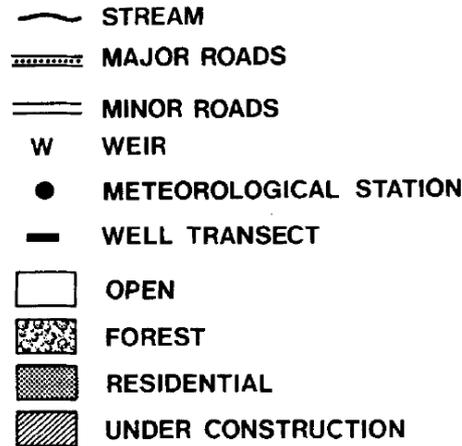
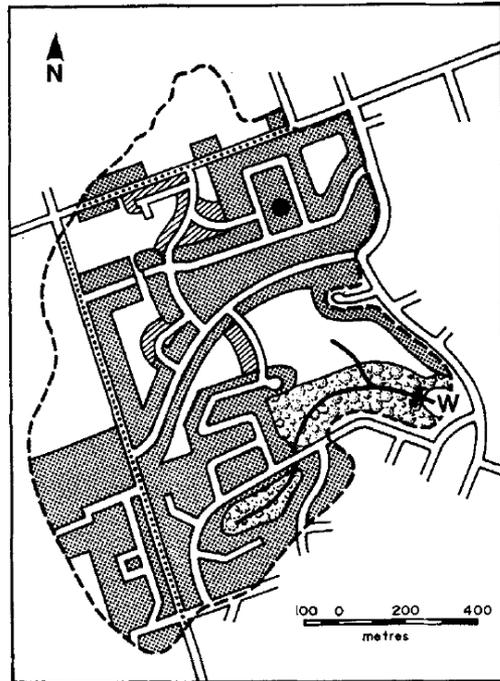
# 5. Urban and agricultural systems do not (always) export old water

✦ Relatively few studies have investigated transit times and runoff routing in large catchments and human-dominated systems

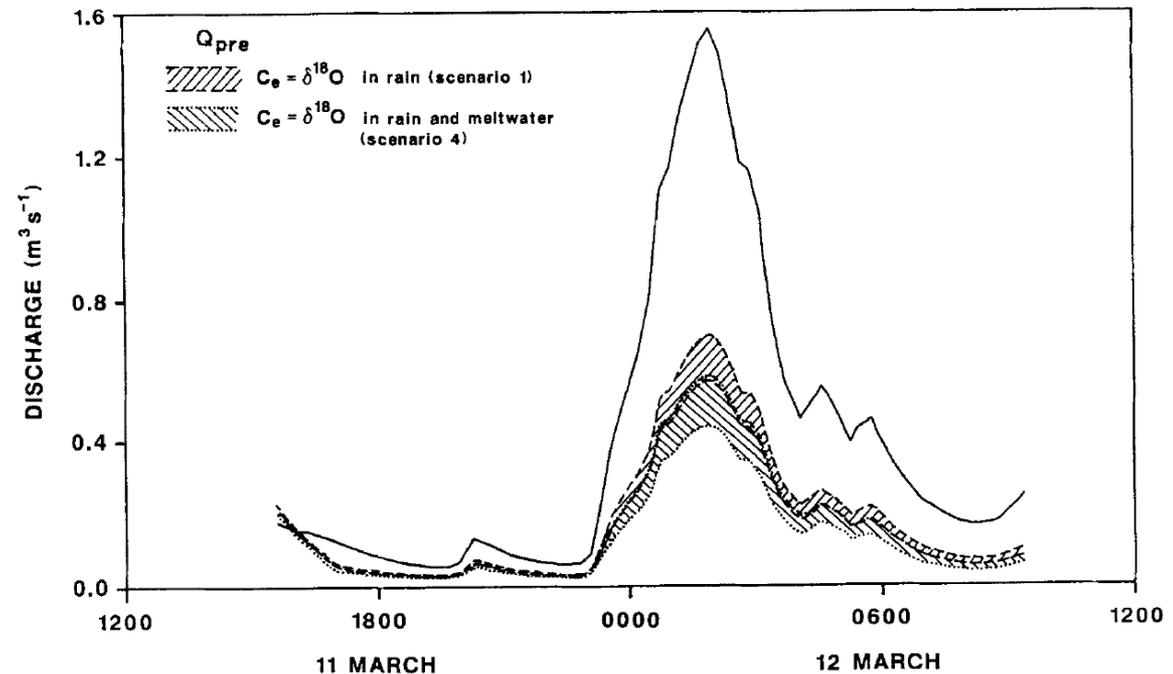
✦ LOTS of great questions relating to land-use effects on runoff generation



# Hydrograph separation - suburban

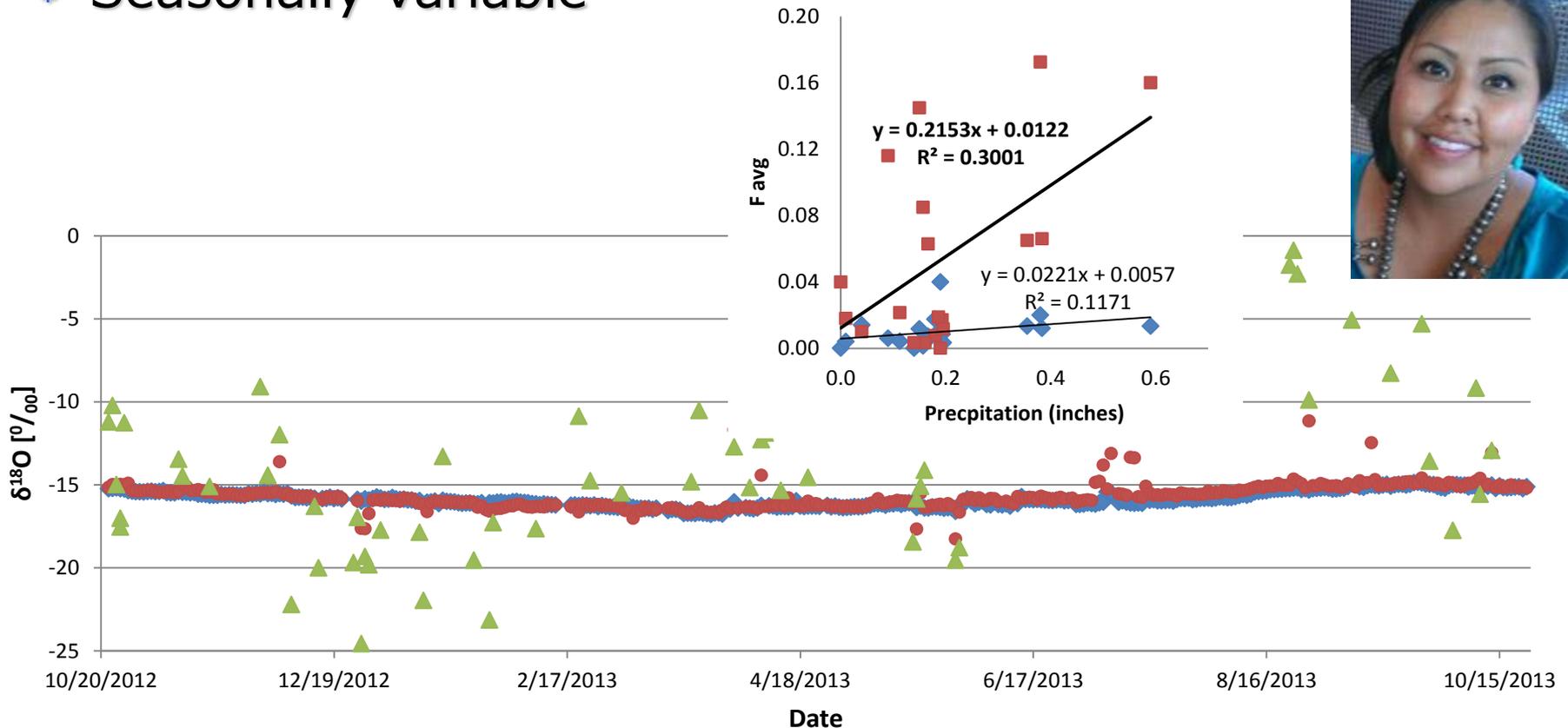


⊕ Pre-event water  
<33% of storm  
runoff



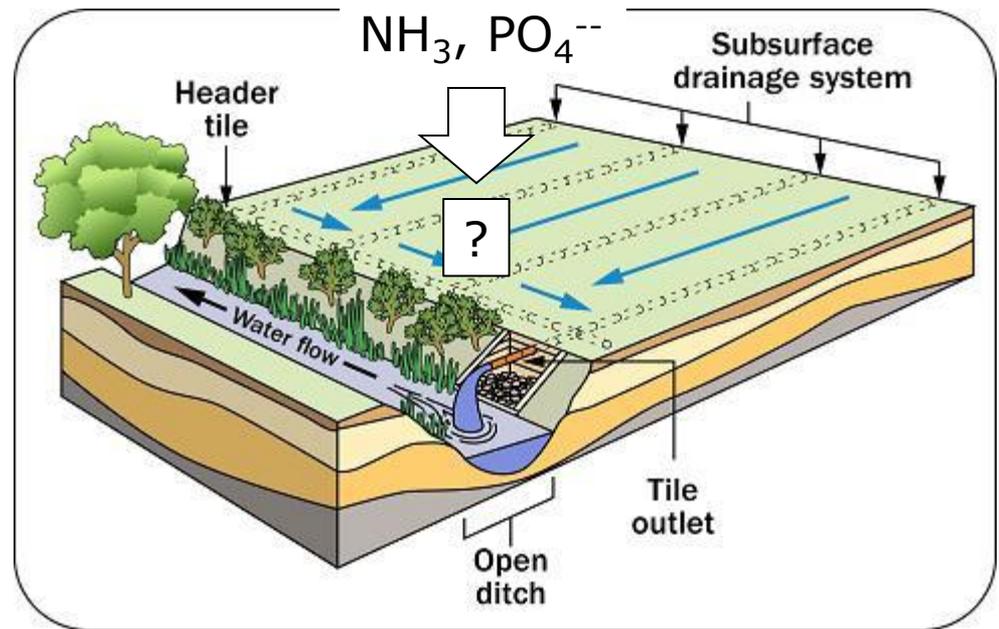
# Urban system – Red Butte Creek

- ⊕ Rapid and substantial addition of storm water in lower developed reach of catchment (UU campus)
- ⊕ Seasonally variable



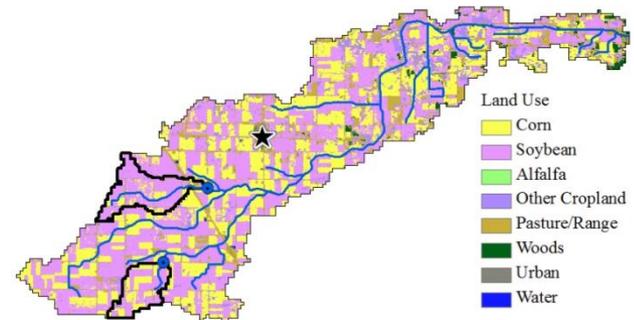
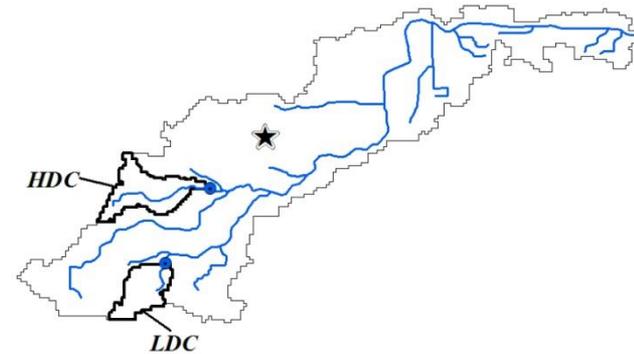
# Agricultural systems – artificial drainage

- ✦ Subsurface drain network increases agricultural land quality
- ✦ Fundamentally alters hydrological flow
- ✦ What is the impact on timing, magnitude of nutrient discharge from these lands?



# Hoagland watershed

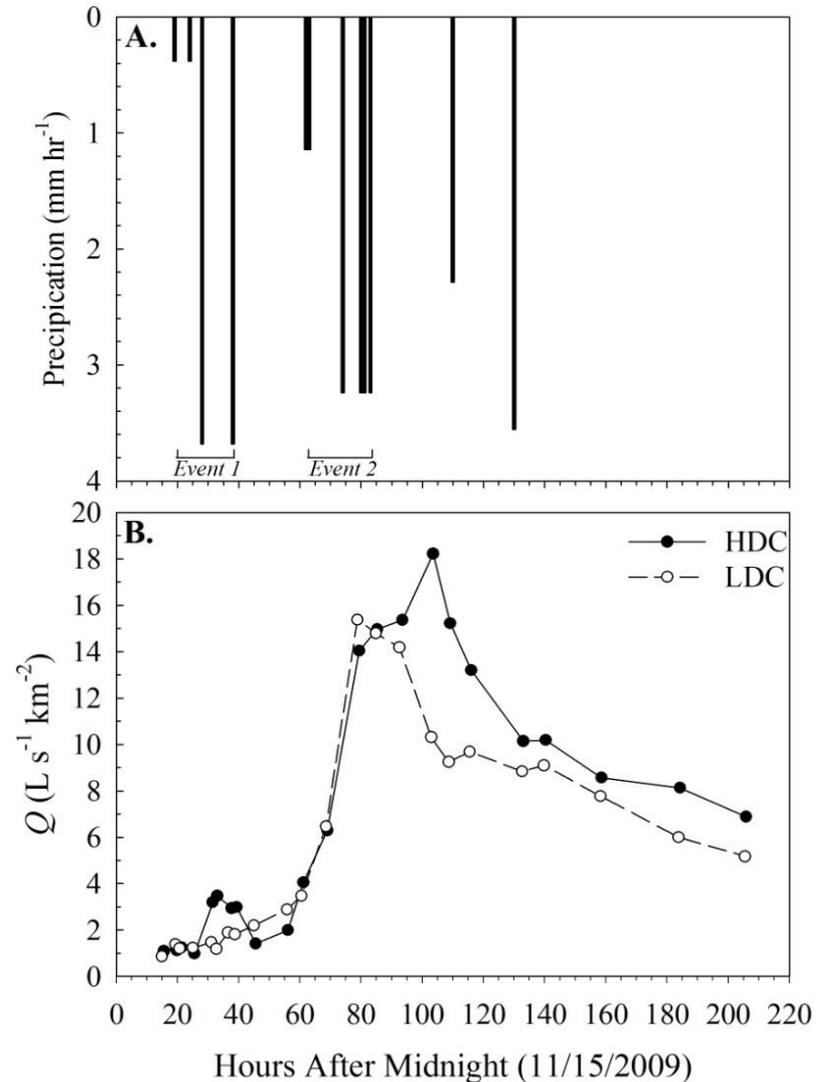
- ⊕ Paired catchment study
- ⊕ High and Low drainage density catchments
- ⊕ Sampling for water quality, isotopes through Nov. storm
- ⊕ Student participation (EAS591 Isotope Hydrology)





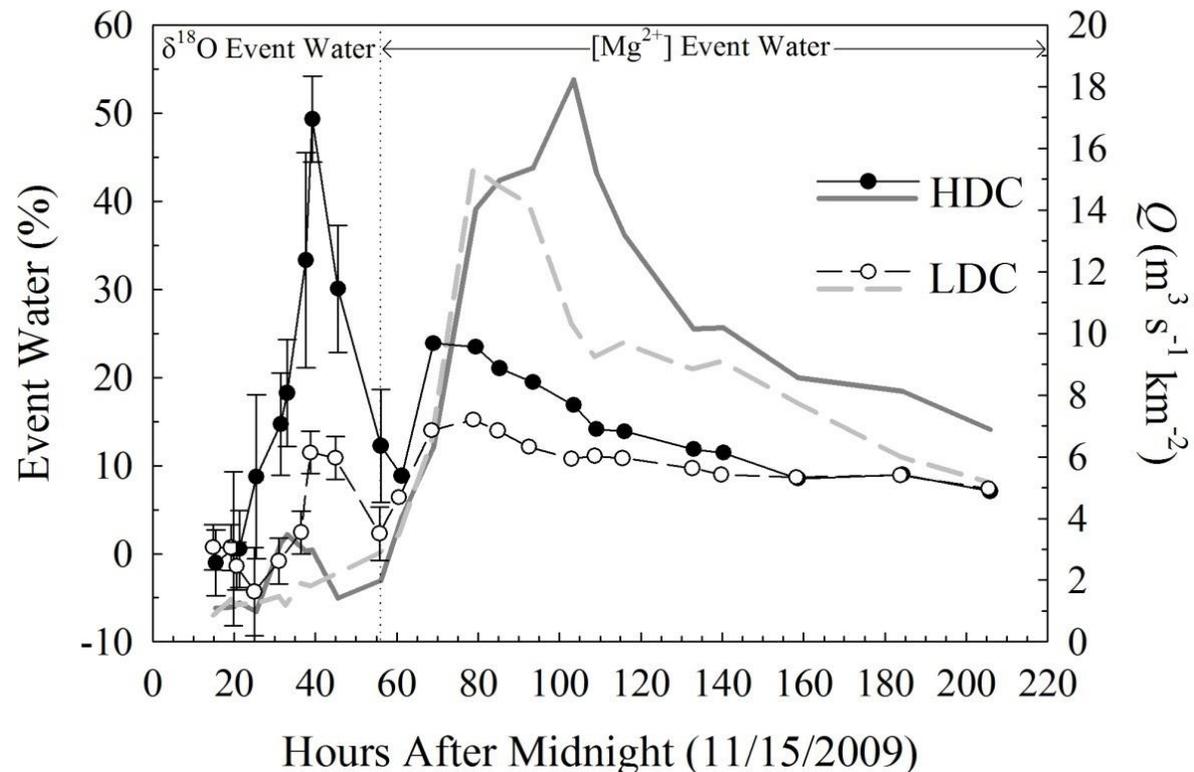
# Storm hydrograph

- ⊕ Different timing of discharge for the high- and low-drainage catchments



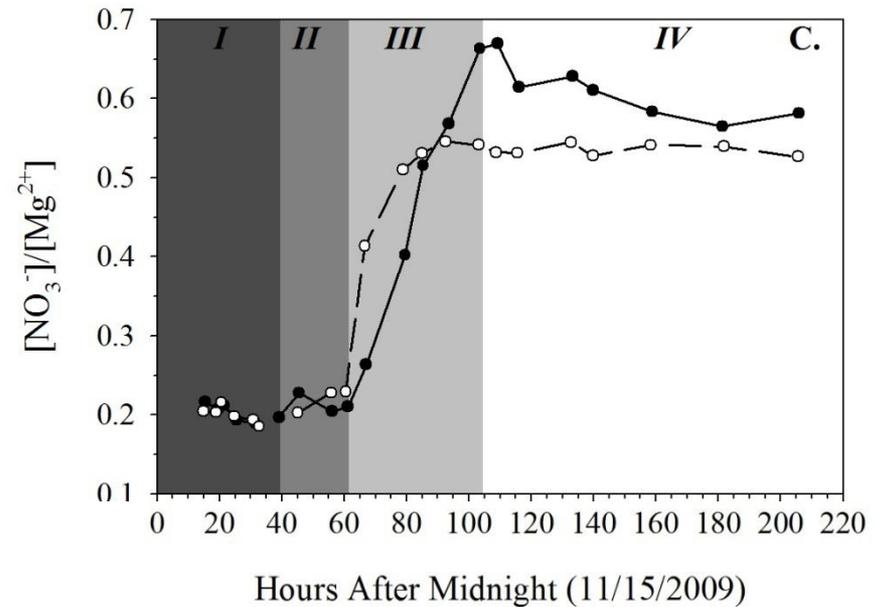
# Hydrograph separation

- Partitioned storm flow into event and pre-event water components using O isotopes,  $Mg^{2+}$
- Faster routing of storm water to stream in high-drainage catchment
- Change in storm water routing through event



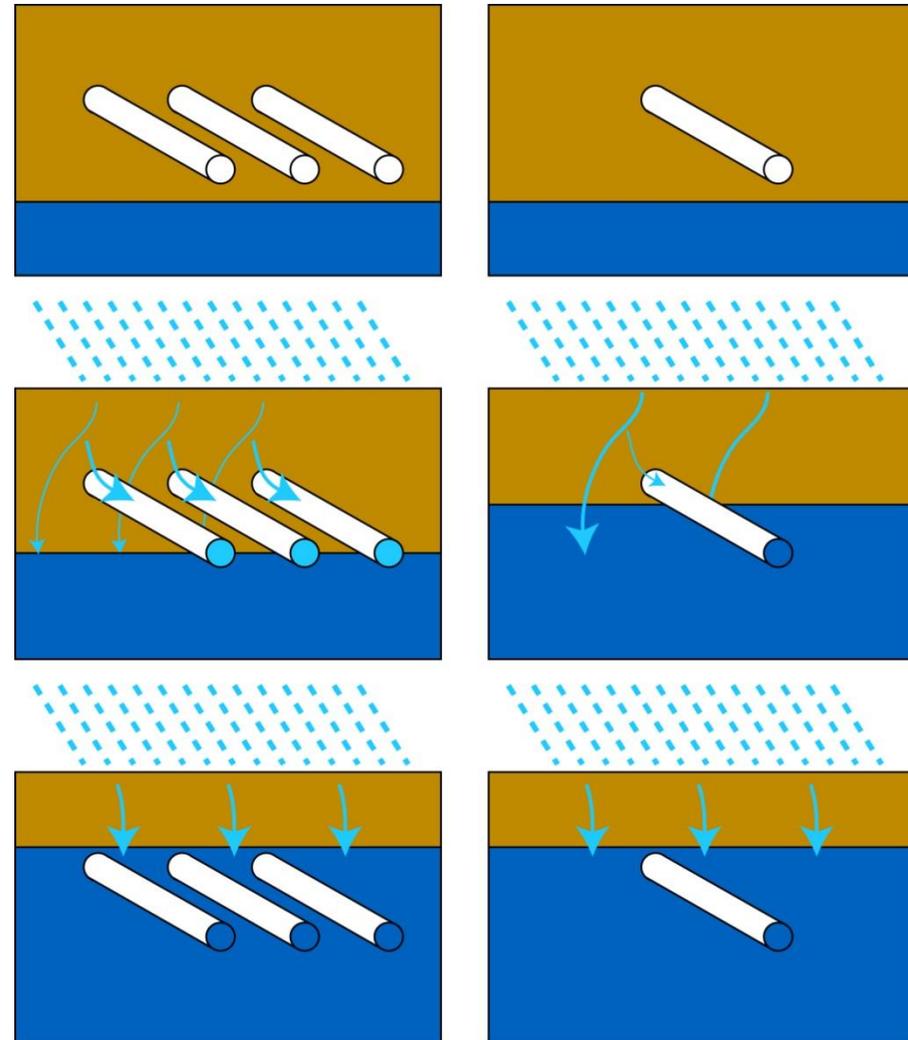
# Nutrient discharge

- Timing and magnitude of peak nitrate discharge different in the two catchments



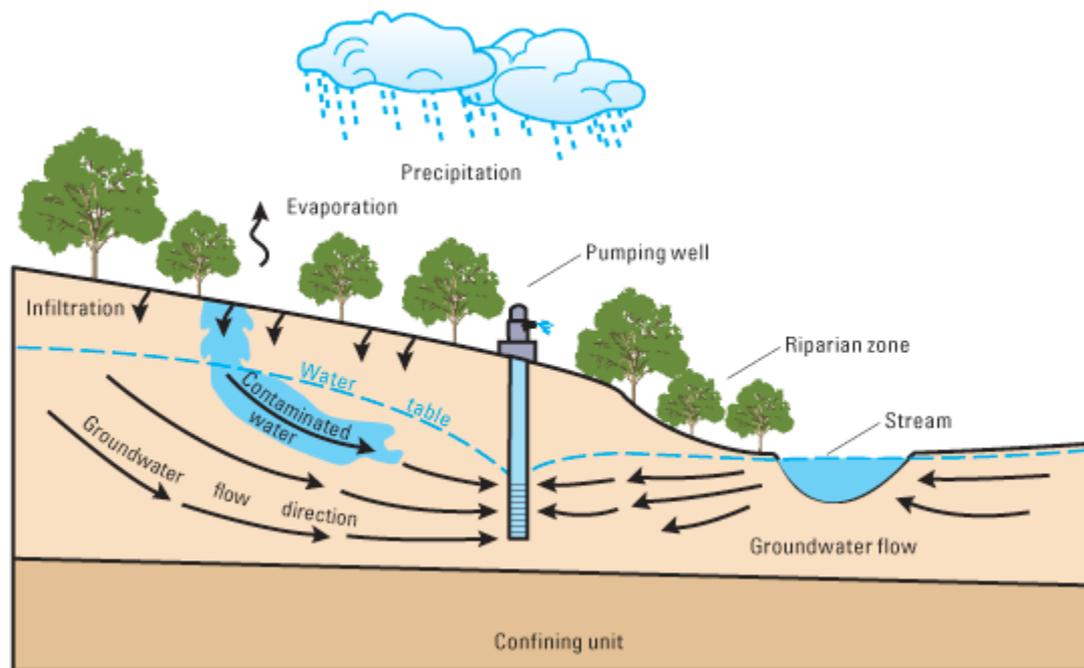
# Flush/bypass model

- ⊕ Late season, drains largely inactive
- ⊕ Drains divert storm water, slowing water table recharge
- ⊕ Drains activation and discharge of high-N groundwater lags in high-drainage catchment
- ⊕ Diversion of infiltration changes 'flashiness' of contaminant export

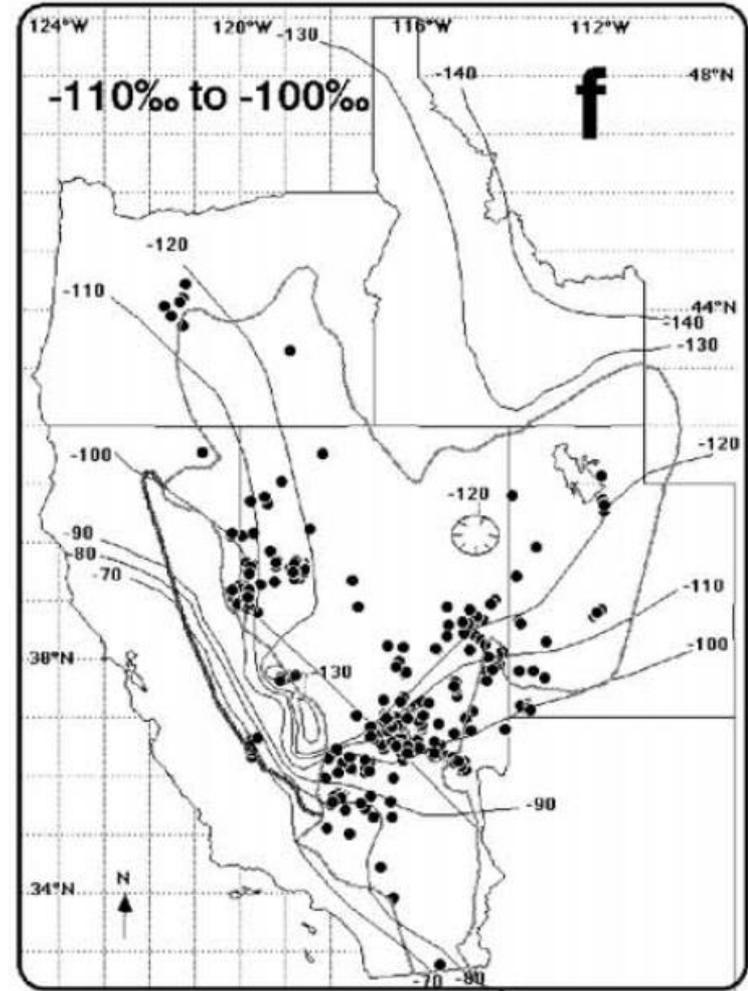
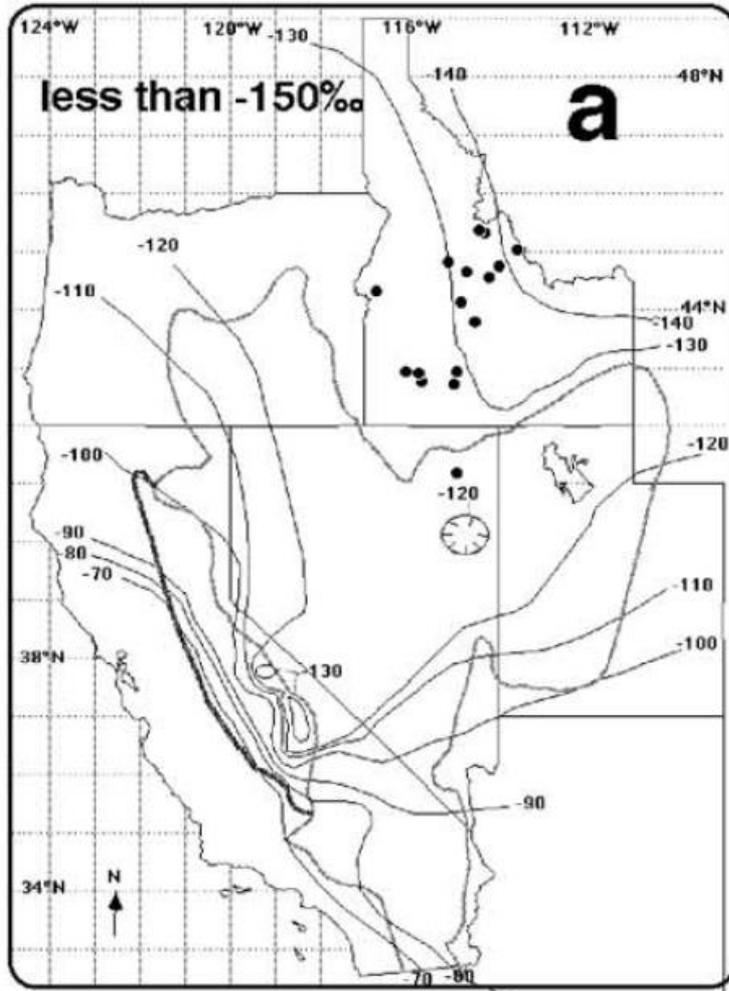


# 6. Groundwater looks like local precipitation, except when it isn't

- ⊕ In most cases groundwater is a well mixed integrator of infiltration
- ⊕ Dogma is that groundwater values usually approximate those of 'annual average precipitation'
  - ⊕ Unbiased recharge



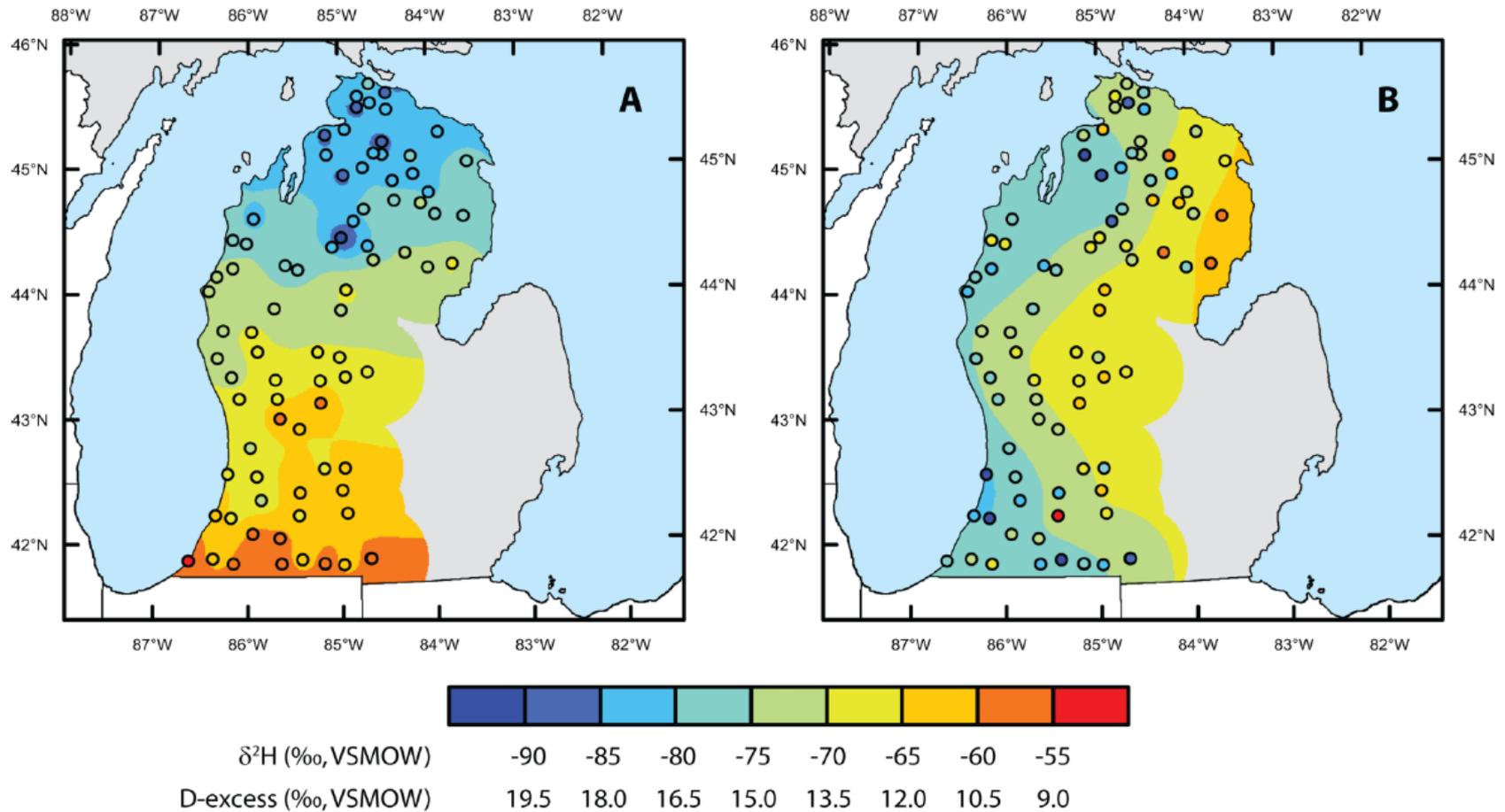
# Great Basin waters





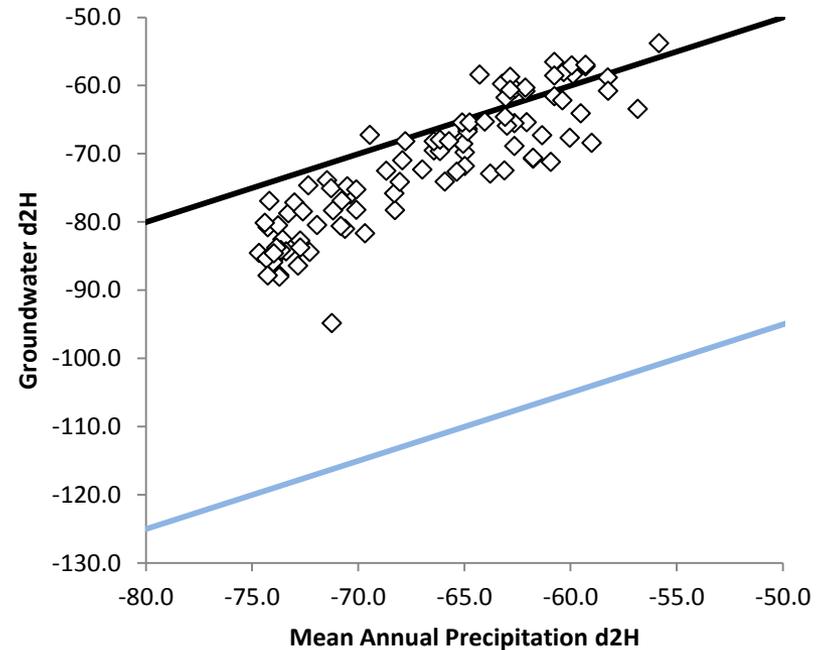


# Michigan shallow groundwater



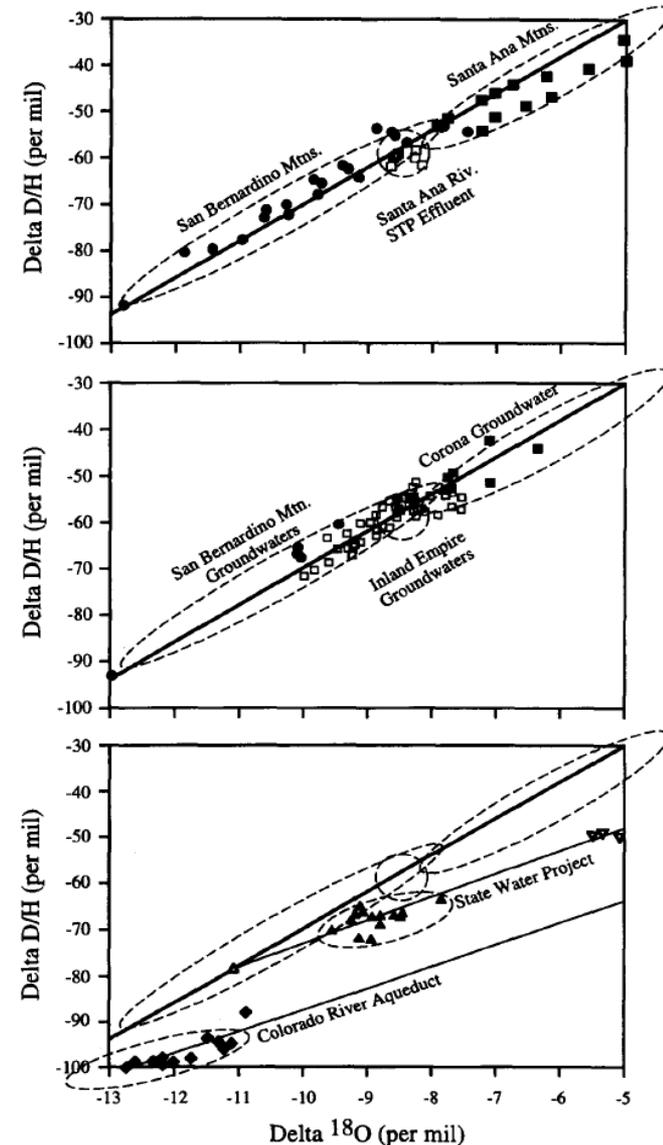
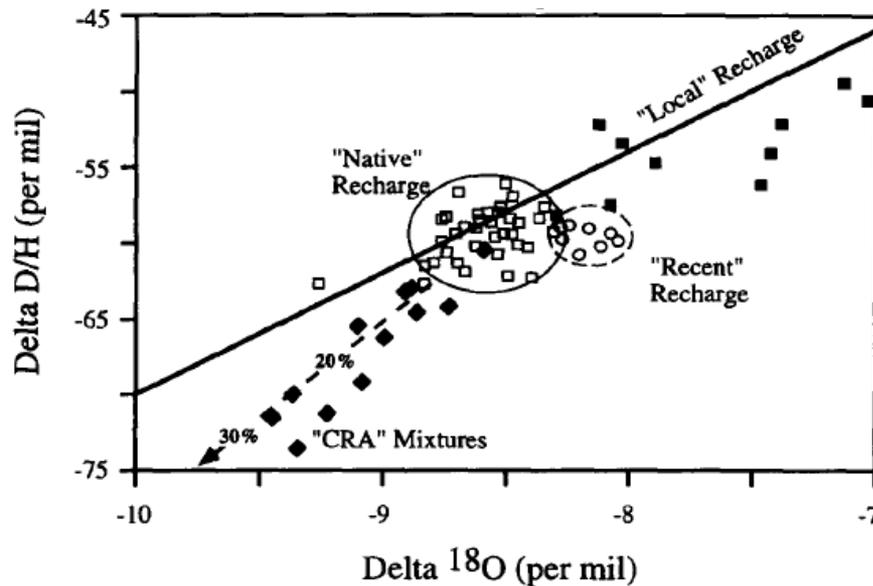
# Michigan shallow groundwater

- ✦ Patterns match precipitation data, predictions to first order
- ✦ Systematic offset (ground water lighter than mean annual precipitation)
  - ✦ Increases with latitude
- ✦ Seasonally biased GW recharge

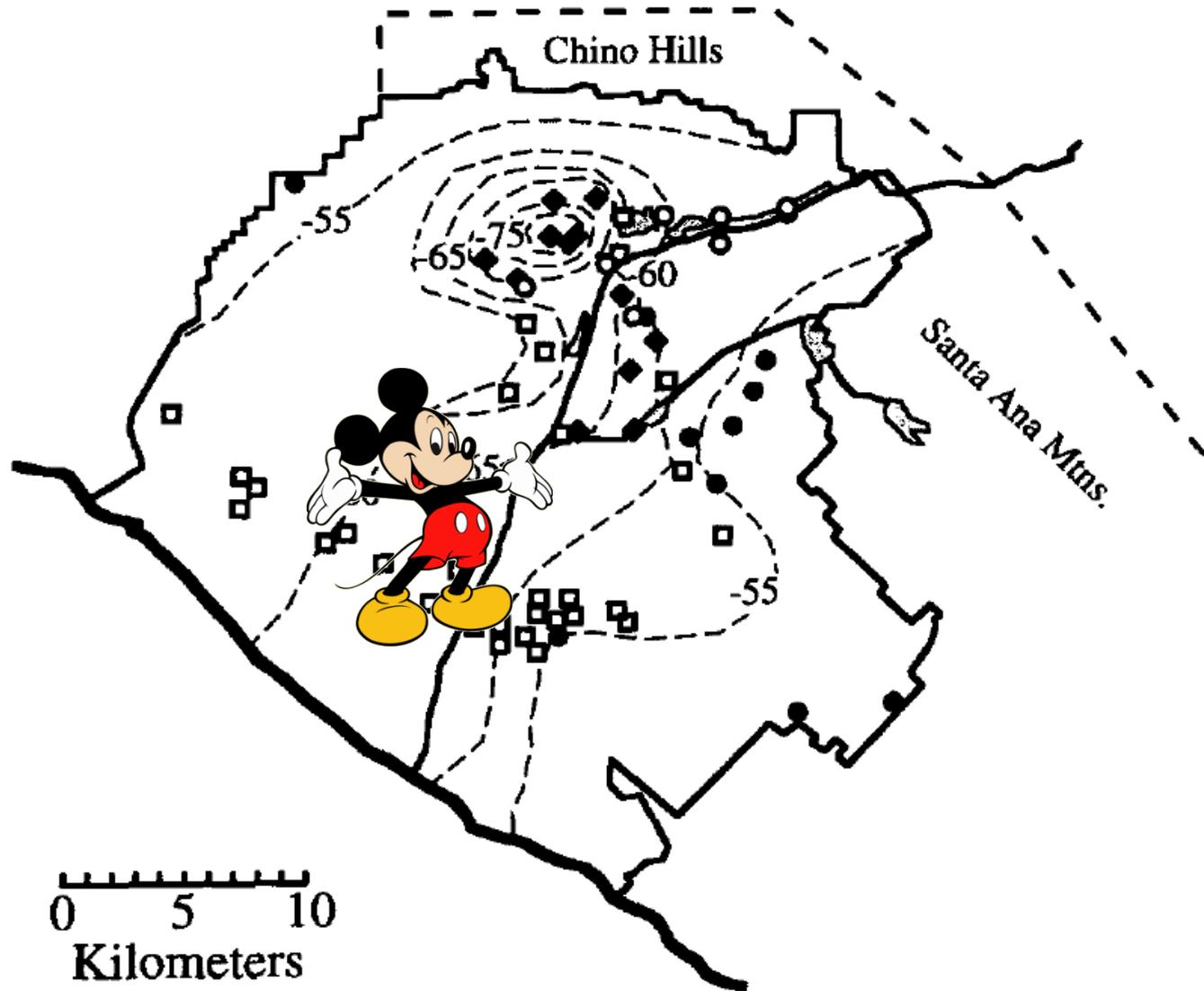


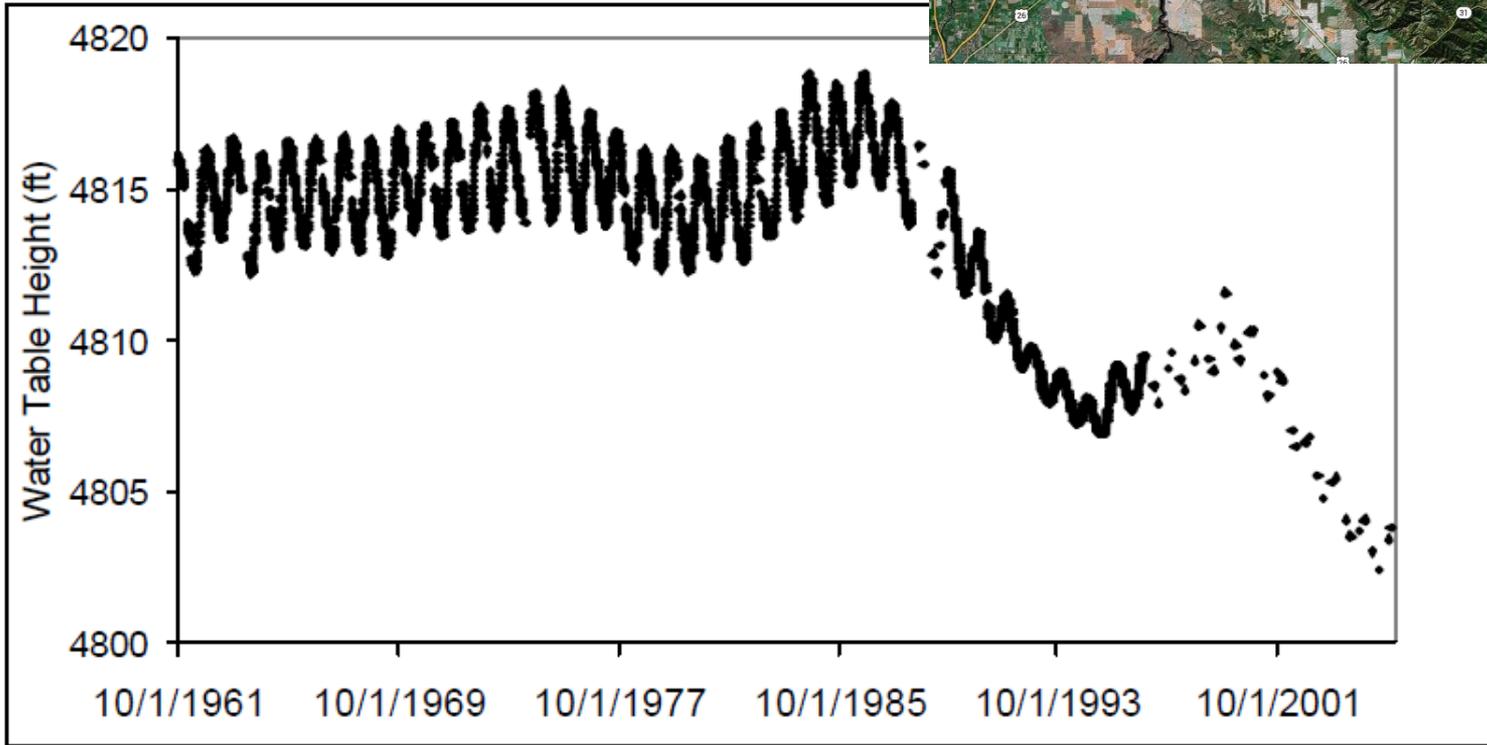
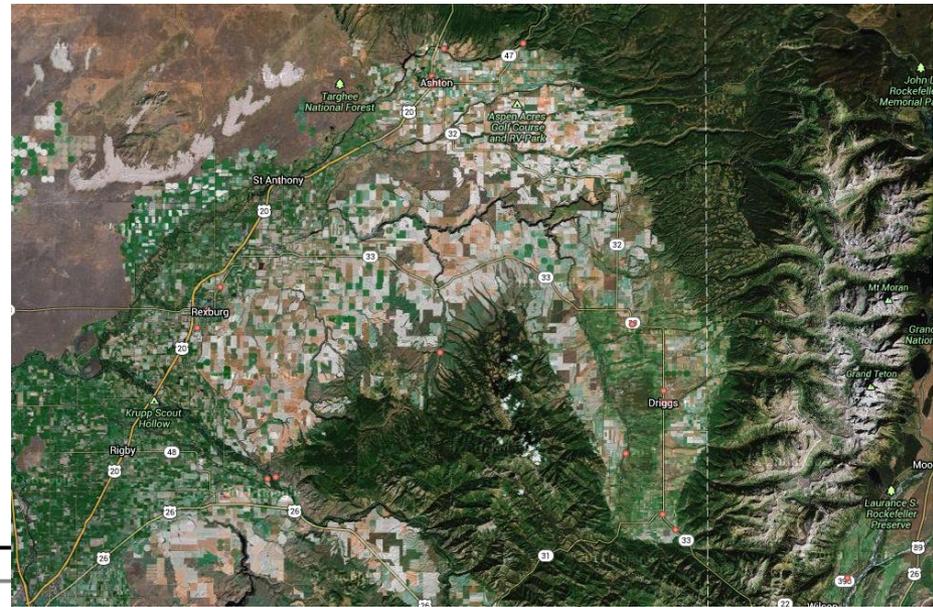
# Humans – another dimension

- ⊕ Not all recharge is 'natural'
  - ⊕ Purposeful (storage)
  - ⊕ Inadvertent (leakage)
- ⊕ Transported water signatures



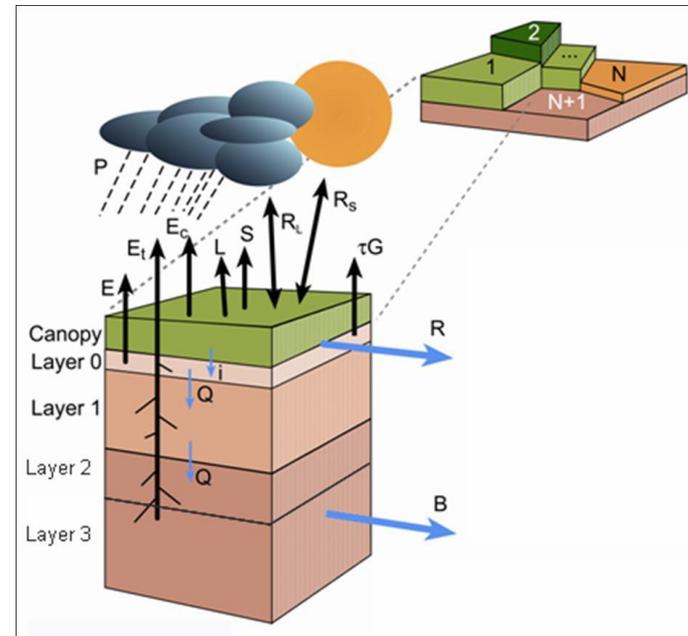
# Artificial recharge



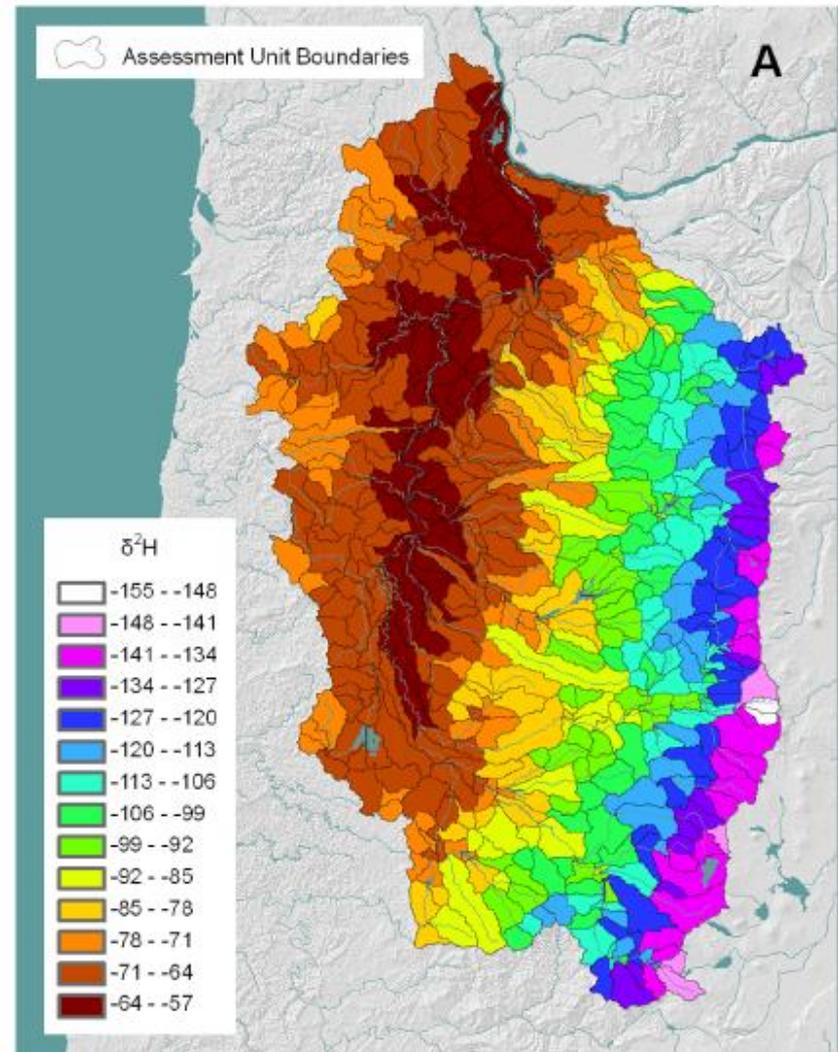
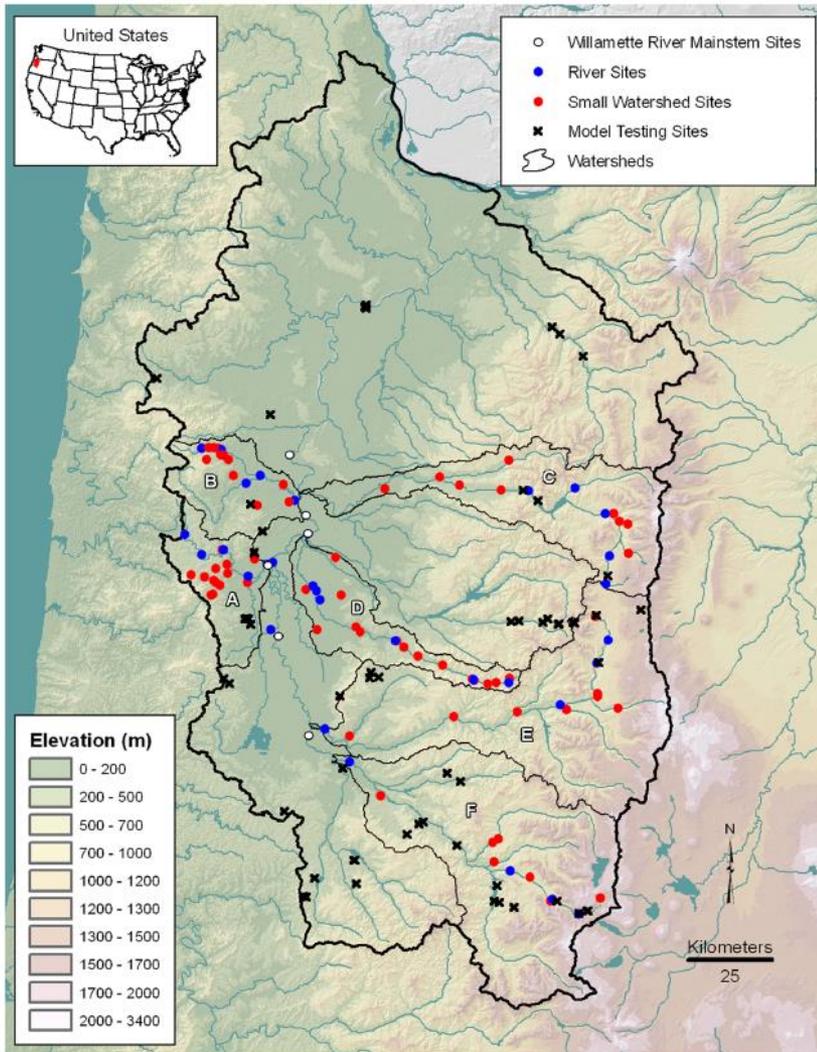


# 7. Regional water balance trends are easy to extract from rivers

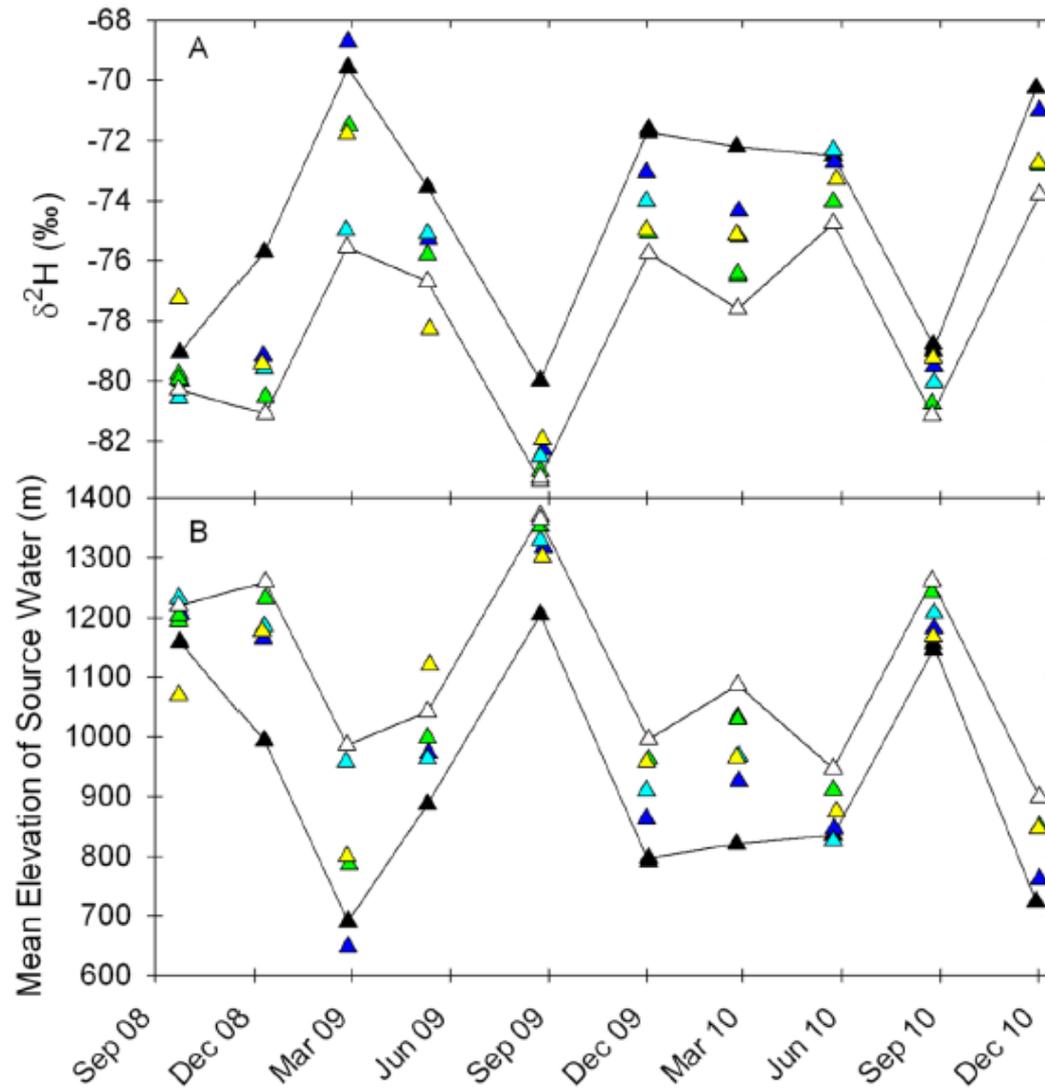
- ⊕ Many (not all) properties of catchments exhibit regional consistency
  - ⊕ Climatic
  - ⊕ Topographic
  - ⊕ Geological
  - ⊕ Biological
- ⊕ Can isotopes be used to identify key properties and characterize catchments?



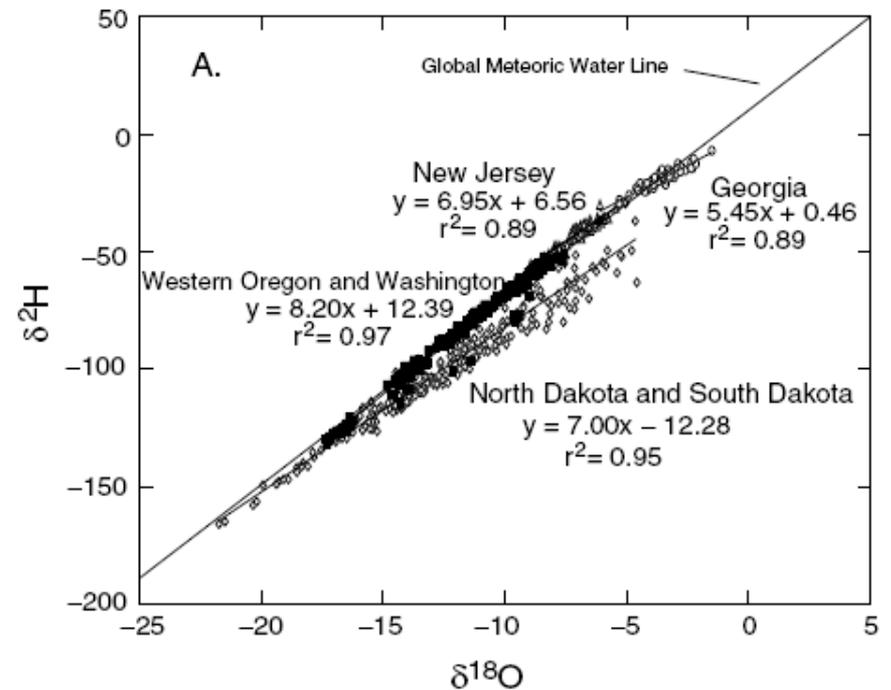
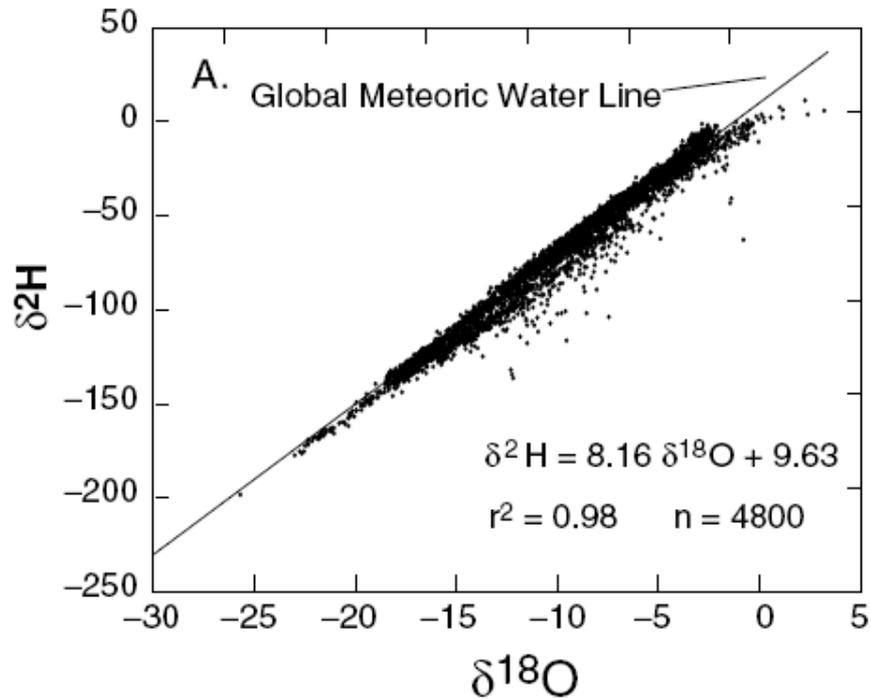
# Oregon rivers



# Willamette River



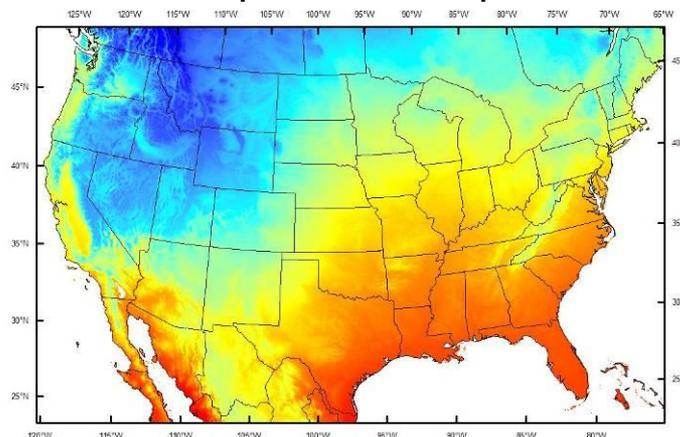
# River water isotopes – continental scale



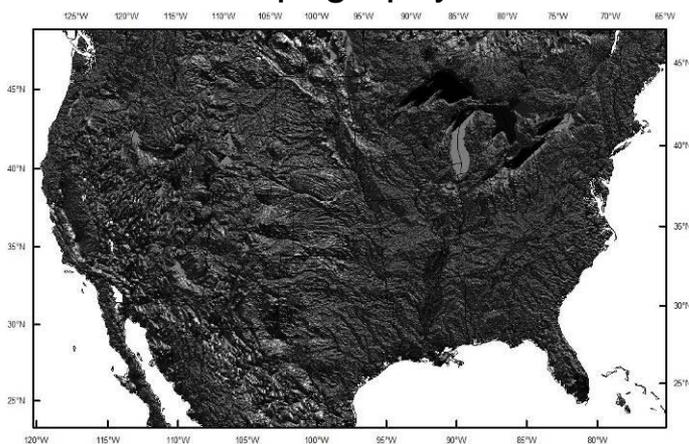
# River water isotopes: rainfall-runoff model

- ⊕ Can we reproduce isotope differences between surface water and precipitation using process models?

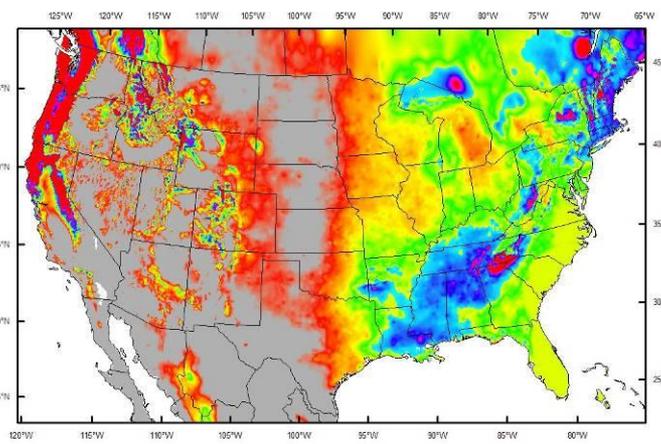
Precipitation isotopes



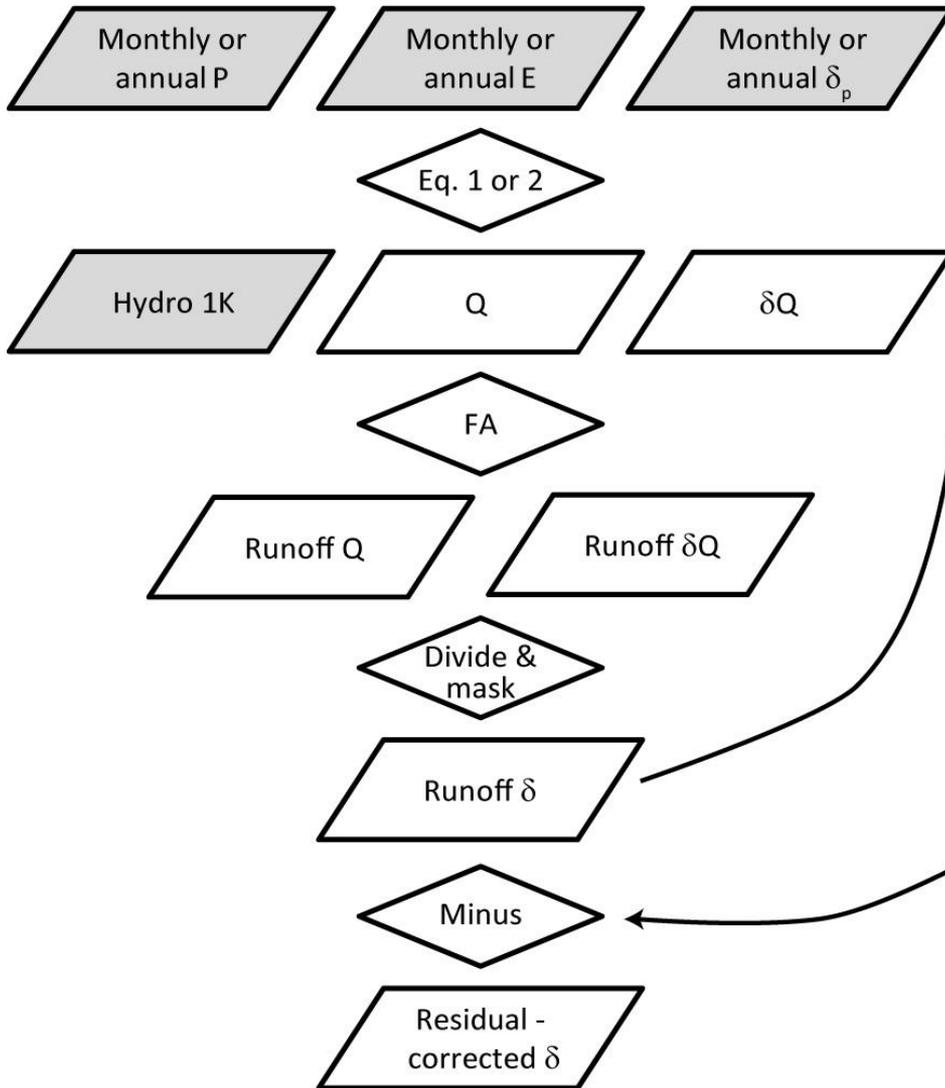
Topography



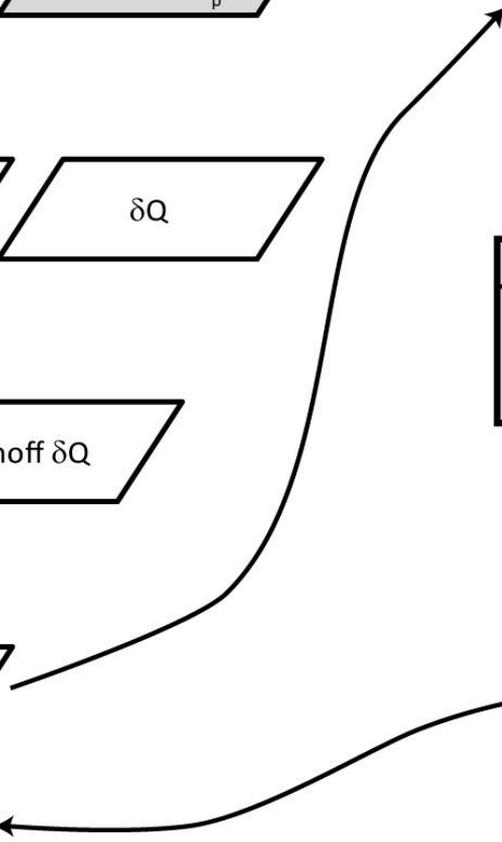
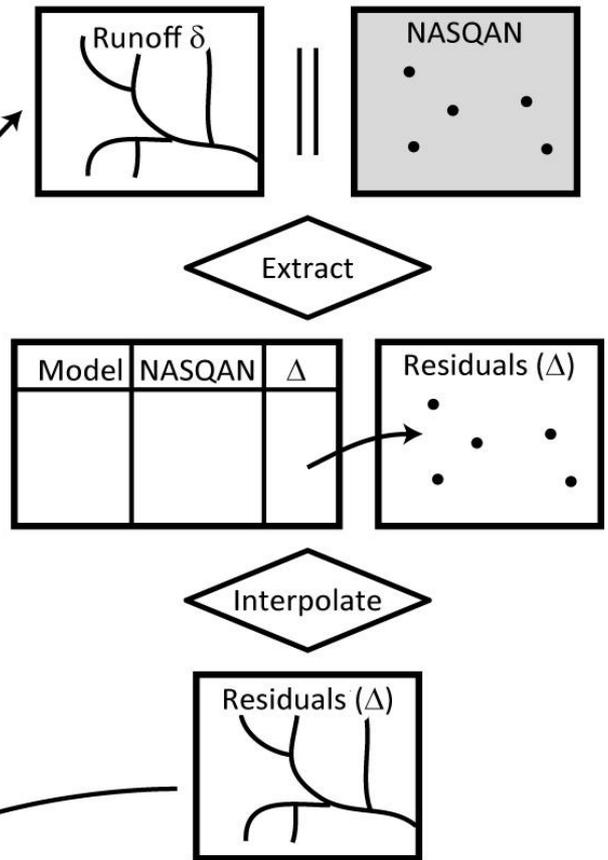
Runoff amount



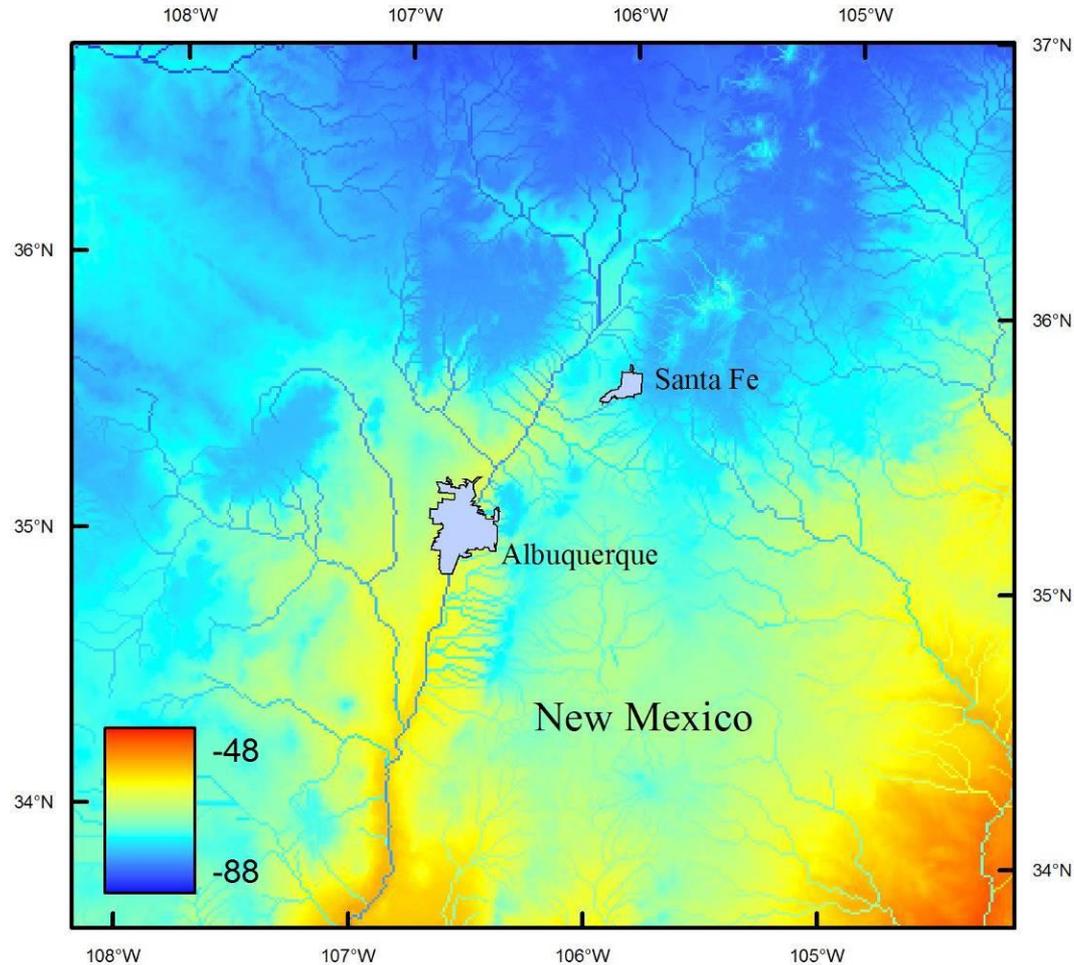
# Modeling



# Validation

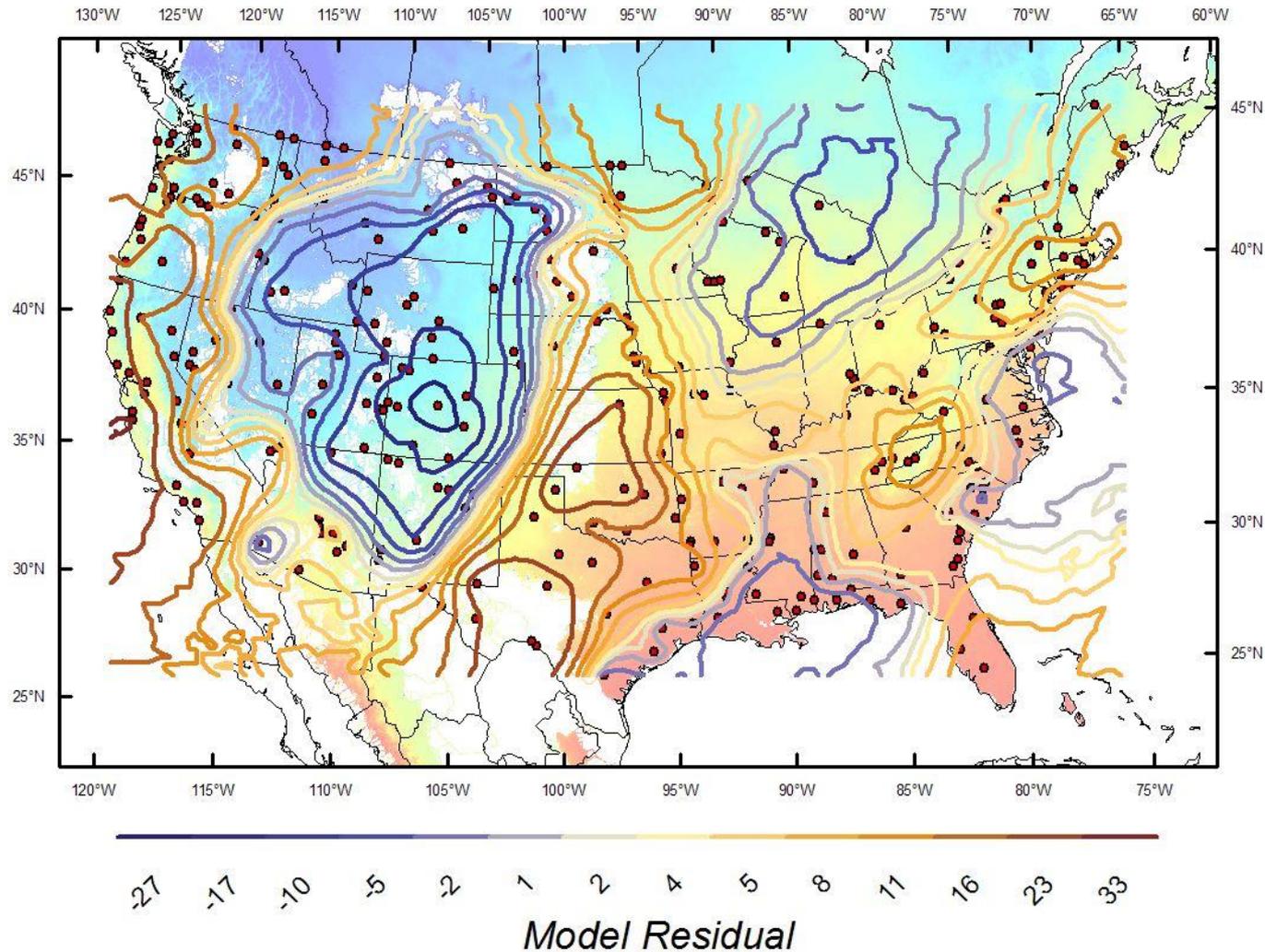


# Runoff model



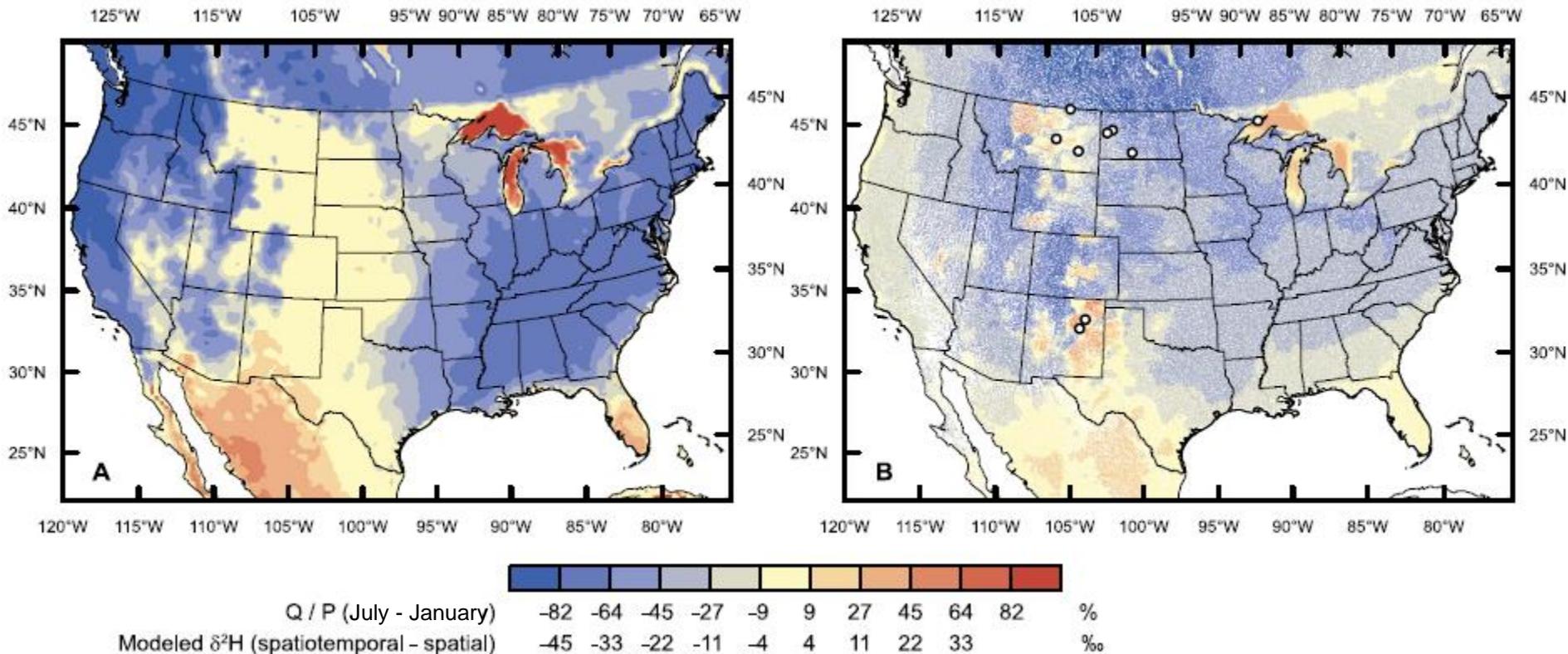
Predicted river  $\delta^2\text{H}$  values superimposed on precipitation  $\delta^2\text{H}$  values

# Runoff model residuals - why?



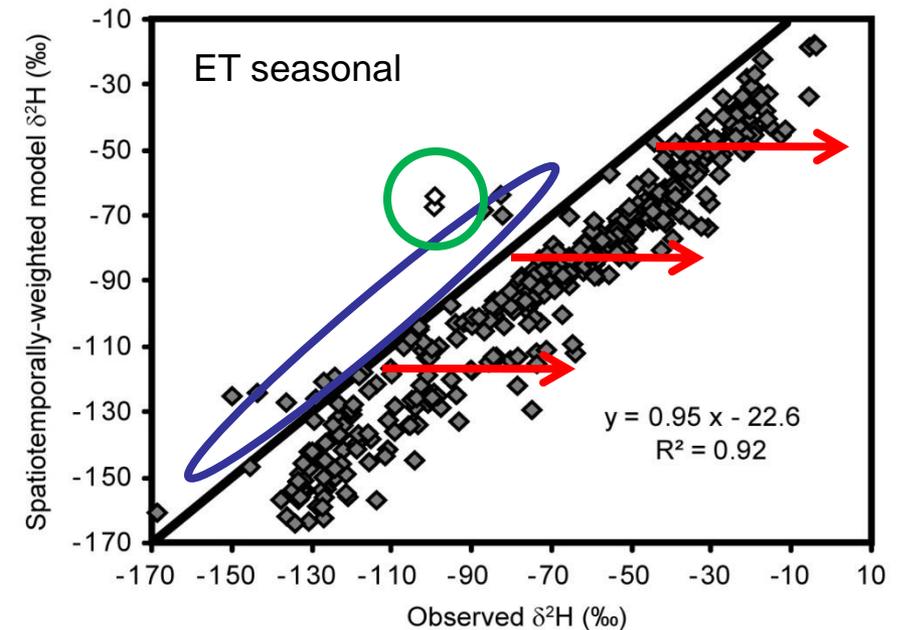
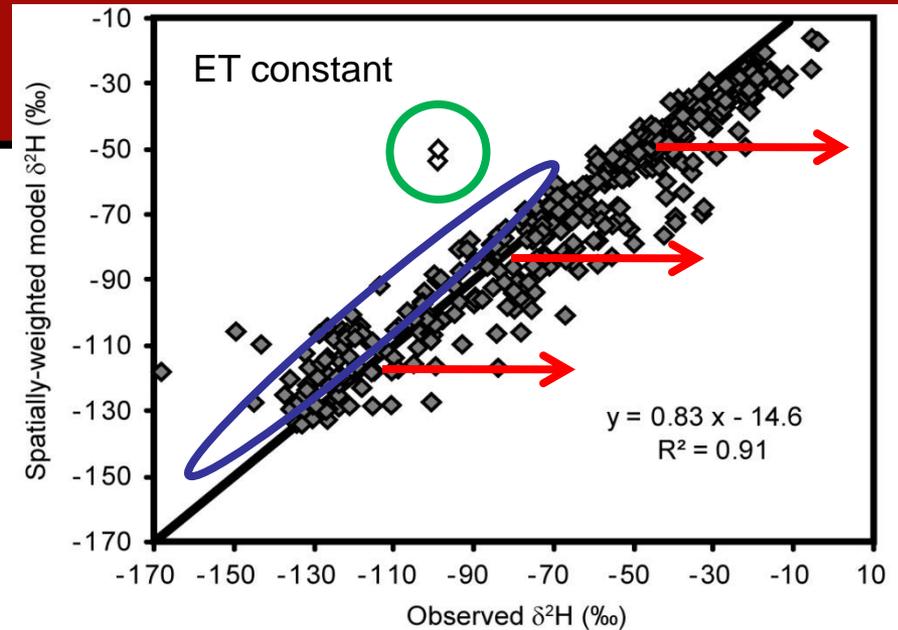
# Sensitivity testing ET patterns

Impact of accounting for different % loss of precipitation to ET by month



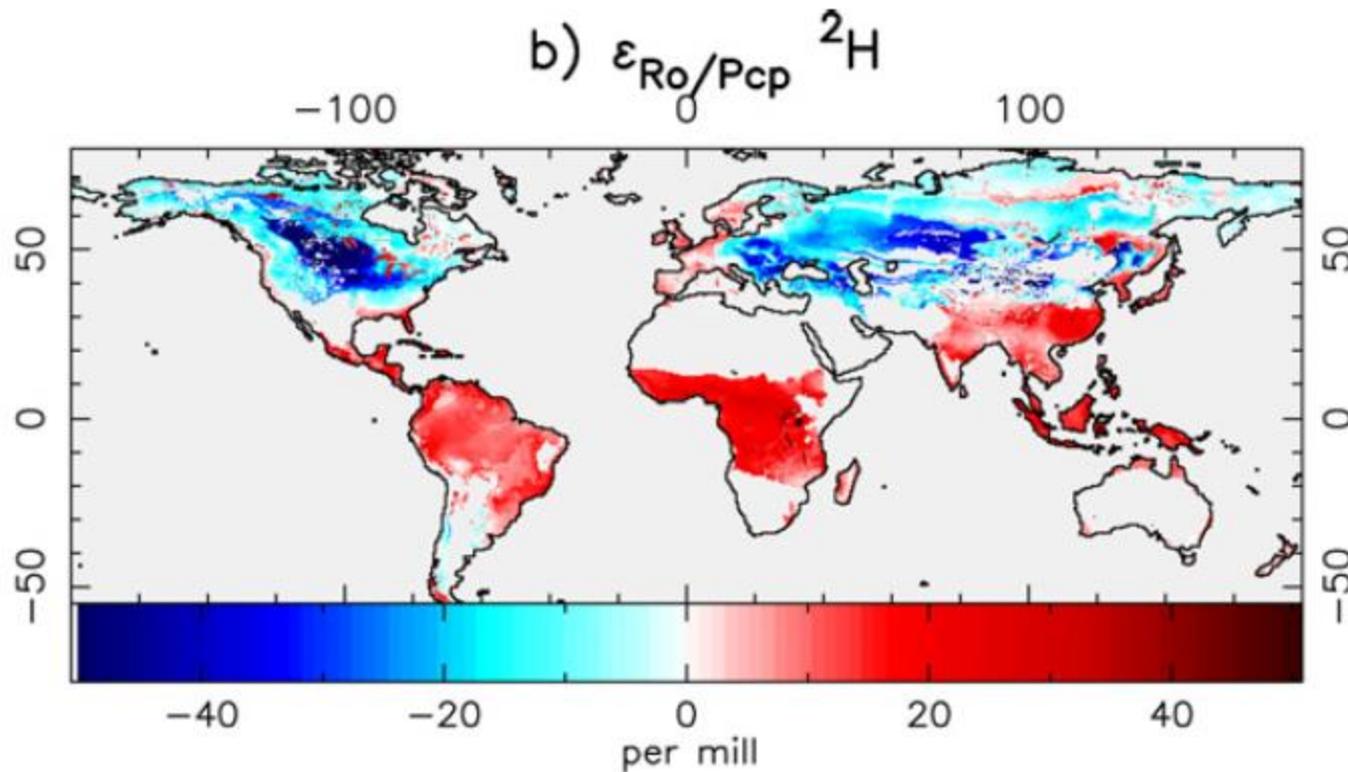
# Interrogating water source

- ⊕ Evaporation
- ⊕ Winter-biased runoff
- ⊕ Imported water
- ⊕ Provides basis for quantifying (and monitoring) seasonal or elevation bias of runoff generation
- ⊕ Identifies non-local water sources



# Distributed hydrology model w/ water isotopes

- ⊕ Same effect predicted by more sophisticated rainfall-runoff models (WBM)
- ⊕ Note contrasting pattern in N. America



# 8. Lake basins evaporate, but even more they transpire

- ⊕ Like rivers, lakes are great integrators of catchment properties, with differences
  - ⊕ Residence time
  - ⊕ Evaporation



# Isotope mass balance - lakes

- ⊕ Water isotopes add tracer to underconstrained mass balance
  - ⊕ No fractionation associated with discharge (Q)
  - ⊕ Evaporation (E) depleted in heavy isotopes
- ⊕ At steady state - leads to simple mass balance equation
- ⊕ Challenge – getting the parameter values right...

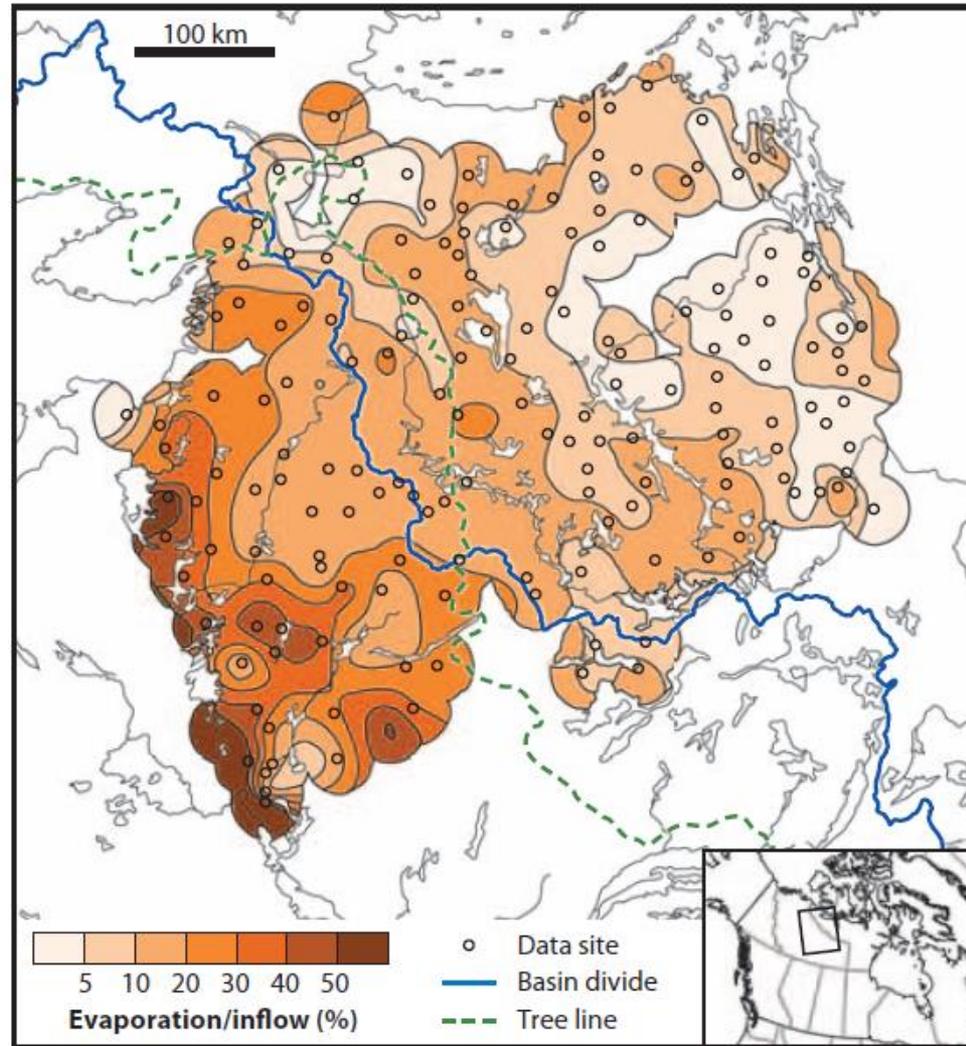
$$I_L = Q_L + E_L$$

$$I_L \delta_I = Q_L \delta_Q + E_L \delta_E$$

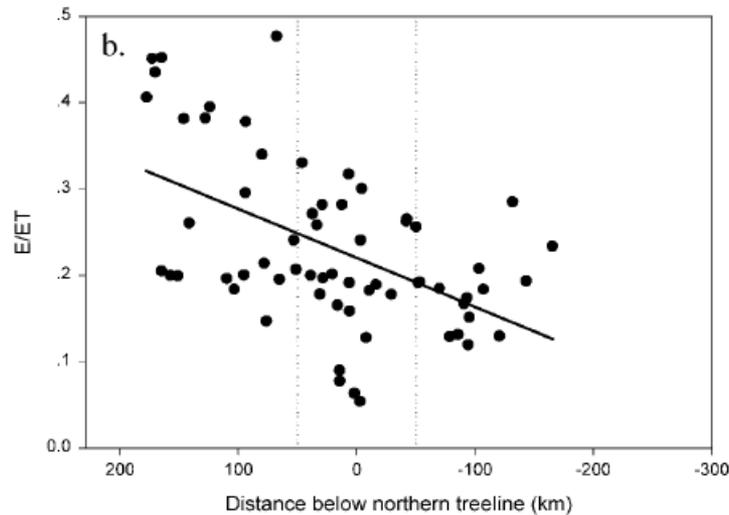
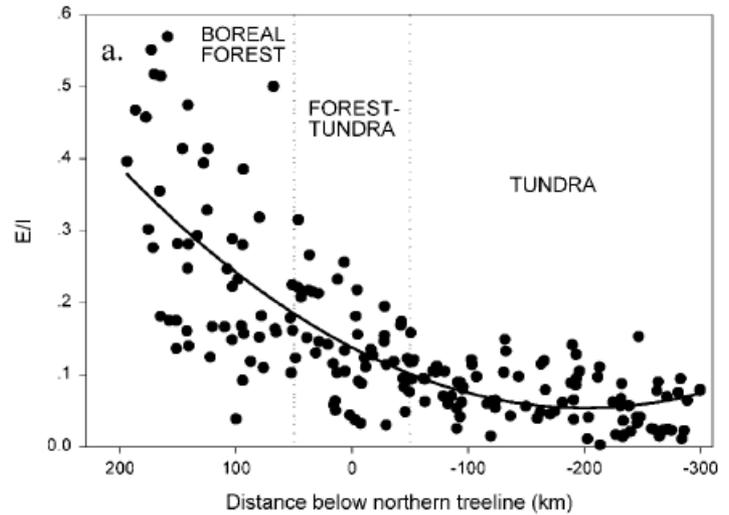
$$\frac{E_L}{I_L} = \frac{\delta_I - \delta_L}{\delta_E - \delta_L}$$

$$\delta_E = \frac{\alpha^* \delta_L - h \delta_A - \epsilon}{1 - h + 10^{-3} \epsilon_K}$$

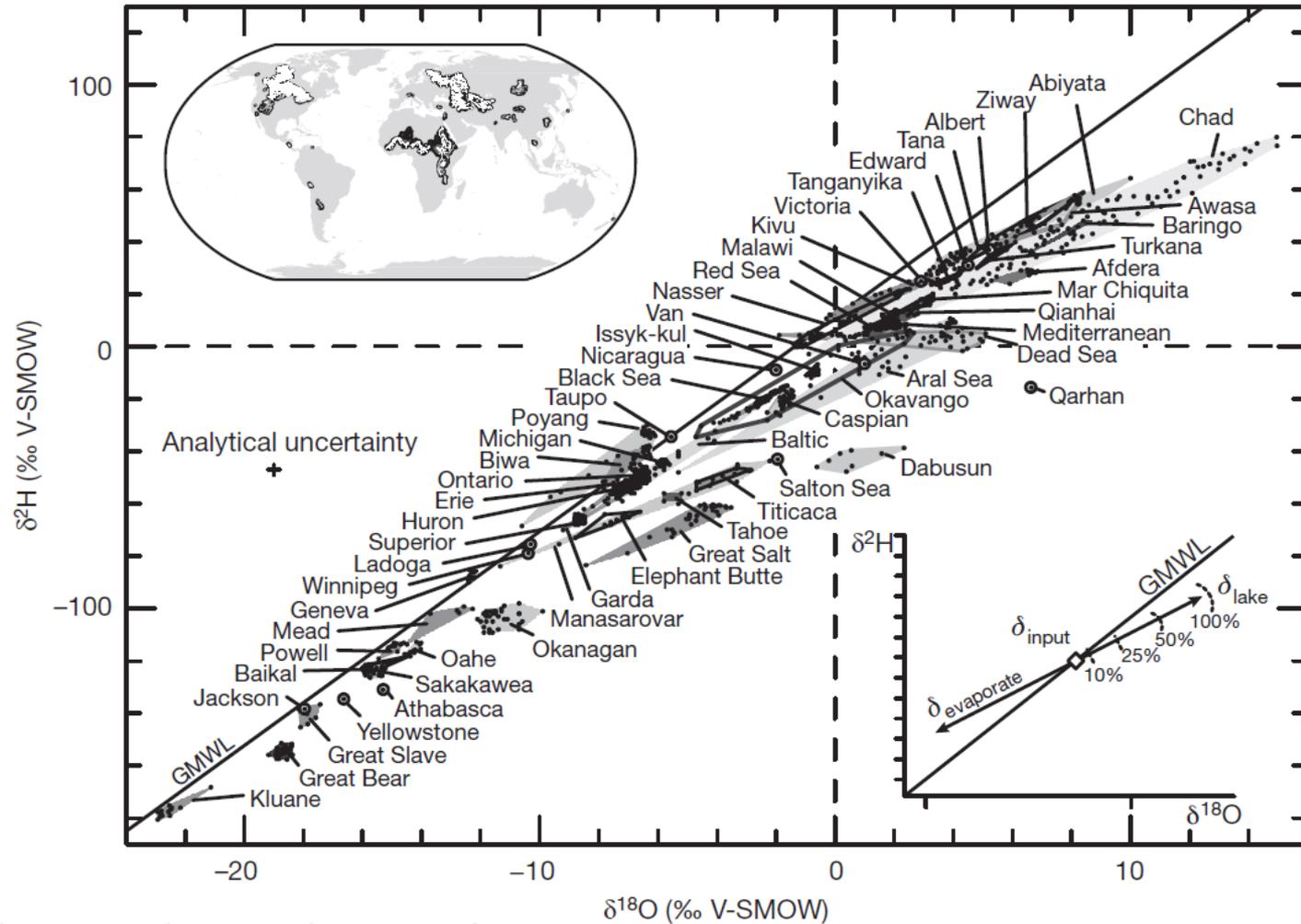
# Isoscape-based E/I, Canadian Arctic



# Water balance of Arctic lakes



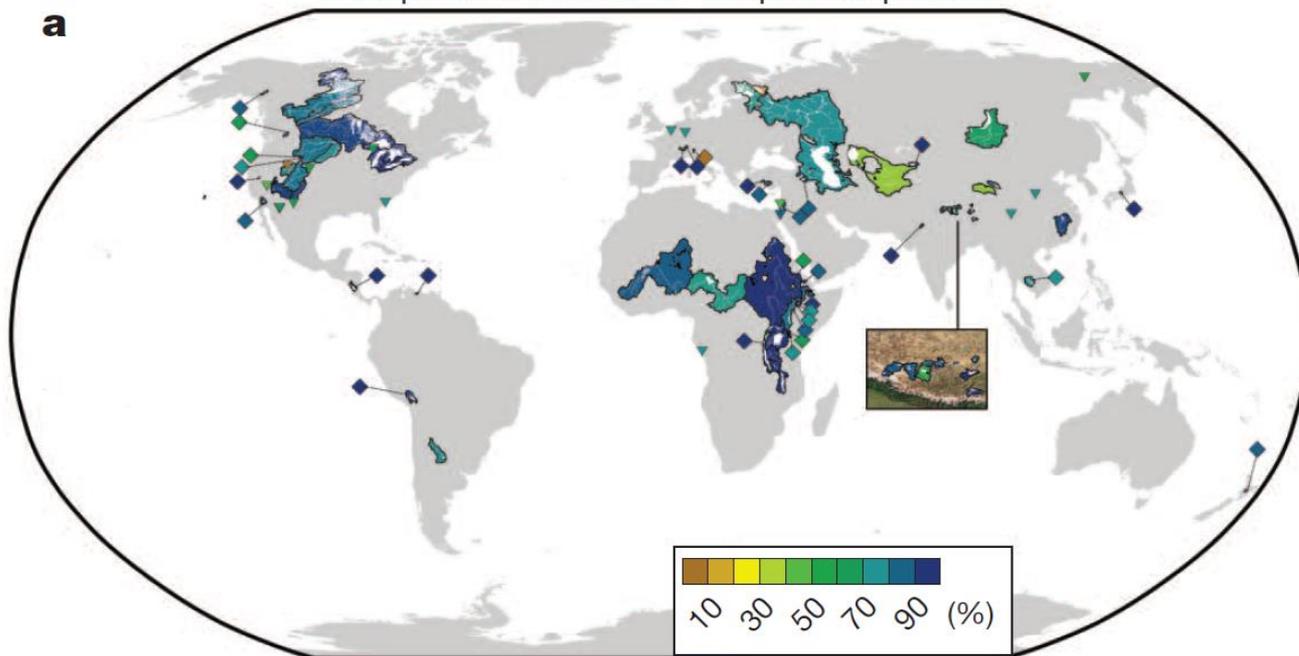
# What about the global scale?



$$T = \frac{I(\delta_I - \delta_E) - Q(\delta_Q - \delta_E) - xP(\delta_P - \delta_E)}{\delta_T - \delta_E}$$

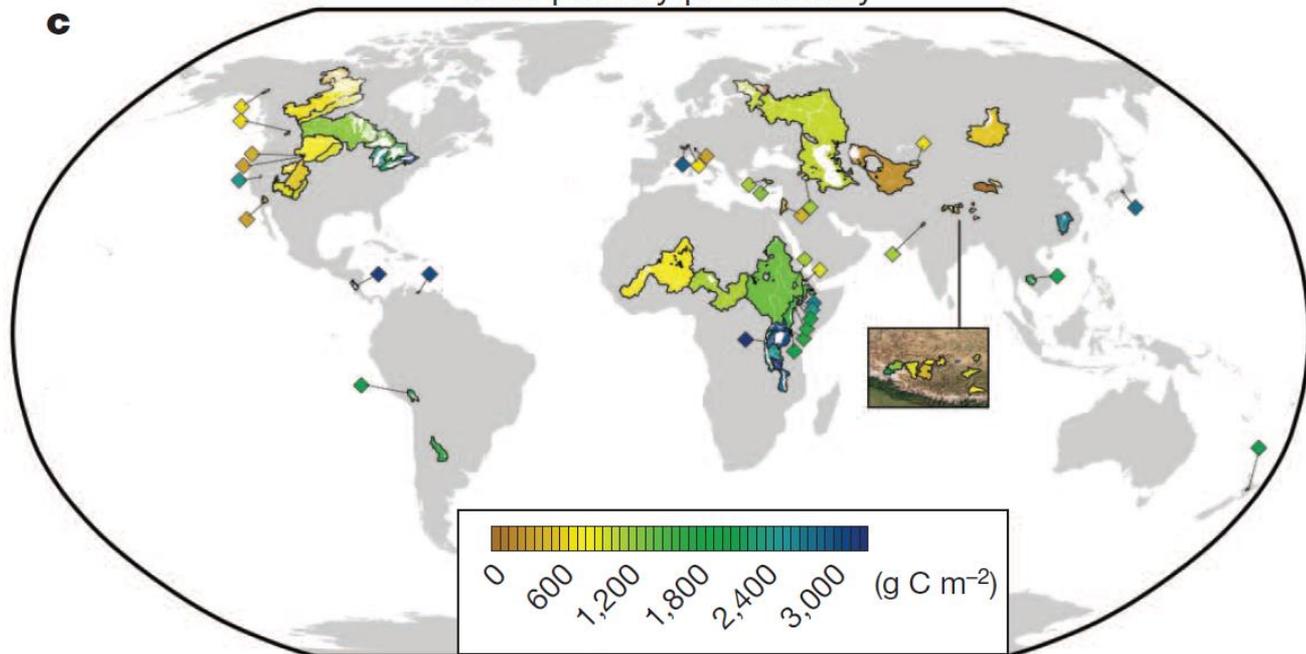
# Transpiration relative to evapotranspiration

**a**



# Gross primary productivity

**c**



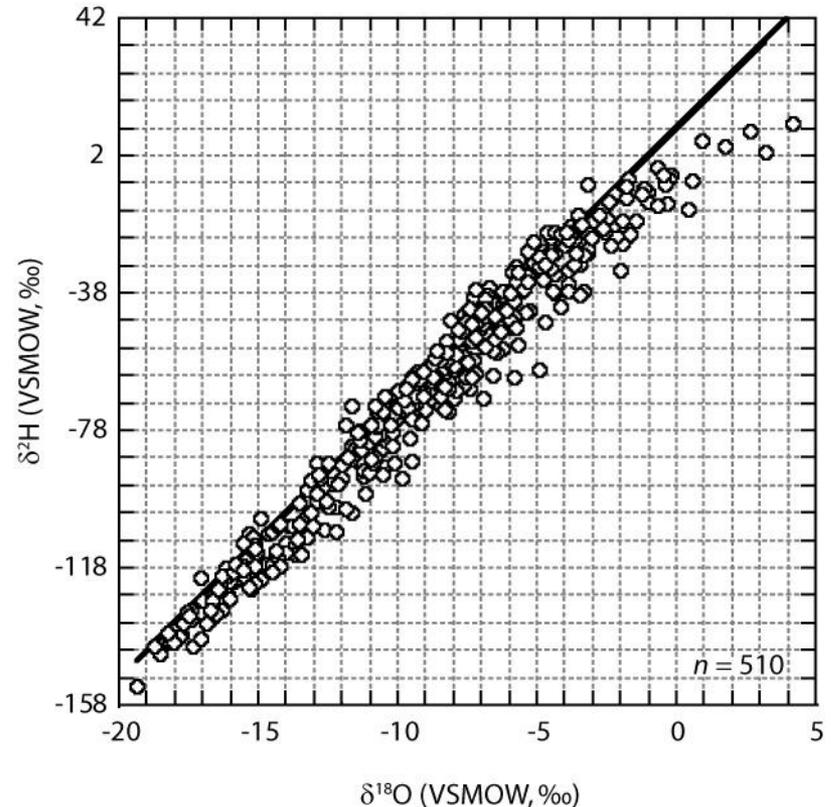
# 9. The water we drink often comes a long way to reach us

- ⊕ Where does your water come from?
  - ⊕ The faucet
  - ⊕ Yes, but...
- ⊕ With spatial information isotopes can
  - ⊕ Establish connectivity
  - ⊕ Document what happens between the source and sink

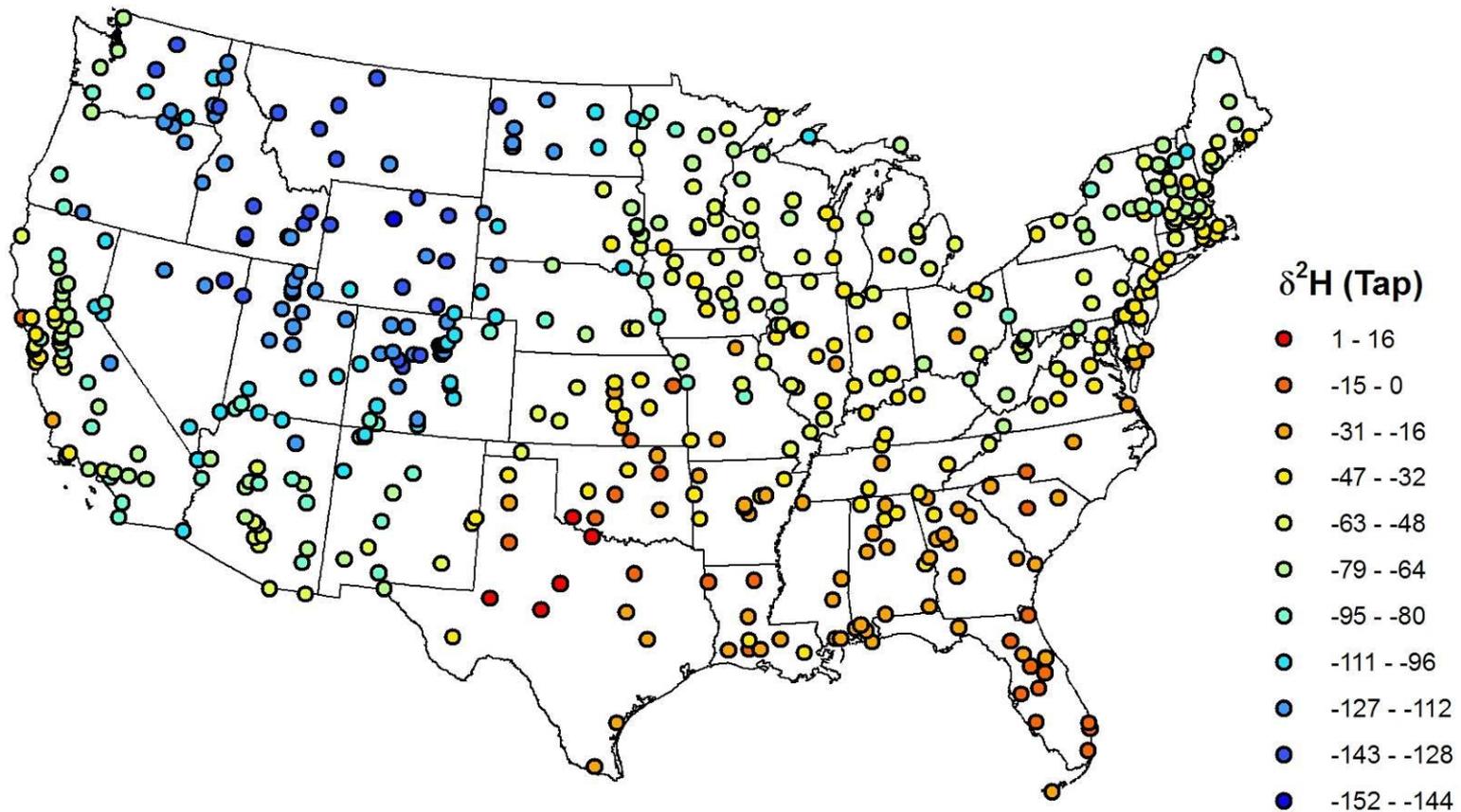


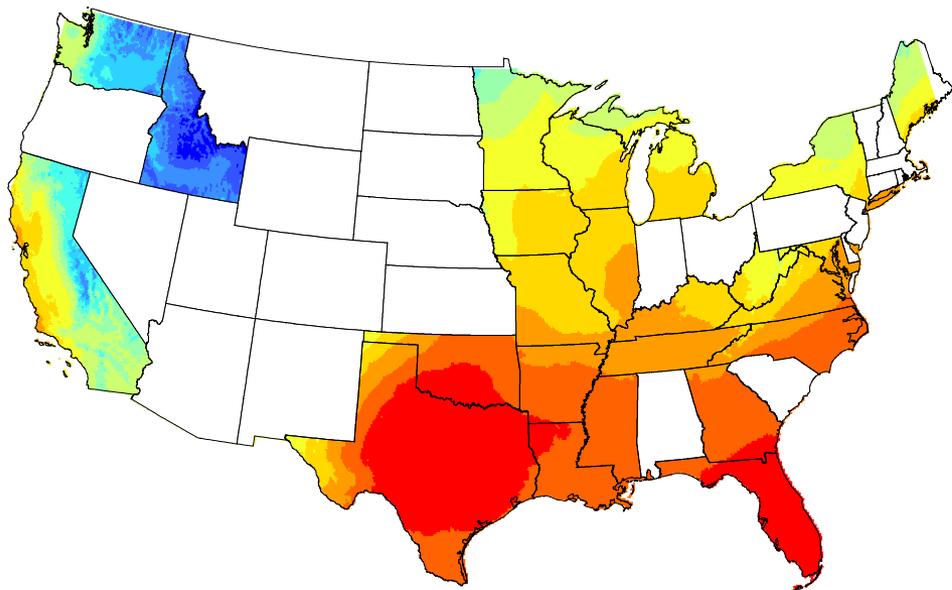
# US tap water isotope ratios

- ✦ Range
  - ✦  $-152\text{‰} < \delta^2\text{H} < +11\text{‰}$
  - ✦  $-19.4\text{‰} < \delta^{18}\text{O} < +4.2\text{‰}$
- ✦ Cluster near the GMWL
- ✦ Average d-excess value of 5 not significantly different from 10

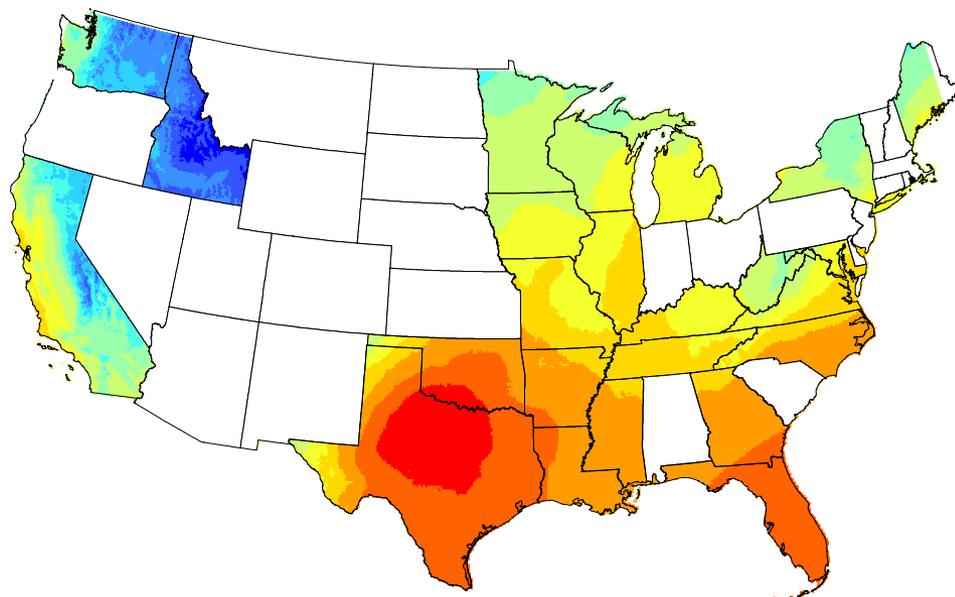
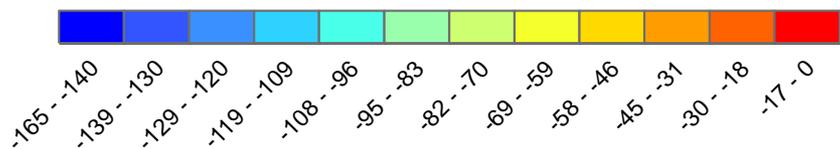


# Isotope ratios of US tap waters

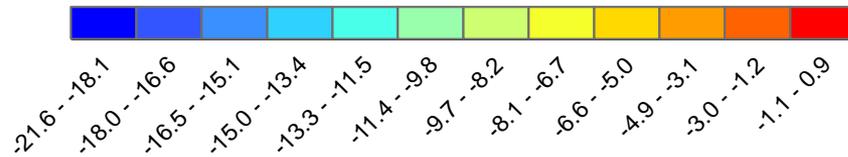




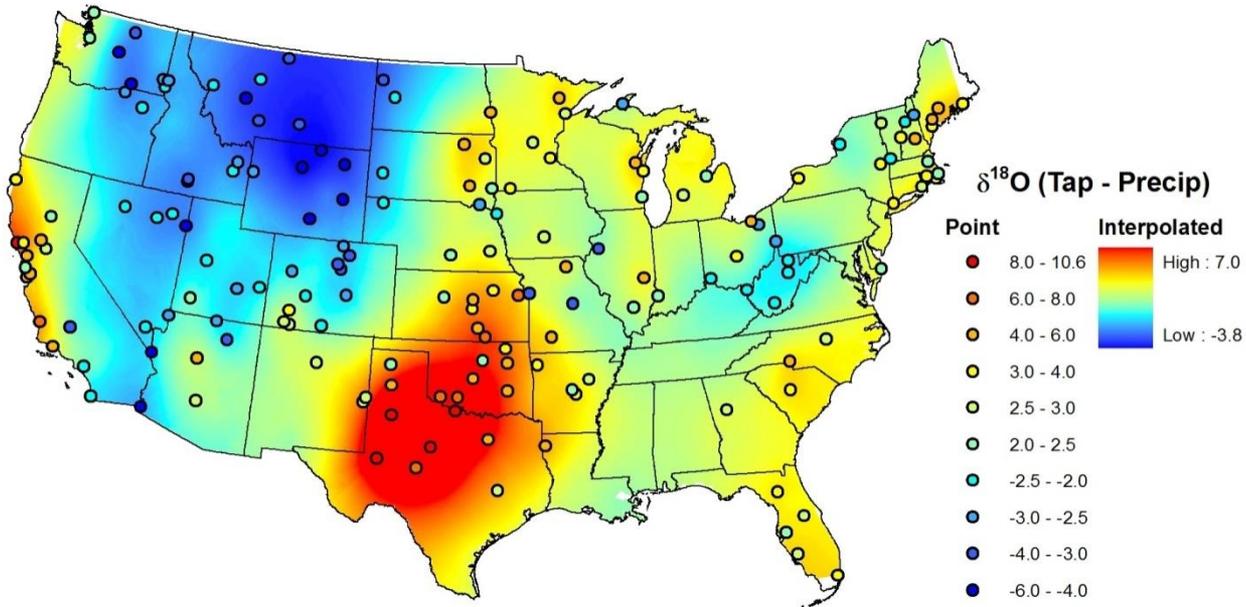
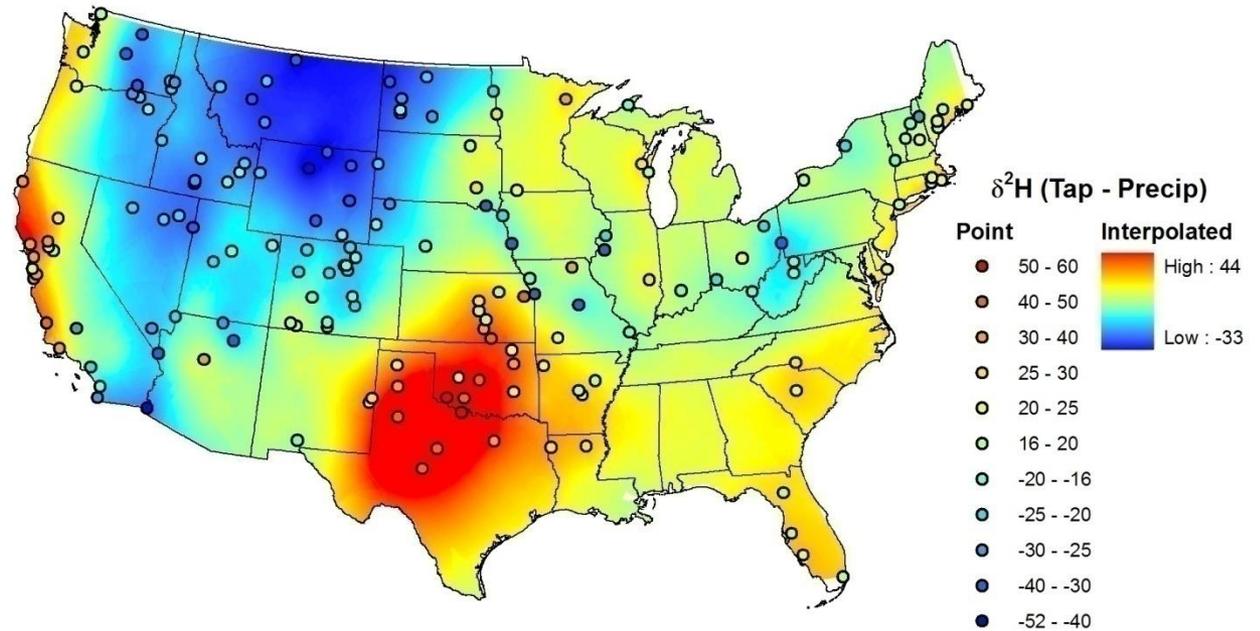
Predicted Tap,  $\delta^2\text{H}$



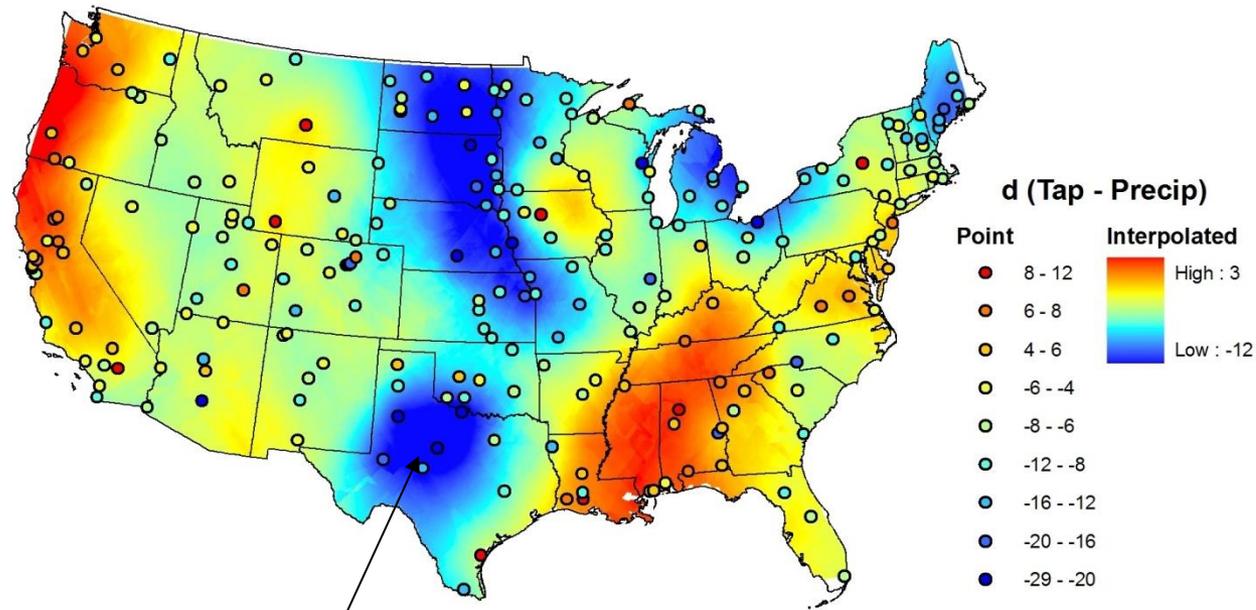
Predicted Tap,  $\delta^{18}\text{O}$



# Tap water vs. local precipitation



# Tap water d values compared to precipitation



20-35%  
evaporative loss

# Catchment areas: source/sink connectivity

- ⊕ Characterize source region for water supply
- ⊕ Map supply footprint of source
- ⊕ Water sinks 1000+ km removed from mean sources

